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Orbit Determination Program Version D

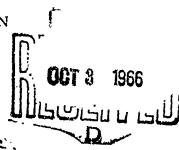
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Prepared by C. C. TONIES, et al Computation and Data Processing Center Electronics Division AEROSPACE CORPORATION



AEROSPACE CORPORATION

Prepared for COMMANDER SPACE SYSTEMS DIVISION
AIR FORCE SYSTEMS COMMAND
LOS ANGELES AIR FORCE STATION
Los Angeles, California



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TRACE ORBIT DETERMINATION PROGRAM VERSION D

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El Segundo Technical Operations AEROSPACE CORPORATION El Segundo, California

September 1966

Prepared for

COMMANDER SPACE SYSTEMS DIVISION AIR FORCE SYSTEMS COMMAND LOS ANGELES AIR FORCE STATION Los Angeles, California

FOREWORD

This report is published by the Aerospace Corporation, El Segundo, California, under Air Force Contract No. AF 04(695)-669. The report was authored by Charles C. Tonies and other members of the technical staff of Aerospace Corporation as part of a continuing support effort extended by the Computation and Data Processing Center to the Satellite Systems Division.

This report describes a computer program which was developed during the period 1 November 1964 through 1 March 1966. The report was submitted on 9 September 1966 to Captain Michael A. Ikezawa, SSTDG, for review and approval.

The computer program (TRACE) has evolved over the past five years at Aerospace Corporation from an original version designed by M. M. Bennett, R. J. Mercer, D. D. Morrison, L. C. Sachnoff, and C. C. Tonies. Subsequent analysis and programming contributions have been made by D. A. Adams, C. C. Christensen, D. E. Groves, R. L. Hale, K. W. Hubbard, A. R. Jacobsen, J. D. Ostlie, A. J. Skulich and, recently, G. Buechler, P. A. Thompson, and D. C. Walker. Much of this material has been collected and revised, with their help, for publication at this time. This TRACE-D document, like the TRACE-D program, is the result of a joint effort.

The contributions of Messrs. Bennett, Hubbard and Mercer require special mention. They have been especially active in TRACE related activities and major parts of this document are due to their efforts. Finally, the editorial assistance provided by Mr. C. R. Feller is gratefully acknowledged; his many hours of diligent and conscientious attention were invaluable.

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Publication of this report does not constitute Air Force approval of the report's findings or conclusions. It is published only for the exchange and stimulation of ideas.

Michael A. IKEZAWA, Capt.

Project Officer, SSTDG

Space System Division
Air Force Systems Command

ABSTRACT

The TRACE-D computer program is designed for use on the IBM 7094 machine as the principal tool in design and analysis studies of all aspects of orbital operations. Its principal characteristics are completeness of the equations of motion, a comprehensive set of differential correction parameters, and the ability to simultaneously process observations of several satellites taken by a number of different types of sensors. The report includes objectives, equations, program structure, and complete instructions for input data preparation and program operation.

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SECTION 1

INTRODUCTION

1.1 OBJECTIVES

The principal value of this document will lie in its usefulness as a technical reference manual and usage guide for people who work with the TRACE-D program. Sections 3 (equations), 4 (program structure), and 5 (usage) are devoted entirely to that purpose. Some theoretical background is given in Section 2 in the interest of technical completeness. The material in Section 1 is presented as an introduction to both the TRACE-D program and the principal problem of concern to those who use TRACE-D.

The basic objective of the TRACE-D Orbit Determination Program (written for the IBM 7094) is to meet the needs of members of the technical staff at Aerospace Corporation for a multipurpose, flexible computational tool for application to problems in orbit analysis. That statement of objective, however, does not fully characterize the program itself. A more interesting and useful statement necessarily includes some description of the specific problems to which the program is addressed, a discussion of program characteristics, and some explanation of how the two are related.

Sections 1.2 and 1.3 therefore include some material related to the nature of the orbit determination problem and to the manner in which TRACE-D is applied. Specific characteristics of the program are given in the context of the problem description. This may be a disadvantage to the reader who wants to know specifically what the program does or does not contain, but subsequent sections, specially Sections 4 and 5, will be useful for this. It is assumed that anyone who is interested in TRACE-D is also interested in the orbit determination problem and in some of the physical considerations and the analytic technique typically associated with the use of TRACE-D at Aerospace Corporation.

Section 1.4 is devoted to a few remarks about future orbit determination programs at Aerospace Corporation.

1.2 GENERAL PROGRAM DESIGN

The idealized design objective for the Aerospace Corporation orbit determination program would be for a nearly automatic computational tool which would provide answers to a wide range of problems relating to orbit and tracking system design, space vehicle performance, and force model analysis. In designing the actual TRACE-D program, however, considerations of automatic operation were relinquished in favor of flexibility. TRACE-D is not a "real time" program. It is used by analysts in a research or investigation environment, and its features are implemented to augment the analytical ability and imagination of its users.

The force model—i.e., the list of accelerations which appear in the equations of motion—is intended to be complete for a near—earth satellite (actually up to six satellites may be treated simultaneously for orbit determination purposes). Since these include atmospheric drag and vehicle originated accelerations and since the entire spectrum of near—earth orbits—all inclinations and eccentricities, and all altitudes up to 100,000 miles—must be considered, numerical integration and the Cowell trajectory formulation are employed. A rather extensive list of observation types is available for input to the orbit determination function or for output in the data generation mode.

1.3 MAJOR PROGRAM FUNCTIONS

The program has four major modes of operation: ephemeris generation or trajectory, orbit determination, data generation, and residuals analysis. These are all related in some direct way to the orbit determination problem, although all the functions are used extensively in solving a variety of associated problems. The characteristics of these four functions and a few specific applications examples are given in Section 1.3.1 through 1.3.4.

1, 3, 1 Ephemeris Generation (Trajectory) Mode

Basic to all TRACE-D functions is generation of a time history of the positions of the orbiting object in inertial space. For example, an ephemeris is necessary to calculate the "computed" or estimated observations that are required

in the orbit determination, data generation, and residuals analysis modes. Hence, every TRACE-D run involves either calculation of an ephemeris for one or more satellites or use of previously generated ephemeris information which has been stored on magnetic tape. In addition, the inertial ephemeris (trajectory) of a satellite, as well as associated quantities such as the ground track and altitude history, often are of interest in themselves.

Given the appropriate input data, the object of the trajectory or ephemeris generation function is to generate the foregoing types of information. The motion of an orbiting object is simulated by numerical integration of the applicable differential equations of motion. Specifically, the equations of motion are represented in the Cowell formulation, wherein the total acceleration vector is expressed as three components in a cartesian coordinate system. The resulting three second-order nonlinear differential equations are integrated directly by using a predictor/corrector technique with time as the independent variable.

The TRACE-D equations of motion include earth geopotential (gravity) effects in the form of a spherical harmonic expansion with provision for zonal harmonic terms J_2 through J_{10} and all tesseral and sectorial terms through $J_{6,6}$. Effects due to other bodies in the solar system (Sun, Moon, Venus, Mars, and Jupiter) are computed from inverse-square-law formulas, and positions of the other bodies are obtained from tabulated coordinates stored on magnetic tape. Acceleration due to atmospheric drag is assumed to be directly proportional to the square of the velocity relative to the air. Atmospheric density is obtained from one of three different model atmospheres that are incorporated in the program.

Instantaneous changes in the inertial velocity vector may be applied at specified times to simulate maneuvers such as orbit adjust or vehicle separation. Also, an included low-thrust acceleration term may be used to simulate thrust tailoff in cases involving large engines, long-term constant thrust, or, in some instances, leaking tanks or valves.

Although the terms of the equations of motion (i. e., the force model) are programmed into TRACE-D, the model which is used on any particular run is to a great extent optional, and the program user may specify terms to be included in calculating the accelerations by means of indicators supplied at the time of program execution. In keeping with TRACE-D programming philosophy of avoiding built-in constants of any kind, all coefficients and arguments in the equations of motion are loaded at execution tir e and may be changed at the discretion of the user.

The TRACE-D trajectory or ephemeris generation mode may be employed for a variety of specific analyses. The comparative listing of associated input and output quantities given in Table 1-1 suggests the range of potential application. Complete instructions for preparation of trajectory mode input data and a sample of a typical trajectory mode output listing are given in Section 5.

1. 3. 2 Orbit Determination Mode

Solving the orbit determination problem is the principal objective of the TRACE-D program, consequently not only is it the most important program feature, but all other major program functions are related to it in some way.

Stated in simplest form, the orbit determination problem consists of extracting information from observations of a satellite in orbit. The observational data typically are gathered by a network of tracking stations on the surface of the earth. The information to be extracted from these data nearly always includes the orbital elements and may include other parameters as well. In the case of TRACE-D, the information extraction process takes the form of a generalized least-squares differential correction procedure.

Because the problems encountered in orbit determination are numerous and varied, comprehensive discussion of all related TRACE-D applications is not possible within the scope of this document. Eather, it is convenient to illustrate the features and characteristics of the TRACE-D orbit determination

Table 1-1. Input/Output Quantities Associated with TRACE-D Trajectory Mode

	Input Data		Output Data
i.	Earth-model constants		Satellite mertial position and velocity in rectangular and spherical coordinates
2.	Atmosphere-model constants		2. Magnitudes of geocentric-radius and inertial-
3.	Solar system constants		velocity vectors
4.	Units conversion factors		3. Latitude and longitude of sub-vehicle point
5.	Numer cal integration-control constants	Items Printed Out	4. Altitude above earth
6.	Epoch time		5. Differences between two trajectories in rectangular, spherical, classical element, and orbit-plane
7.	Position and velocity or orbital elements at epoch time	at Regular	coordinates
8.	Satellite ballistic coefficient	Time Intervals	6. * Time difference between corresponding points of two trajectories
9.	Time, magnitude, and direction of velocity increments		7. * Magnitudes of distance and velocity difference vectors for two trajectories
10,	Interval, amplitude, and decay rate of low thrust		8. ** Partial derivatives of trajectory position with respect to differential-equation parameters
11.	Table of time points where output is to occur		9. ** Differences between changes in position and
12.	Parameter selection indicators	į	velocity produced by perturbing parameters and changes predicted by corresponding calculated partial derivatives
13.	Tape-unit numbers for trajectory differencing		10. At time when vehicle crosses ascending node:
14.	Latitudes and longitudes where special print- outs are to occur Minor option indicators	, , , , , , , , , , , , , , , , , , ,	Output Items 1 through 4 above Classical orbital elements Mean and true anomaly Nodal regression rate
		Items Printed Out at Special	Rate of advance of the line of apsides Apogee and perigee radius and altitude Keplerian, anomalistic, and nodal periods Revolution number Nodal period Nodal period decay Nodal regression Rate of advance of the line of apsides (this set obtained by simple differencing rather than by formula)
		Time Points	11. At the time of the event:
			Crhit adjust magnitude and direction Magnitude of low thrust at start and stop times and at ascending node times
		, [12. At the time when the flight path angle passes through ninety degrees (roughly at apogee and perigee):
			Output Items 1 through 4 above
			13. At the time when the vehicle reaches local maximum or minimum altitude (when h = 0):
			Output Items 1 through 4 above

^{*}Associated with a trajectory differencing.

^{**}Refer to the partial derivatives of trajectory position with respect to selected parameters.

function by outlining the procedure that would be involved in obtaining the solution to a hypothetical but typical problem. For example, a satellite moving for two days in a roughly circular polar orbit (i.e., 90-deg orbital inclination) at an approximately 100-n mi altitude will execute approximately sixteen revolutions around the earth and will come into view of a typical five-station tracking network approximately forty times. Each pass over a tracking station lasts a maximum of about seven minutes, during which time station radar equipment might record range, azimuth, and elevation measurements at 4-sec intervals. A typical TRACE-D application would be to reconstruct the time history of the satellite's position in an earth-centered coordinate system over the entire 2-day period by fitting such a set of tracking observations.

It is important to note that the latter requirement implies the necessity to simulate satellite translational motion over the periods when the vehicle is out of tracking-network view as well as during its passes over the various stations. The TRACE-D program simulates orbital motion by using a model consisting of the differential equations of motion as described in Section 1.3.1. Because these equations define position as a function of time, it is possible to simulate the motion of a ratellite for any time period of interest if initial conditions for the equations are available. Determination of applicable initial conditions from observations of a satellite is part of the TRACE-D orbit determination function.

If the equations of motion for a near-earth satellite, together with associated physical constants, were completely known and if the positions of the tracking stations were exactly identified, then determination of initial conditions, either in terms of initial position and velocity or of any equivalent set of six orbital elements, would constitute a complete solution to a problem such as the previously noted reconstruction of a 2-day period. However, the equations

and their constants can in fact be specified only to a certain degree of accuracy because of such error sources as the following:

- a. Incomplete knowledge of the earth's gravitational field
- b. Dynamic fluctuations in atmospheric density
- c. Extraneous impulses or thrusts originated by a satellite itself
- d. Uncertainties in the geometrical shape of the earth and in locations of tracking stations on its surface
- e. Computing errors accumulated in the solution of the equations of motion

It thus is apparent that determination either of initial position and velocity or of orbital elements is not sufficient to completely define the motion of a satellite at subsequent times, even if their exact values are obtainable.

Although the foregoing factors will always impose a certain degree of inaccuracy on the TRACE-D computational model, its further improvement and refinement remains a continuing objective.

The following sections indicate the manner in which the model problem interacts with orbit determination investigations in general.

1.3.2.1 TRACE-D Applications

One approach that may be adopted by a TRACE-D user when dealing with a problem such as that outlined above is to accept the environment model as programmed and use some "current-best-estimate" set of values for the associated physical constants. The processing then involves determination of initial conditions for the differential equations of motion and possibly of some physical constants directly associated with the satellite system itself.

The seven quantities most frequently determined in TRACE-D applications are the six components of the position and velocity vectors at the beginning of the time interval spanned by the observations and the satellite ballistic coefficient, which is a scale factor associated with acceleration due to atmospheric drag on a vehicle. Because several thousand observations would have been accumulated even with the limited amount of tracking assumed for the sample situation, a least squares approach to the resulting overdetermined system is advantageous. Since it is a safe assumption that overdetermined systems would always arise in connection with TRACE-D applications even though the number of quantities to be determined may be greater than seven and the number of observations fewer than in the above typical example, the least-squares differential correction method has been adopted for TRACE-D purposes. Throughout this document the quantities so determined are conventionally referred to as parameters. This process is illustrated schematically in Figure 1-1, wherein it should be noted that a feedback to the beginning of the process, implying an iterative procedure, is indicated.

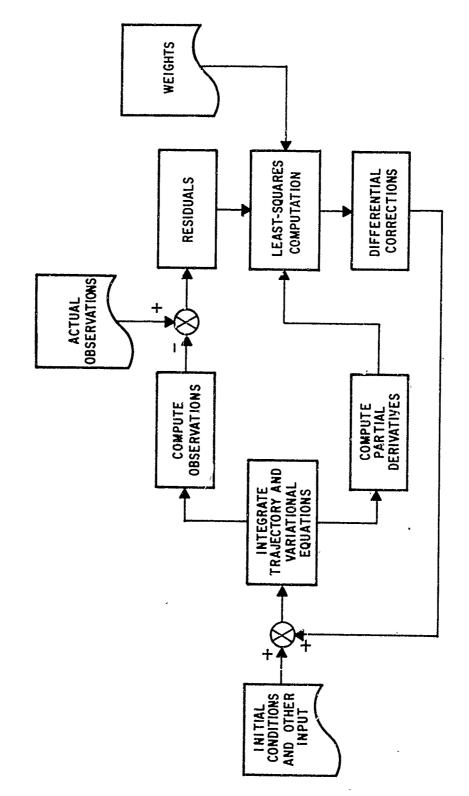
Nearly every TRACE-D application to orbit determination problems requires iteration because of the usual reason that linear techniques are used to approximate a process which inherently is nonlinear. The iteration process ordinarily is continued until the residuals (i. e., the differences between the actual observations and the computed observations) are minimized in the weighted least-squares sense. A "one-batch" processing approach is used, wherein all observations to be fit are processed (i. e., residuals and corresponding partial derivatives are computed) before corrections to the parameters are computed.

C:

Available TRACE-D parameters are itemized in Section 1. 3. 2. 2 together with characteristics of the other major features of the orbit determination function.

1. 3. 2. 2 Specific Features of the Orbit Determination Function

The following listings of specific features and options of the TRACE-D orbit determination function are given for convenient reference as well as to characterize more clearly the environment of the orbit determination problem. Complete explanation of TRACE-D program operation is given in Section 5.



5 h

Figure 1-1. Schematic Diagram of Least-Squares Differential Correction Process

1. 3. 2. 2. 1 The Force Model

The satellite is assumed to move in an environment in which the following physical forces may be acting:

- a. Gravitational attraction of the earth (zonal harmonics through J₁₀ and tesseral harmonics through J₆, 6 are included.)
- b. Atmospheric drag (three density models are incorporated in the Trace-D program.)
- c. Gravitational attraction of other bodies in the solar system
- d. Vehicle-originated forces (instantaneous changes in velocity (kicks) and a low-thrust effect of exponential form are available.)

Inclusion of any of these types of forces or of any subset is completely under the control of the program user through input options.

1. 3. 2. 2. 2 Parameter List

TRACE-D is programmed to determine by differential correction the following quantities:

- a. Initial position and velocity components in either spherical, rectangular, or classical element form for up to six independent orbital arcs
- b. Reciprocals of ballistic coefficients (CDA/W) for up to six different satellites
- c. Up to six velocity increments (kicks) for one satellite
- d. Amplitude and time constant for an exponentially decaying low thrust
- e. Zonal harmonic coefficients J₂ through J₁₀ and all tesseral harmonics J_{2,1} through J_{6,6}
- f. Constant biases on all types of observations
- g. Scale factors for range and range-rate observations
- h. Time biases (i. e., biases in reported times at which observations were made)
- i. Latitudes, longitudes, and altitudes above sea level of up to 100 observing stations

On any one computer run any set of the foregoing quantities may be selected as parameters to be determined by means of differential correction, subject to a maximum limit of sixty items from items a through e above and a maximum of one hundred items total.

1. 3. 2. 2. 3 Observation Types

The following types of observations are accepted by TRACE-D:

- a. Slant range
- b. Local azimuth
- c. Local elevation
- d. Topocentric right ascension
- e. Topocentric declination
- f. Topocentric hour angle
- g. Geocentric right ascension
- h. Geocentric declination
- i. Horizon sensor outputs
- j. Altitude above the earth
- k. Earth-fixed geocentric rectangular coordinates
- l. Range rate
- m. Differences in range and range rate between two stations

1. 3, 2. 2. 4 Residuals Editor

Each time an iteration is carried out, the residuals are subject to an editing criterion. In general terms, the criterion is determined by the root-mean square (RMS) value for all residuals on the previous iteration which carried the appropriate tracking station and observation-type identifiers. For example, the RMS value of the residuals for range data from Station A is used to edit the range residuals for Station A on the subsequent iteration. An important by product of this process is the printed RMS of the residuals by station and by observation type, or even by pass and observation type, at the end of each iteration.

1. 3. 2. 2. 5 Weights

In general, observations are given a priori weights by station and observation type. The twofold purpose of the weights is to normalize units so that different types of observations may be mixed in the least-squares process and to adjust their relative influence in the process of fitting observations of different accuracies. An important example of use of weights is zero weighting. If observations from a certain source are given zero weights they will have no influence in determining the values of the parameters, but corresponding residuals will appear and the RMS summary of residuals will be given. Non-zero weights may be thought of as divisors—the smaller the number, the greater the influence of the associated observations.

1. 3. 2. 2. 6 The Correlation Matrix

A by-product of the least-squares process is the inverse normal matrix. If certain assumptions are made regarding the statistical properties of the observation errors and the linearity of certain partial derivatives, this matrix may be interpreted as a variance/covariance matrix for the parameters.

A correlation matrix is computed from the inverse normal matrix by the program. Premised by the same assumptions, elements of this matrix may be interpreted as a measure of the correlation among parameter estimates.

1. 3. 2. 3 TRACE-D As An Analytical Tool

Additional insight into the use of TRACE-D as a tool for analysis of satellite motion may be gained by further consideration of the 2-day arc-fitting problem discussed above. Assuming the previously described seven-parameter fit approach were adopted as a typical first step, the program would be put into execution and the least-squares differential correction process would be continued to convergence, which in practice is obtained when no significant further reduction in the numerical value of the RMS of all weighted residuals is obtainable. It is important to realize that corrections to the parameters

do not become arbitrarily small near convergence in accordance with theoretical prediction, but that the very best that can be expected in reduction of correction size is to approach the level of round-off error. Often it is not possible to obtain even this degree of resclution because of contributions from other error sources such as those previously itemized in Section 1. 3. 2, and because the parameters are correlated--correction to one may be partially equivalent to correction to another.

The interaction of convergence behavior and a typical model error may be illustrated by supposing that convergence occurs somewhat more slowly than experience would indicate for this type of fit, requiring perhaps six iterations (no more than three would normally be involved with correct model selection and all data consistent), and that convergence resolution also was poor; i. e., the magnitudes of the corrections with respect to the parameters remain large when the residuals RMS value has apparently reached its lowest value. Using output from the final iteration for construction of corresponding residual patterns, plots of range data residuals versus time, for example, might be of the general form shown in Figure 1-2, where each graph represents one pass (approximately four minutes) over some radar station and obviously exhibits a systematic pattern in addition to the expected random noise.

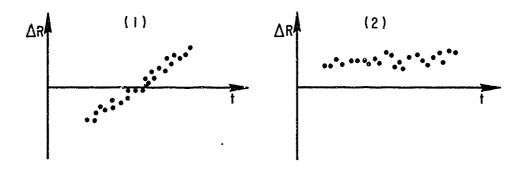


Figure 1-2. Typical Plots of Range Data Residuals

It should be noted that in this case the magnitudes of residuals for all other types of observations would be found to be large compared to the known quality of the data, and also that all the patterns of residuals versus time would be systematic.

Although the values of the initial conditions and drag parameters given by the last iteration of the run could be accepted as the solution at this point, the fact that something is obviously not right with the fit would indicate that an ephemeris derived from those parameters could not be expected to be very accurate. Consequently, the first step that might be applied by experienced analysts in this situation would be to determine whether some bad data have been included in the fit, since a batch of observations that are completely inconsistent with all others present will prevent acceptable convergence. Ordinarily a check of the listing of residuals produced on the last iteration of the run will serve to answer this question since residuals for observations that are grossly inaccurate will stand out by virtue of magnitude provided that the majority of the data are not grossly inaccurate. If a group of offending observations is detected, it may of course be deleted, which is the usual procedure if the bad data constitute a small fraction of the total set and if the reason for the poor quality is either known or not of interest.

In cases where a significant amount of data appears to be in error, additional investigation is usually required. The listing of residuals will often reveal correlation between large residuals and a station designation, which would occur when a station is reporting especially noisy or biased observations, when the station clock is inaccurate, or when the specified station location is incorrect. Careful examination of plotted residuals patterns on a pass-by-pass basis often supplies a clue as to the nature of the trouble, as in the case of the two residuals plots shown in Figure 1-2, which suggest a time bias and a range bias, respectively. However, it is not possible to conclude immediately that such biases are indeed present in the data because patterns such as the two shown may also be explained in terms of other error sources.

At this point the job of the analyst thus becomes one of accumulating evidence with respect to various hypotheses concerning the characteristics of his observation set. If the accumulated evidence supports the hypothesis that one station did indeed have a bias in the range system, for instance, a rangebias parameter for that station may be selected on the next run. Usually such a parameter is added to the list of parameters previously adopted, which in this case would make the run an eight-parameter fit. Similar discussion also is applicable to the other bias and scale-factor parameters previously itemized in Section 1.3.2.2.2, a number of which might be selected for a single run. TRACE-D will adjust these factors by differential correction and automatically apply them to corresponding observations on each iteration.

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If inspection of the residuals listing suggests a station location error, some combination of latitude, longitude, and altitude parameters for that station is selected on a subsequent run and the location of the station is shifted by the program on each iteration as it attempts to minimize the residuals. The ability to determine the location of a tracking site from satellite observations has proved to be very useful, especially in cases where the site is remotely located and ground surveys are difficult to undertake.

If no strong evidence of systematic errors in the observations or station locations is apparent, the manner in which the programmed force model may differ from the real environment experienced by the satellite must be evaluated.

The necessarily inaccurate nature of the programmed models, stemming from incomplete present knowledge of real world forces, is manifested by systematic residuals patterns remaining at convergence in most of the current cases of TRACE-D orbit determination applications involving orbital arcs of more than a few revolutions. Thus it is not expected that residuals would be reduced to the level of random noise by a seven-parameter fit to observations over a 2-day arc. It therefore would be necessary for an analyst to decide by inspecting the magnitudes of the final residuals whether or

not they may be attributed to the estimated deficiencies in his model. If so, the choice would be either to accept the parameter solution or to proceed to refine the model itself by differential correction.

If residuals remain above the noise level, further significant information may still be extracted from the observation set, at least in theory. (In fact, if residuals were reduced to noise level, further information might even be extracted by means of statistical inference.) In an alternative sense, the matter may be visualized as a circumstance wherein, if the program is given additional degrees of freedom or parameters that it can adjust, the residuals will be reduced and the values of the additional parameters—model constants in this case—presumably will be improved. For example, the latter general motivation has led to inclusion of all programmed geopotential harmonic coefficients among available TRACE—D parameters.

It should be pointed out again, however, that the program user is not usually free to select simultaneously all the parameters which he may wish to determine. Parameters generally are correlated with one another; i. e., an adjustment to the value of one will result in changes in the residuals nearly identical to changes caused by an adjustment to another. The program therefore has no means by which to discriminate between parameters in computing differential corrections, and poor convergence behavior results. Given observations associated with only one orbital arc, for example, it is possible to estimate only a very limited number of geopotential parameters.

Another significant error source derives from the atmospheric density models programmed into TRACE-D, one of which is selected by the user to account for effects of atmospheric drag. The error arises because the programmed density models do not truly represent actual environment at 100-n mi altitude for instance. In this case the modeling problem is generally more difficult than that associated with the gravity field because the physical processes are dynamic, complicated, and partly unknown, and the

indices used to characterize the process are difficult to measure. Nevertheless, experienced analysts will be aware of the magnitudes of residuals that reasonably may be attributed to atmospheric uncertainties. Such judgment will be facilitated to some degree by the availability of the values of the above-noted indices, since they will serve to indicate whether or not the real atmosphere was undergoing any major perturbation such as a magnetic storm during the period when the satellite of interest was in orbit.

Use of the drag parameter, allowing the program to differentially correct the inverse ballistic coefficient, is equivalent to finding the best average density for observation-fitting purposes. Later versions of the TRACE-D program will also include additional atmosphere model parameters whose differential correction may help to reduce further the effects of uncertainties in atmospheric density. However, to the present time, the drag parameter technique has proved effective even for such demanding applications as using data from satellite observations for studying the geopotential field at 100-n mi altitudes.

One further major aspect of the model problem may be illustrated by supposing that the residuals printout reveals no obvious questions associated with the observations themselves even though the residuals magnitudes are much larger than can be attributed o uncertainties in the gravity and atmosphere models. If such a condition were to occur in combination with the poor convergence assumed for the original seven-parameter fit, the next logical hypothesis would be that the motion of the satellite was influenced by some phenomenon that was not included in the chosen model. An obvious candidate would be some force originated by the vehicle system itself, for instance thrusting by an on-loard system.

An intentional maneuver involving on-orbit thrusting would not be considered in this connection because it would have been simulated as part of the computed trajectory in the original fit. However, this does not preclude the unknown force assumed to be operating on the real satellite from also being a thrust, inasmuch as an unanticipated expulsion of material from any satellite-vehicle assemblage might result in application of a net impulse to the center of gravity of the satellite. If the satellite were injected into orbit by an engine that remained attached to the orbiting payload, the payload might be subjected to continued low-level thrusting by the engine following its shutdown at time of injection, for example, because of imperfect propellant valves. Another possibility would be development of a small leak in some pressurized tank during injection, since the cumulative effect of fuel escaping through a pinhole-sized leak in a fuel tank would easily be detectable in the motion of a satellite as measured by ground tracking systems.

One method for testing the extraneous-thrust hypothesis would be to use the time bias parameters available in TRACE-D, originally included in the program to search for and remove biases in reported observation times (i. e., station clock errors) but currently used much more extensively to aid in identifying model discrepancies. Under this procedure, observations from each pass over each station are uniquely identified. A fit permitting derivation of a time bias parameter for each pass is then made. Since the principal measureable effect of a model error usually becomes apparent as discrepancies in time of arrival at given points along an orbit, the time bias parameters offer a way for the program to reduce the residuals artificially by finding an adjustment to the reported observation times for each pass (one constant time bias for all observations from a given pass) and automatically applying this adjustment to the observation times. A plot of the time bias values versus revolution number for the present hypothetical case might appear as shown in Figure 1-3. In this connection it must be remembered that the time bias values are not actual errors in the observations, but are empirical factors introduced by the program for the purpose of fitting observations to the model used.

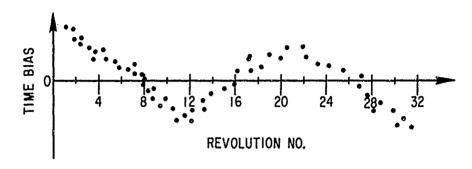


Figure 1-3. Plot of Time Bias Values Versus Revolution Number for Fit of Revolutions 1 Through 32

The plot of Figure 1-3 reflects two distinct segments in that Revolutions 1 through 11 show a monotonically decreasing pattern whereas Revolutions 12 through 32 show a concave arc. Since it is known from experience that the curved arc shape is produced when the program is forced to fit with the wrong drag factor and since drag was a parameter in the original fit, it must be true that a single value of drag would not fit both segments and that the plot in fact appears to represent two different orbits.

The next step would be to fit one of the segments at a time. Revolutions 12 through 32 would be the logical choice since a seven-parameter fit over that interval would converge quickly, final corrections would be small, and residuals would be acceptable. If the hypotheses were correct and the solution from this run were used to solve for time biases as before, a plot would then take the form shown in Figure 1-4.

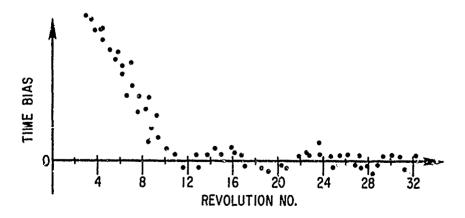


Figure 1-4. Plot of Time Bias Values Versus Revolution Number for Fit of Revolutions 12 Through 32

On the other hand, an attempt to fit Revolutions 1 through 11 with seven parameters would meet with little success since, again, convergence would be slow and it would not be possible to reduce the residuals to a desirable level.

Analysis and some intuitive deduction lead to the conclusion that the trouble on Revolutions 1 through 11 must be a continuous low thrust, probably caused by a leak that stopped somewhere on Revolutions No. 11 or 12. Since TRACE-D incorporates a low-thrust acceleration option with two associated parameters, a subsequent fit over all 32 revolutions, with the low thrust added to the model for the interval through Revolution 11, would yield the desired solution to the fitting problem.

Once the initial-condition, drag, and thrust parameters have been determined, they may be input to the TRACE-D trajectory function to produce a complete time history of position together with associated quantities such as the ground track and altitude above the earth, as described in Section 1. 3. 1.

1.3.3 Data Generation

As noted in Section 1. 3. 1, the TRACE-D trajectory, or ephemeris generation, function is a means for computing the path of an orbiting vehicle in inertial (space-fixed) coordinates as well as the associated ground track and other related quantities. However, no information directly related to the tracking problem is produced in the trajectory mode. The object of the data generation function therefore is to generate various forms of simulated observation measurements from a given definition of the ephemeris of a vehicle and the locations of observing stations on the earth's surface.

The most frequent application of the TRACE-D data generation feature is associated with visibility considerations. When and how long each of the tracking stations would see a particular satellite might be determined for a certain given set of burnout conditions for a launch from a particular launch

site. If associated measurements, for example, of range, azimuth, and elevation readings as functions of time also were needed, input of the appropriate indicators would produce data at whatever time frequencies were desired.

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Such simulated data may either be punched on cards in appropriate format for input to the TRACE-D orbit determination function or be written on magnetic tape for subsequent input to an orbit determination run. These options are oriented toward the typical application of generating simulated data to be fit with TRACE-D in connection with orbit determination feasibility studies and error analyses. Experiments in convergence behavior, for example, may be conducted by producing simulated observation sets with various bias, noise, and distribution characteristics and then observing the influence of these factors upon convergence speed and resolution in the orbit determination mode. Fitting data with a force model different from the one used to generate the data is another typical activity providing insight into the real-world problem of fitting actual observations with a programmed force model that is always less than perfect.

Required input to the data generation function includes force model definition, epoch conditions, tracking station locations, and specifications defining the types and frequency of the data to be generated for each station. Items to be output are selected by the user through input indicators. Among available output items are all observation types accepted by the TRACE-D orbit determination function, uncertainties in certain observations as determined by uncertainties in orbit elements, indication of mutual visibility between two tracking stations, satellite ground track coordinates, and aspect angles associated with orientation of on-board antennas. A detailed list of data generation output quantities is shown in Table 5-5.

Special features of the data generation mode include:

- a. A minimum-output option which allows computation and printing only of quantities associated with rise (initial visibility) time, maximum elevation angle incidence, and set (loss-of-visibility) time
- b. An option to write generated observations on magnetic tape in card image format
- c. Capability to compute satellite attitude in terms of pitch, roll, and yaw angles referenced to the local vertical and in-track directions
- d. Optional addition of random noise and biases to generated observation data

1.3.4 Residuals Analysis

One of the end products of a TRACE-D orbit determination run is a group of residuals (differences between the actual observations and the values corresponding to the derived ephemeris). Because errors in both the observations and the program model are significant in typical TRACE-D orbit determination applications, residuals remaining after a final iteration are an important source of information for program users, as previously suggested in Section 1.3.2.

Formation of residual vectors for certain types of residuals and rotation of these vectors into an orbit-plane coordinate system, where the vector components may be more easily associated with the direction of satellite motion, is a device that often facilitates analysis of data system malfunctions and model effects. The residuals analysis function accomplishes these operations and also provides statistics such as the RMS of residuals in terms of the rotated vector components.

Residuals analysis input data and usage are essentially the same as for the orbit determination mode except for the following special operating features:

a. In normal mode the residuals analysis link computes observations from ephenieris information supplied via tape. These observations are then subtracted from the

actual observations to form the residuals. Alternatively, the "computed" observations may be supplied directly to provide a means for differencing either sets of actual observations or possibly sets of observations generated by other computer programs.

- b. An edit and punch option permits a set of observations to be subjected to a residuals-editing criterion, after which a revised deck of observation cards is punched. The new deck includes only those measurements which passed the editing test.
- c. Ephemeris points may be treated in the same way as observations in that they may be differenced and the resulting difference vectors resolved into orbit-plane coordinates. For example, ephemeris differences for two orbit reconstructions obtained by using the same observations but different models may be generated. This feature is frequently used at Aerospace Corporation to compare ephemeris tapes generated by orbit determination programs other than TRACE-D.

1. 4 THE FUTURE OF TRACE-D

Among the most significant modifications and additions to the basic or reference version of the TRACE-D program that are now in preparation are the following:

- a. An additional atmosphere model (identified as the Jacchia-Nicolet model at Aerospace Corporation) which computes density values based on actual measured values of magnetic and radiation flux indices. Seventeen constant coefficients of the model are available as parameters.
- b. Additional geopotential terms which will provide a means for investigating resonance phenomena (i. e., resonance associated with orbital period and rate of earth rotation)
- c. An option to sort residuals by station and observation type before printing
- d. Interpolation for impact time and location
- e. Availability of fifty orbit-adjust events (not parameters) in addition to the six events that are available as parameters in the reference version
- f. A lunar orbiter mode
- g. Many minor additional output items and format improvements

TRACE-D will become obsolete at the end of 1966 and will no longer be used at Aerospace Corporation. Documentation describing all program modifications will be published at that time which, in conjunction with this document, will completely define the terminal TRACE-D program.

A new program designated TRACE-66, to be operated in the Chippewa Operating System FORTRAN programming language, is being written at Aerospace Corporation for the CDC 6600 computer. The first operating version of TRACE-66 is expected to be in use at Aerospace Corporation in the Fall of 1966 and a full production version, together with supporting documentation, is expected to be available early in 1967. The first reference manual for the TRACE-66 program will be published at that time.

SECTION 2

THEORY

2. 1 INTRODUCTION

2.1.1 General

Section 2 develops some mathematical statements of the various TRACE-D applications to orbit determination problems previously identified in Section 1. Section 2 emphasizes theoretical aspects and functional relations; Section 3 presents the specific equations and methods used in the TRACE-D program.

The applications treated in the following analysis are considered in order of increasing scope, but not in uniform Cepth. Thus, less familiar topics are emphasized, but more usual problems such as the numerical solution of differential equations are largely ignored.

2.1.2 Derivative with Respect to a Vector

The indication of a derivative with respect to a vector is a very convenient notational device for representing partial derivative matrices and chain rule differentiation. In this connection, the following conventions are observed throughout this document:

- a. The term "vector" denotes a column vector. A row vector is described as such or denoted as a transposed vector (for example, $(x, y, z) = X^{T}$).
- b. The derivative of a vector with respect to a scalar is a vector.
- c. The derivative of a scalar with respect to a vector is a row vector.
- d. The derivative of a vector with respect to a vector is a matrix (for example, if F is a vector function of a vector variable X, then $\partial F/\partial X$ is the matrix of partial derivatives whose i-jth element is $\partial F_i/\partial X_i$).

The neatness of this approach is exemplified by assuming X(t) is the vector $[x_1(t), x_2(t), \dots, x_n(t)]^T$ and y is a scalar function of X, or $y = f[x_1(t), x_2(t), \dots, x_n(t)] = f[X(t)]$. Differentiating then leads to

$$\frac{dy}{dt} = \frac{\partial f}{\partial x_1} \frac{dx_1}{dt} + \frac{\partial f}{\partial x_2} \frac{dx_2}{dt} + \cdots + \frac{\partial f}{\partial x_n} \frac{dx_n}{dt} = \frac{\partial f}{\partial x} \frac{dx}{dt}$$
 (2-1)

where $\partial f/\partial X$ is by convention a row vector, dX/dt is a column vector, and their juxtaposition indicates the scalar product.

2.2 THE TRAJECTORY AND ITS PARTIAL DERIVATIVES

The trajectory of a space vehicle is described by the differential equation of motion

$$\ddot{X} = -\frac{\mu X}{r^3} + F \tag{2-2}$$

with the initial values

$$X(t_0) = X_0$$
, $\dot{X}(t_0) = X_0$

where

X = 3-vector of rectangular components of position (x, y, z) in an inertial coordinate system

$$r = |x| = (x^2 + y^2 + z^2)^{1/2}$$

 μ = product (GM) of the Newtonian gravitational constant and mass of the earth

F = acceleration vector resulting from perturbing forces; i.e., all forces other than the inverse square central force due to gravitation.

One application of TRACE-D is the solving of the foregoing differential equation. The solution X(t), $\dot{X}(t)$ is generated numerically at time points $t = t_i$ (j = 0,1,2,...) and defined at $t \neq t_i$ by an interpolation formula.

More sophisticated TRACE-D applications additionally require the sensitivity, as expressed by partial derivatives, of the trajectory to its initial conditions and other parameters.

It is obvious that \ddot{X} is a function of μ , which is an example of a "differential-equation parameter." Other parameters of this nature, such as ballistic or oblateness coefficients, also may appear in F. The solution depends on the initial conditions X_0 and \dot{X}_0 , which in turn may be computed from "initial-condition parameters." Letting vectors of these types of parameters be represented by β and α respectively, the functional relations associated with Eq. (2-2) may be written

$$\ddot{X} = -\frac{\mu X}{r^3} + F(X, \dot{X}, \beta, t)$$
 (2-3a)

or

$$\ddot{X} = \ddot{X}(X, \dot{X}, \beta, t) \tag{2-3b}$$

in conjunction with the initial conditions

$$X(t_{o}) = X_{o}(a)$$
 , $\dot{X}(t_{o}) = \dot{X}_{o}(a)$

It should be noted that F and X will be functions of X whenever drag forces are present.

The dependence of the solution upon applicable parameters may be indicated by

$$X(t) = X(\alpha, \beta, t_0, t)$$
 , $\dot{X}(t) = \dot{X}(c, \beta, t_0, t)$

Thus, the solution also can be given by the integral equations

$$\dot{\mathbf{X}}(\alpha,\beta,t_{o},t) = \dot{\mathbf{X}}_{o}(\alpha) + \int_{t_{o}}^{t} \ddot{\mathbf{X}}[\mathbf{X}(\alpha,\beta,t_{o},t''),\dot{\mathbf{X}}(\alpha,\beta,t_{o},t''),\beta,t'']dt''$$

and

$$\begin{split} X(\alpha,\beta,t_{o},t) &= X_{o}(\alpha) + \int_{t_{o}}^{t} \dot{X}(\alpha,\beta,t_{o},t')dt' \\ &= X_{o}(\alpha) + (t-t_{o})\dot{X}_{o}(\alpha) \\ &+ \int_{t_{o}}^{t} \int_{t_{o}}^{t'} \ddot{X}[X(\alpha,\beta,t_{o},t''), \dot{X}(\alpha,\beta,t_{o},t''),\beta,t'']dt''dt' \end{split}$$

The double integral form may be reduced to a single integral form (see Ref. 2 for intermediate steps):

$$X(t) = X_{o}(\alpha) + (t - t_{o})\dot{X}_{o}(\alpha)$$

$$+ \int_{t_{o}}^{t} (t - t'')\ddot{X}[X(\alpha, \beta, t_{o}, t''), \dot{X}(\alpha, \beta, t_{o}, t''), \beta, t'']dt'' \qquad (2-4)$$

Although they are generally unsuitable for computations, the integral expressions are of value for showing the involved functional relations explicitly.

It is now possible to show how the partial derivatives $\partial X/\partial a$, $\partial X/\partial \beta$, and $\partial X/\partial t_0$, which measure to first order the sensitivity of solutions to variations in the trajectory parameters a, β , and t_0 , are obtained. In addition to their extensive use in numerous TRACE-D applications, the physical interpretations of these partial derivatives often are of independent interest.

Differentiating Eqs. (2-3a) and (2-3b) with respect to α , interchanging orders of differentiation, and using the notation X_{α} for $\partial X/\partial \alpha$ leads to

$$\ddot{\mathbf{x}}_{\alpha} = \left[\frac{\partial}{\partial \mathbf{X}} \left(-\frac{\mu \mathbf{X}}{\mathbf{r}^3} \right) + \frac{\partial \mathbf{F}}{\partial \mathbf{X}} \right] \mathbf{x}_{\alpha} + \frac{\partial \mathbf{F}}{\partial \dot{\mathbf{x}}} \dot{\mathbf{x}}_{\alpha}$$
 (2-5)

vith initial conditions

$$X_{a}(t_{o}) = \frac{\partial X_{o}}{\partial a}$$
 , $\dot{X}_{a}(t_{o}) = \frac{\partial \dot{X}_{o}}{\partial a}$

Equation (2-5) is called a "variational equation," and is a second-order linear vector differential equation whose solution is the vector of partial derivatives $X_{\alpha} = \partial X/\partial c$ of the components of position with respect to the initial condition parameter α . In the course of solving Eq. (2-5), $\dot{X}_{\alpha} = \partial \dot{X}/\partial \alpha$ will also be obtained. A similar equation can be derived for each initial condition parameter.

Equation (2-5) also may be obtained by differentiating the integral, Eq. (2-4), with respect to a to give

$$X_{\alpha} = X_{\alpha}(t_{o}) + (t - t_{o})\dot{X}_{\alpha}(t_{o}) + \int_{t_{o}}^{t} (t - t'') \left(\frac{\partial \ddot{X}}{\partial X} + \frac{\partial X}{\partial \alpha} + \frac{\partial \dot{X}}{\partial \dot{X}} + \frac{\partial \dot{X}}{\partial \alpha}\right) dt'' \qquad (2-6)$$

It should be noted that Eq. (2-6) corresponds to Eq. (2-5) in exactly the same way that Eq. (2-4) corresponds to Eq. (2-3).

The variational equations for initial time to are of the same form

$$\ddot{\mathbf{x}}_{t_o} = \left[\frac{\partial}{\partial \mathbf{X}} \left(-\frac{\mu \mathbf{X}}{\mathbf{r}^3} \right) + \frac{\partial \mathbf{F}}{\partial \mathbf{X}} \right] \mathbf{X}_{t_o} + \frac{\partial \mathbf{F}}{\partial \dot{\mathbf{X}}} \dot{\mathbf{X}}_{t_o}$$

However, they are associated with different initial conditions

$$X_{t_{o}}(t_{o}) = -\dot{X}_{o}(\alpha)$$
 , $\dot{X}_{t_{o}}(t_{o}) = -\ddot{X}_{o}(\alpha)$

These expressions may be derived by differentiating with respect to t_0 integral Eq. (2-4), which best shows the dependence upon t_0 .

The variational equations for the differential equation parameter β are

$$\ddot{\mathbf{x}}_{\beta} = \left[\frac{\partial}{\partial \mathbf{x}} \left(-\frac{\mu \mathbf{x}}{\mathbf{r}^{3}} \right) + \frac{\partial \mathbf{F}}{\partial \mathbf{x}} \right] \mathbf{x}_{\beta} + \frac{\partial \mathbf{F}}{\partial \dot{\mathbf{x}}} \dot{\mathbf{x}}_{\beta} + \frac{\partial \mathbf{F}}{\partial \beta}$$
 (2-7a)

and

$$X_{\beta}(t_{o}) = \dot{X}_{\beta}(t_{o}) = 0$$
 (2-7b)

As a source of partial derivatives, variational equations yield more accurate results than typical analytic derivatives, which usually assume two-body motion. Also, the partials can be generated more rapidly than difference quotient approximations because the terms $[\partial(-\mu X/r^3)/\partial X + \partial F/\partial X]$ and $\partial F/\partial X$ of Eq. (2-5) are identical in all the variational equations, and only the nonhomogeneous term $\partial F/\partial \beta$ of Eq. (2-7a) varies with a particular parameter.

A further advantage of the variational equations is that they permit use of the difference quotient technique as a checking device since lack of substantial agreement between the partial derivative estimates obtained by the two methods would indicate the presence of error. Although this test should not be considered fool proof, it is valuable and should not be overlooked.

2. 3 BASIC ORBIT DETERMINATION PROBLEM

The basic orbit determination problem, as discussed in Section 1, is to find values for a set of observational-model parameters such that the differences between the actual measured observations and corresponding values computed

from the model will be minimized in a generalized least-squares (GLS) sense. With respect to TRACE-D, GLS refers to a fitting process which allows weighting matrices to contain some off-diagonal elements as described in Section 2.5.2.

The TRACE-D program model includes the trajectory of the vehicle with associated initial-condition and differential-equation parameters, locations of observing stations, and certain systematic errors in the observation sensing equipment. The full list of parameters available in TRACE-D is given in Section 1. Relative significance may be assigned to observations of various types and quality by means of a weighting matrix. This weighting matrix is also used to a limited extent in processing correlated observations (See Section 2.5 2 for discussion of TRACE-D correlated data option).

The basic orbit determination problem thus may be restated: Given a set of n observations of orbiting objects, an appropriate weighting matrix, and a model from which corresponding observations may be computed, determine values of the model parameters to minimize the expression.

$$||O_{m} - O_{c}(P)||_{W}^{2} = [O_{m} - O_{c}(P)]^{T} W[O_{m} - O_{c}(P)]$$
 (2-8)

where

Om = vector of measured observations

O_c = vector of corresponding computed observations

P = vector of model parameters

W = observation weighting matrix

The particular significance of the minimization process depends on the nature of the weighting matrix. In TRACE-D this process usually is simple weighted least squares (WLS) if W is diagonal, or generalized least squares (GLS)

otherwise. However, under certain circumstances the process may be minimum variance. Detailed explanation of the weighting-matrix options and their significance is given in conjunction with the statistical aspects of the orbit determination problem (Section 2. 5).

An approximate solution P_0 of Eq. (2-8) is nearly always available, since trajectory initial conditions may be estimated from design information or preliminary orbit determination methods. Also, the "current best" values for force model parameters and station locations usually represent an excellent first approximation. Thus, expanding $O_c(P)$ in a Taylor series about P_0 to first order, the quantity to be minimized, Eq. (2-8), becomes

$$||O_{m} - O_{c}(P)||_{W}^{2} = ||O_{m} - O_{c}(P_{o}) - A \cdot \Delta P||_{W}^{2}$$
 (2-9)

where

$$A = \frac{\partial O_c}{\partial P} = matrix$$
 of partial derivatives evaluated at $P = P_o$

For the case where the parameters are quantities appearing in the equations of motion (including initial conditions), the partial derivatives are computed from the chain rule

$$\frac{\partial O_{c}}{\partial P} = \frac{\partial O_{c}}{\partial X} \frac{\partial X}{\partial P} + \frac{\partial O_{c}}{\partial \dot{X}} \frac{\partial \dot{X}}{\partial P}$$
 (2-10)

where

$$\frac{\partial X}{\partial P}$$
 , $\frac{\partial \dot{X}}{\partial P}$ = matrices of solutions of the variational equations

The matrices $\partial \Omega_c/\partial X$ and $\partial \Omega_c/\partial \dot{X}$ and those rows of $\partial \Omega_c/\partial P$ that correspond to parameters not appearing in the equations of motion (station locations and observation-error terms) are computed directly from geometrical relations.

The differences $O_{mc}(P_0) = O_m \cdot O_c(P_0)$ between the observations and the corresponding quantities computed from the assumed values P are called residuals. These result from the presence of random observational errors, inadequacies in the form of the model, incorrect values for the model parameters and computational errors due to roundoff and truncation effects. Since the original nonlinear GLS problem has been replaced by the approximate linear problem of finding a correction vector ΔP such that $|O_{mc}(P_0) - A \cdot \Delta P||_W^2$ is minimized, the expression $P = P_0 + \Delta P$ is in general only an approximate solution, and an iterative process is required. Then $||O_{mc}(P_0)||_W$ measures the degree to which an orbit computed from the current values Po of the parameters fits the observations and the expression $||O_{mc}^{p}||_{W} = ||O_{mc}(P_{o}) - A \cdot \Delta P||_{W}$ (superscript p means "predicted") then is an approximation, based upon the linearity assumption, to the value of $|O_{mc}||_{W}$ that would be obtained by replacing P_{o} with $P_{o} + \Delta P$. In a wellbehaved iteration the observed $|O_{mc}||_{W}$ should follow the predicted $||O_{mc}^{p}||_{W}$, the relative agreement between the two factors being a measure of convergence of the process.

The correction vector ΔP may be shown to be the solution of the linear system $(A^TWA)\Delta P = A^TWO_{mc}$ in various ways. Two proofs of this are the following:

Proof 1:

If

$$f(\Delta P) = ||A \cdot \Delta P - O_{mc}||_{W}^{2} = (A \cdot \Delta P - O_{mc})^{T} W(A \cdot \Delta P - O_{mc})$$

and if $f(\Delta P)$ is differentiated with respect to ΔP , one obtains

$$\frac{\partial \mathbf{f}}{\partial (\Delta P)} = 2 \left(\mathbf{A}^T \mathbf{W} \mathbf{A} \cdot \Delta P - \mathbf{A}^T \mathbf{W} \mathbf{O}_{mc} \right)^T$$

The latter expression must be zero if ΔP minimizes $f(\Delta P)$.

Proof 2:

If

$$A^TWA \cdot \Delta P = A^TWO_{mc}$$

then, for any $\Delta P' \neq \Delta P$, one obtains

$$\begin{split} f(\Delta P') &= \left| \left| A \cdot \Delta P - O_{mc} + A(\Delta P' - \Delta P) \right| \right|_{W}^{2} \\ &= \left| \left| A \cdot \Delta P - O_{mc} \right| \right|_{W}^{2} + 2 [A \cdot \Delta P - O_{mc}]^{T} W [A(\Delta P' - \Delta P)] \\ &+ \left| \left| A(\Delta P' - \Delta P) \right| \right|_{W}^{2} \\ &= f(\Delta P) + 2 \left(A^{T} W A \cdot \Delta P - A^{T} W O_{mc} \right)^{T} (\Delta P' - \Delta P) \\ &+ \left| \left| A(\Delta P' - \Delta P) \right| \right|_{W}^{2} \\ &= f(\Delta P) + \left| \left| A(\Delta P' - \Delta P) \right| \right|_{W}^{2} \end{split}$$

or

$$f(\Delta P') > f(\Delta P)$$

From Proof 2 it is evident that ΔP minimizes $F(\Delta P)$.

2.4 CONSTRAINED AND BOUNDED LEAST-SQUARES SOLUTIONS

Two distinct types of restrictions upon the solution of the generalized least-squares (GLS) problem may be necessary or desirable, in that constraints among the parameters may be a part of the physical problem, and bounds upon the magnitude of the corrections may facilitate computation.

2.4.1 Constraints

An example of a physical constraint which could be imposed upon parameters would be precise knowledge of the <u>relative</u> locations of two nearby observing stations. If the actual locations of such a pair of stations were among the parameters P in a differential correction, it would be important to constrain the ΔP corrections in such a manner that the relative locations of the stations

were preserved. In TRACE-D this is accomplished by introducing linear constraints in the form

$$\Delta P = B \cdot \Delta P' + C \qquad (2-11)$$

where

B = rectangular matrix

ΔP' = reduced set of independent parameters

and by solving the GLS problem in terms of $\Delta P'$ and using Eq. (2-11) to obtain the constrained correction ΔP . Solving the GLS problem in terms of $\Delta P'$ requires minimizing $||A \cdot \Delta P - O_{\text{rnc}}||_W^2$ subject to the constraint Eq. (2-11), which is equivalent to minimizing $||A \cdot (B \cdot \Delta P' + C) - O_{\text{mc}}||_W^2 = ||(AB) \cdot \Delta P' - (O_{\text{mc}} + AC)||_W^2$. This required minimum is obtained as the solution of the linear system

$$(AB)^{T}W(AB)\Delta P' = (AB)^{T}W(O_{mc} + AC)$$
 (2-12)

2.4.2 Bounds

Under conditions fairly common in the solving of the GLS problem, which for example might involve inadequacies in the observational model or a poor initial approximation P_o , the observed $| \cdot e_{mc} | \cdot e_$

The simple geometrical interpretation for a two-parameter example is illustrated in Figure 2-1, wherein the problem is to find a minimum of the surface $f(\Delta P) = ||A \cdot \Delta P - O_{mc}||_W^2$ over all ΔP within the ellipse defined by g_i and g_2 . An elliptic rather than a circular region is used to account for the range of magnitudes of the various parameters.

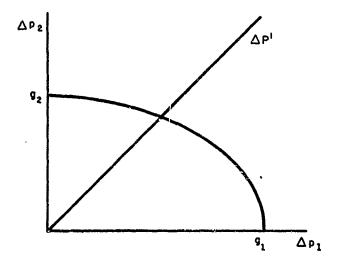


Figure 2-1. Two-Parameter Constraint Ellipse

If the unconstrained solution does not occur within the ellipse $||G \cdot \Delta P||^2 = 1$, a new function $F(\Delta P) = f(\Delta P) + z ||G \cdot \Delta P||^2$ is minimized, whose minimum point $\Delta P'(z)$ is found as the solution of

$$(A^{T}WA + zG^{T}G)\Delta P' = A^{T}WO_{mc}$$
 (2-13)

As z increases, minimization of F requires smaller and smaller values of $\Delta P'(z)$. More precisely, it will be shown that $||G \cdot \Delta P'(z)||$ is a decreasing function of z and that, in particular, by a search and interpolation procedure a value z' of z can be found such that $||G \cdot \Delta P'(z')||^2 = 1$. Since minimizing $F = f + z' ||G \cdot \Delta P'(z')|| = f + z'$ actually is equivalent to minimizing f, because these terms differ only by the constant z', the point $\Delta P'(z')$ which minimizes

 $f(\Delta P)$ along the bounding ellipse is identified. It also will be shown that $f[\Delta P'(z)]$ is an increasing function of z. Thus, any interior point of the ellipse corresponds to larger values of z and of f, and therefore the constrained minimum point is on the boundary and is the solution $\Delta P'(z')$ of $(A^TWA + z'G^TG)\Delta P = A^TWO_{mc}$ for which $||G \cdot \Delta P'(z')||^2 = 1$. Throughout the following proofs of the above, primes have been dropped for convenience.

The monotonic decreasing character of $||G \cdot \Delta P||$ as a function of z may be demonstrated by differentiating

$$(A^{T}WA + zG^{T}G)\Delta P(z) = A^{T}WO_{mc}$$
 (2-14)

with respect to z to obtain

$$(A^{T}WA + zG^{T}G)\frac{d}{dz}(\Delta P) + (G^{T}G)\Delta P = 0$$
 (2-15)

or

$$\frac{\mathrm{d}}{\mathrm{d}z}(\Delta P) = -(A^{\mathrm{T}}WA + zG^{\mathrm{T}}G)^{-1}(G^{\mathrm{T}}G)\Delta P \qquad (2-16)$$

Differentiating $d | |G \cdot \Delta P| |^2 / dz$ and substituting Eq. (2-16) then leads to

$$\frac{\mathrm{d}}{\mathrm{d}z} ||G \cdot \Delta P||^2 = 2(\Delta P^{\mathrm{T}})(G^{\mathrm{T}}G) \left(\frac{\mathrm{d}}{\mathrm{d}z} \Delta P\right)$$

$$= -2\Delta P^{\mathrm{T}}(G^{\mathrm{T}}G)(A^{\mathrm{T}}WA + zG^{\mathrm{T}}G)^{-1}(G^{\mathrm{T}}G)\Delta P \qquad (2-17)$$

Since $(A^TA + zG^TG)^{-1}$ is positive definite for positive z, the following is true

$$\frac{\mathrm{d}}{\mathrm{d}z} ||\mathbf{G} \cdot \Delta \mathbf{P}||^2 < 0 \tag{2-18}$$

whenever $(G^TG) \cdot \Delta P \neq 0$.

The monotonic increasing character of $f[\Delta P(z)]$ may similarly be established by showing that df/dz > 0. Differentiating $f[\Delta P(z)]$ then leads to

$$\frac{\mathrm{df}}{\mathrm{dz}} = \frac{\partial f}{\partial (\Delta P)} \frac{\mathrm{d}(\Delta P)}{\mathrm{dz}}$$

$$= \left[2 \left(A^{\mathrm{T}} W A \Delta P - A^{\mathrm{T}} W O_{\mathrm{mc}} \right) \right]^{\mathrm{T}} \left[-(A^{\mathrm{T}} W A + z G^{\mathrm{T}} G)^{-1} (G^{\mathrm{T}} G) \Delta P \right]$$

$$= -2 \left[(A^{\mathrm{T}} W A + z G^{\mathrm{T}} G) \Delta P - A^{\mathrm{T}} W O_{\mathrm{mc}} - z (G^{\mathrm{T}} G) \Delta P \right]^{\mathrm{T}} \left[(A^{\mathrm{T}} W A + z G^{\mathrm{T}} G)^{-1} (G^{\mathrm{T}} G) \Delta P \right]$$
(2-19)

However, since by Eq. (2-14) $(A^TWA + zG^TG)\Delta P(z) = A^TWO_{mc}$, differentiating leads to

$$\frac{\mathrm{df}}{\mathrm{dz}} = +2z\Delta P^{\mathrm{T}}(G^{\mathrm{T}}G)(A^{\mathrm{T}}WA + zG^{\mathrm{T}}G)^{-1}(G^{\mathrm{T}}G)\Delta P \qquad (2-20)$$

which is positive whenever $(G^{T}G)\Delta P \neq 0$.

2.4.3 Solution of the Linear System

Solution of the linear system $(A^TWA + zG^TG)\Delta P = A^TWO_{mC}$ and inversion of the coefficient matrix $C = A^TWA + zG^TG$ is accomplished by a special method related to a procedure known classically as the square root method (Ref. 3). This method is finite, or noniterative, is applicable only to symmetric matrices, and is based on the fact that a symmetric matrix can be decomposed as a product of the form $C = LDL^T$, where L is a lower triangular matrix with (-1) as diagonal elements and D is a diagonal matrix. In such a representation, det (L) = ± 1 and det (D) = det (C). Therefore, L^{-1} exists and in fact is also a lower triangular matrix with (-1) on the diagonal, and D has no zero elements if C is nonsingular. Two equivalent forms consequently are

(i)
$$L^{-1}C(L^{T})^{-1} = L^{-1}C(L^{-1})^{T} = D$$

(2)
$$C^{-1} = (L^{-1})^T D^{-1} L^{-1}$$

OI

(1')
$$SCS^T = D$$

(2')
$$C^{-1} = S^{T}D^{-1}S$$

where $S = L^{-1}$.

It thus is apparent that the inversion of C and the solution $\Delta P' = (C^{-1})A^TWO_{mc}$ require matrices S and D such that $SCS^T = D$.

A bordering technique used to find S and D assumes at the k^{th} stage that the k^{th} -order principal minors of S and D have been found. The $(k+1)^{st}$ -order minors require the vector V and the scalar b such that

$$\begin{pmatrix} S_{k} & 0 \\ V^{T} & -1 \end{pmatrix} \begin{pmatrix} C_{k} & d \\ d^{T} & \alpha \end{pmatrix} \begin{pmatrix} S_{k}^{T} & V \\ 0 & -1 \end{pmatrix} = \begin{pmatrix} D_{k} & 0 \\ 0 & b \end{pmatrix}$$
 (2-21)

where

$$\begin{pmatrix} C_k & d \\ d^T & a \end{pmatrix} = (k+1)^{st} - order minor of C$$

It may easily be verified that the required V and b are

$$V = S_k^T D_k^{-1} S_k^{d}$$

and

(2-22)

$$b = a - V^{T}d$$

2. 5 THE STATISTICS OF ORBIT DETERMINATION

In the process of orbit determination by the method of weighted least squares (WLS), no assumptions regarding the statistics of the observational errors are necessary. Although no statistical conclusions can be drawn from obtained results, the justification for the method is that solutions gained by minimizing residuals in the least squares sense have proved to be very useful. It should be noted that all previous TRACE- program versions employed WLS exclusively.

On the other hand, if the two frequently adopted assumptions that (1) the observational errors ϵ_i are random with mean zero and known covariance matrix Σ and (2) that the weighting matrix $\mathbb{W} = \Sigma^{-1}$, then the inverse normal matrix is the linear approximation of the variance-covariance matrix (often abbreviated "covariance matrix") of the parameters being determined. Inasmuch as this matrix depends only on the partial derivatives of observations with respect to the parameters and on the weighting matrix, it may be generated and used for statistical analysis of tracking networks and spacecraft systems in the absence of actual or simulated observations. Details pertinent to the variance-covariance matrix, as well as the relation of WLS orbit determinations to minimum-variance and maximum-likelihood criteria and the particular parameter estimation methods available in the TRACE-D program are outlined in the following sections.

2.5.1 The Variance-Covariance Matrix

If it is assumed that the vector of measured observations O_m is the true value $O_c(P_t)$ (subscript t denotes "true") plus a random ϵ cror ϵ , the linear approximation to $O_c(P_t)$ is

$$O_c(P_t) = O_c(P_0) + A \cdot \Delta P \qquad (2-23)$$

and the residual vector is

$$O_{mc} = O_m - O_c(P_o) = A \cdot \Delta P_t + \epsilon$$
 (2-24)

where

 $O_c(P_o)$ = vector of computed quantities P_o = estimate of the true parameter vector P_t ΔP_t = P_t - P_o A = matrix of partial derivatives $\partial O_c/\partial P_o$ ϵ = vector of unbiased observational errors

As noted previously, the GLS problem is minimizing $f(\Delta \Gamma) = ||O_{mc} - A \cdot \Delta P||_{W}^2$, for which the solution is $\Delta P' = (A^T W A)^{-1} A^T W O_{mc}$.

It can readily be shown for the linear problem that the vector $\Delta P'$ is an unbiased estimate of the true value ΔP_t and that the expected value of $\Delta P'$ is the true value ΔP_t , even though $\Delta P'$ is a random quantity since it depends upon the residuals and therefore upon the observational errors. Thus, with

$$\Delta P' = (A^{T}WA)^{-1}A^{T}WO_{mc}$$

$$= (A^{T}WA)^{-1}A^{T}W(A \cdot \Delta P_{t} + \epsilon)$$

$$= (\Delta P_{t} + (A^{T}WA)^{-1}A^{T}W\epsilon)$$

then

$$E(\Delta P') = \Delta P_t + E[(A^T W A)^{-1} A^T W \epsilon] = \Delta P_t$$
 (2-25)

The latter expression reflects appeal to the linearity of $E(\cdot)$ and the assumption that $E(\epsilon)=0$. It should be noted that the vector $\delta P'=\Delta P'-\Delta P_t$ would be the deviation, due to random errors, of the solution $\Delta P'$ from the true value ΔP_t . This vector has previously been shown to have the expected value zero.

The expected values of the square of the deviations (the product of two components of the deviations) are summarized in the quantity $E(\delta P' \delta P'^T)$, which by definition is the covariance matrix C(P') of the (estimated) parameters. If the symmetry of the matrices W and A^TWA is used, the expression may be written

$$E(\delta P' \delta P'^{T}) = E[(A^{T}WA)^{-1}A^{T}W(\epsilon \epsilon^{T})WA(A^{T}WA)^{-1}]$$
 (2-26)

However, since $E(\epsilon \epsilon^T) = \Sigma$, the covariance matrix of the observational errors, Eq. (2-26) becomes

$$C(P') = (A^{T}WA)^{-1}A^{T}W \Sigma WA(A^{T}WA)^{-1}$$
 (2-27)

Equation (2-27) is the general form of the covariance matrix for a GLS estimate of the parameters. However, use of the second assumption, $W = \Sigma^{-1}$, results in the important simplification

$$C(P') = (A^T W A)^{-1} = (A^T \Sigma^{-1} A)^{-1}$$
 (2-28)

This latter expression represents the basic covariance matrix calculated in TRACE-D.

2. 5. 2 Minimum-Variance and Maximum-Likelihood Estimates

In most instances of orbit determination from observations, least-squares methods (WLS or GLS) not only require no statistical justification, but in fact none exists. These methods are intended simply to produce fits and predictions of acceptable quality. Conversely, statistical conclusions are sought in other applications such as systems analysis and design. These are commonly based on minimum-variance (MV, or "Markov") or on maximum-likelihood (ML) estimations. This section describes in general terms the assumptions governing MV and ML techniques and their relation to TRACE-D program procedure.

The MV estimate of ΔP is the linear unbiased estimate which minimizes the diagonal terms (variances) of the variance-covariance matrix of parameters P (Ref. 4). The applicable formulas are

$$\Delta P_{MV} = (A^T \Sigma^{-1} A)^{-1} A^T \Sigma^{-1} O_{mc}$$
 (2-29)

and

$$C(P_{MV}) = (A^T \Sigma^{-1} A)^{-1}$$
 (2-30)

When Σ^{-1} is used as the weighting matrix W, the GLS estimate and the covariance matrix in TRACE-D also are MV.

The WLS procedure, which has been used in prior TRACE- program versions, also is available in TRACE-D and in fact remains the most frequently utilized weighting option. However, one alternative weighting option that has been added to TRACE-D, and whose inclusion in the program represents a step in the direction of a generalized MV capability, is the possibility of supplying non-diagonal weighting submatrices up to 3 × 3 in dimension. In this connection, all observations associated with each weighting matrix must be of the same set number (see Section 5.1.3.4), and their observation times must be the same. Although this feature is rather restrictive in that it precludes treatment of cases involving known time correlations in the observations, it permits one important class of observations to be handled correctly, which previously was not possible.

For example, if sets of raw observations of some arbitrary type are subjected to a data-reduction process which finally produces a series of three-component (x, y, z) vectors representing estimates of the position of a satellite at various times, the data-reduction process typically also will yield a 3×3 covariance matrix for the estimated errors in (x, y, z) that is derived from estimates of errors in the original raw observations. In the fitting of the

(x, y, z) points with the TRACE program, the desirability of weighting these points with the inverse of the covariance matrix for each (x, y, z) set has been realized for the first time in TRACE-D.

Since the criterion for MV is that $W = \Sigma^{-1}$, which is assumed to be the case for data such as those noted above, the solution obtained by fitting the data with TRACE-D may said to be an MV estimate,

Nothing has so far been assumed about the actual form of the distribution of the random errors. If a specific probability density function is assumed, then it is possible to seek the estimate that maximizes the probability or likelihood that the actual observations would occur, given the estimated values of the parameters. In the case of a joint normal (or gaussian) distribution of observational errors with covariance matrix Σ , the ML estimate reduces to MV. In practice the gaussian assumption is always made (Ref. 5).

The foregoing may be summarized: If the weighting matrix applied in the least-squares process is the inverse of the estimated covariance matrix for the observational errors, the GLS estimate obtained by TRACE-D is also MV; if the errors are further assumed to be normally distributed, the estimate is also ML.

SECTION 3

EQUATIONS

3.1 COORDINATE SYSTEMS

Several coordinate systems are employer in TRACE-D. Basic to all is the earth-centered inertial system, which has as its reference plane and direction the true equator at epoch and the mean equinox at 0 hour GMT of the date of epoch. This description follows from the manner in which input quantities are treated, in which connection the longitude reference is a_g (Ref. 6), or the right ascension of the Greenwich meridian from the mean equinox of date at 0^{th} GMT (a_g is also known as Greenwich mean sidereal time), and the reference plane for initial position and velocity parameters is the equator.

Three types of coordinates within the foregoing system that are useful for TRACE-D program purposes are described in Section 3.1.1. A station-dependent coordinate system that has been introduced to facilitate radar computations and an orbit-plane coordinate system that is used for analysis of residuals are described in Sections 3.1.2 and 3.1.3. The station-centered inertial and the vehicle-centered coordinate systems discussed in Section 3.1.4 and 3.1.5 are introduced for convenience in the computation of partial derivatives and vehicle-centered quantities, respectively.

²TRACE-A and TRACE-D are identical in this regard. The corresponding statement in Section 3 of Ref. 1 is incorrect.

3.1.1 Earth-Centered Inertial System

The basic earth-centered coordinate system is shown in Figure 3-1,

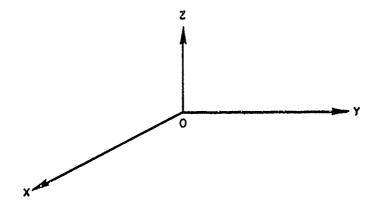


Figure 3-1. Earth-Centered Coordinate System

where

0 = center of mass of the earth

X = vector from 0 in the equatorial plane directed to the vernal equinox at t_g, (0 hour GMT of epoch date)

Y = vector from 0 perpendicular to X in such direction that (X, Y, Z) is a right-handed system

Z = vector from 0 perpendicular to the equatorial plane and directed north

The position and velocity of a body at a point P within this reference frame may be expressed in rectangular or spherical coordinates or in terms of the classical elements of its orbit.

3, 1.1.1 Rectangular Coordinates

Within rectangular coordinates, representation of a point P may be expressed by

$$P = P(x, y, z, \dot{x}, \dot{y}, \dot{z})$$

where x, y, z are, respectively, the components of position of the point in the X, Y, Z directions as defined in Figure 3-1 and \hat{x} , \hat{y} , \hat{z} are the components of its velocity in those directions.

3.1.1.2 Spherical Coordinates

In the spherical coordinate system shown in Figure 3-2, position and velocity

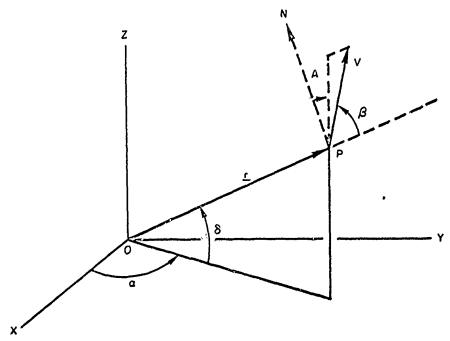


Figure 3-2. Spherical Coordinate System

at a point may be written

$$P = P(\alpha, \delta, \beta, A, r, v)$$

where

V = a vector equal in magnitude and direction to the velocity of the vehicle at P

a = right ascension measured from X-axis, positive eastward

 δ = geocentric latitude (- $\pi/2 \le \delta \le \pi/2$)

 β =angle between V and the geocentric vertical at P (0 \leq β \leq $\pi)$

A - azimuth of V from true north, measured eastward on a plane normal to geocentric vertical

r = magnitude of OP

v = magnitude of V

3.1.1.3 Orbital Elements

In Figure 3-3. P is a point on the osculating conic described by the parameters a, e, i, Ω , and ω . The position of F on this conic is determined by τ and by a value for the current time. Within this reference framework,

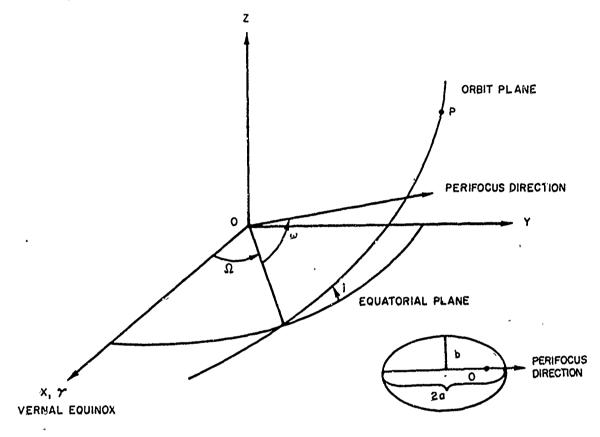


Figure 3-3. Orbital Elements

the expression for position is given by

$$P = P(a, e, i, \Omega, \omega, \tau)$$

where

a, b = semi-major and semi-minor axes

$$e = eccentricity = \sqrt{a^2 - b^2}/a$$

i = inclination of orbit plane

 Ω = right ascension of ascending node

 ω = angle between direction of perigee and the line of nodes

 τ = time in minutes from t_g of last previous perigee passage (t_g = 0 hours GMT of day of epoch)

3.1.2 Station-Dependent Coordinate System

A station-dependent coordinate system intended to facilitate radar computations is shown in Figure 3-4,

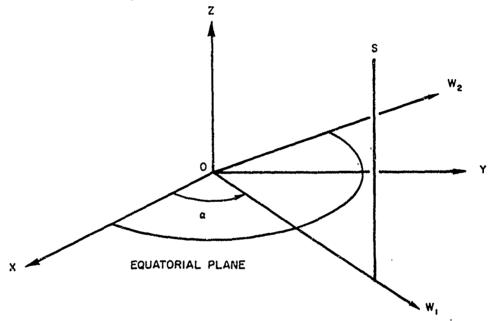


Figure 3-4. Station-Dependent Coordinate System (W₁, W₂, Z)

where

S = station location at some time t

 $a = l + a_g + \omega_e(t - t_g)$

l = geographic longitude of station

ag = right ascension of Greenwich at time tg

 ω_e = rate of rotation of the earth

 W_1 , W_2 = axes X and Y rotated through angle α .

3.1.3 Orbit-Plane Coordinate System

In Figure 3-5 the basic coordinate system is the earth-centered inertial reference frame described in Section 3.1. However, in this instance the

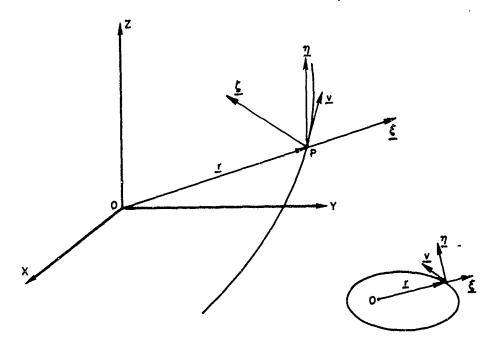


Figure 3-5. Orbit-Plane Coordinate System

point P, which usually is the position of a reference vehicle, represents the origin of the orbit-plane coordinate system defined by the vectors $\underline{\xi}$, $\underline{\eta}$, $\underline{\zeta}$, which are in the radial, in-track, and cross-track directions, respectively. In the smaller sketch it should be noted that the $\underline{\xi}$ axis is an extension of the geocentric radius vector. The $\underline{\eta}$ axis is both normal to the $\underline{\xi}$ axis and positive in the same general direction as the inertial velocity vector \underline{v} . All lie in the instantaneous orbit plane. The $\underline{\zeta}$ axis is directed out of the page, or normal to the orbit plane, thus forming a right-handed orthogonal system.

The position and velocity of an alternate point P₁ relative to the point P are then given by

$$P_1 = P_1(\xi, \eta, \zeta, \xi, \eta, \zeta)$$

3.1.4 Station-Centered Inertial Coordinate System

The station-centered inertial coordinate system used for partials computation is shown in Figure 3-6,

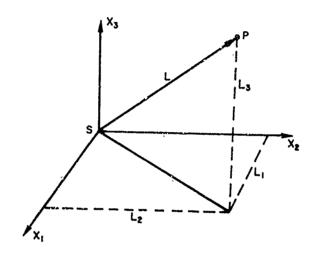


Figure 3-6. Station-Centered Inertial Coordinate System

where

S = station location at some time
$$t = (x_s, y_s, z_s)$$

$$a = \ell + a_g + \omega_e(t - t_g)$$

$$x_s = w_1^s \cos a$$

$$y_s = w_1^s \sin a$$

$$z_s = w_3^s$$

$$= station position at time t in ECI system (see Section 3.4.1 for definition of w_1^s and w_3^s)
$$L_1 = x - x_s$$

$$L_2 = y - y_s$$

$$L_3 = z - z_s$$$$

and where vectors X_1 , X_2 , and X_3 . "e parallel to axes X, Y, Z, respectively.

3.1.5 Vehicle Coordinate System

A coordinate system convenient for computing vehicle-fixed effects is shown in Figure 3-7,

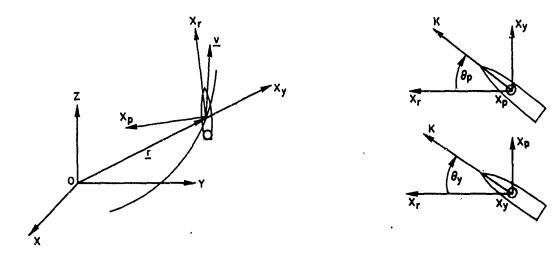


Figure 3-7. Vehicle Coordinate System

where

X = vehicle position vector in basic ECL system

X = vehicle velocity vector in basic ECI system

$$X_y = X/|X| = yaw axis$$

$$X_p = \frac{X \times \dot{X}}{|X \times \dot{X}|} = pitch axis$$

$$X_r = X_p \times X_y = roll axis$$
unit vectors

K = magnitude of instantaneous velocity adjustment (kick) vector

 θ_{D} = direction of deflection for positive pitch-angle adjustment

 θ_{v} = direction of deflection for positive yaw-angle adjustment

X and \dot{x} are identical to the usual symbols \underline{r} and \underline{v} , and the vectors X_y , X_p , X_r are in the radial, in-track, and cross-track directions, respectively.

3.2 INITIAL CONDITIONS AND COORDINATE TRANSFORMATIONS

The parameters of an orbit may be given within any of the coordinate categories described in Section 3.1.1. The primary trajectory computations are accomplished in earth-centered rectangular coordinates. Supplemental outputs include spherical coordinates and orbital elements. Formulas for necessary transformations are given in Sections 3.2.1 through 3.2.4, wherein the date chosen to determine the X-axis is t_g (0 hour GMT of epoch date). The time t_o at which the parameters are specified is referenced to t_g , i.e., the program operates with time in units of minutes from t_g .

3.2.1 Spherical to Rectangular Coordinates

 $x = r \cos \delta \cos \alpha$

 $y = r \cos \delta \sin \alpha$

 $z = r \sin \delta$

 $\dot{x} = v[\cos \alpha(-\cos A \sin \beta \sin \delta + \cos \beta \cos \delta) - \sin A \sin \beta \sin \alpha]$

 $\dot{y} = v[\sin \alpha(-\cos A \sin \beta \sin \delta + \cos \beta \cos \delta) + \sin A \sin \beta \cos \alpha]$

 $\dot{z} = v[\cos A \cos \delta \sin \beta + \cos \beta \sin \delta]$

If longitude (1) is input instead of a in the foregoing expressions, a is computed as in Section 3.1.2. In this case, $t - t_g = t_o$.

3. 2. 2 Rectangular to Spherical Coordinates

$$\alpha = \tan^{-1}(y/x)$$

$$\delta = \tan^{-1}\left(z/\sqrt{x^2 + y^2}\right)$$

$$\beta = \cos^{-1}\left[(x\dot{x} + y\dot{y} + z\dot{z})/rv\right]$$

$$A = \tan^{-1} \left[\frac{r(x\dot{y} - y\dot{x})}{y(y\dot{z} - z\dot{y}) - x(z\dot{x} - x\dot{z})} \right]$$

$$r = \sqrt{x^2 + y^2 + z^2}$$

$$v = \sqrt{\dot{x}^2 + \dot{y}^2 + \dot{z}^2}$$

3.2.3 Orbital Elements to Rectangular Coordinates

$$x = x_{\omega} P_{x} + y_{\omega} Q_{x}$$

$$y = x_{\omega} P_{y} + y_{\omega} Q_{y}$$

$$z = x_{\omega} P_{z} + y_{\omega} Q_{z}$$

$$\dot{x} = \dot{x}_{\omega} P_{x} + \dot{y}_{\omega} Q_{x}, \text{ etc}$$

where, if the conic is an ellipse,

 $P_x = \cos \Omega \cos \omega - \sin \Omega \sin \omega \cos i$

 $P_{V} = \sin \Omega \cos \omega + \cos \Omega \sin \omega \cos i$

 $P_z = \sin \omega \sin i$

 $Q_{x} = -\cos \Omega \sin \omega + \sin \Omega \cos \omega \cos i$

 $Q_y = -\sin \Omega \sin \omega + \cos \Omega \cos \omega \cos i$

 $Q_z = \cos \omega \sin i$

 $p = a(1 - e^2) = semi-latus rectur$

 μ = gravitational constant

$$n = \sqrt{|\mu/a^3|} = mean motion$$

 $M = n(t - \tau) = mean anomaly$

E = solution of (M = E - e sin E) = eccentric anomaly

$$r_{\omega} = a(1 - e \cos E)$$

$$x_{\omega} = a(\cos E - e)$$

$$y_{\omega} = \sqrt{|ap|} \sin E$$

$$\dot{x}_{\underline{\omega}} = -\frac{\sqrt{|\mu a|}}{r_{\underline{\omega}}} \sin E$$

$$\dot{y}_{\omega} = \frac{\sqrt{\mu p}}{r_{\omega}} \cos E$$

If the orbital conic is a hyperbola (e > 1), E is the solution of M = $e \sinh E - E$. Also, $\sin E$ and $\cos E$ above must be replaced by $\sinh E$ and $\cosh E$.

3.2.4 Rectangular Coordinates to Orbital Elements

$$a = \left(\frac{2}{r} - \frac{v^2}{\mu}\right)^{-1}$$

$$e = \sqrt{(e \cos E)^2 + (e \sin E)^2} \qquad \text{(for elliptic orbits)}$$

$$e = \sqrt{(e \cosh E)^2 - (e \sinh E)^2} \qquad \text{(for hyperbolic orbits)}$$

$$i = \tan^{-1} \left(\frac{\sqrt{P_z^2 + Q_z^2}}{P_x Q_y - P_y Q_x}\right)$$

$$\Omega = \tan^{-1} \left(\frac{P_y Q_z - P_z Q_y}{P_x Q_z - P_z Q_x}\right)$$

$$\omega = \tan^{-1} \left(\frac{P_z}{Q_z}\right)$$

$$\tau = t - \frac{M}{n}$$

where

$$r = \sqrt{x^{2} + y^{2} + z^{2}}$$

$$v^{2} = \dot{x}^{2} + \dot{y}^{2} + \dot{z}^{2}$$

$$e \cos E = 1 - \frac{r}{a}$$

$$e \sin E = \frac{x\dot{x} + y\dot{y} + z\dot{z}}{\sqrt{|a|\mu}}$$
(for elliptic orbits)

e cosh
$$E = 1 - \frac{r}{a}$$

e sinh
$$E = \frac{x\dot{x} + y\dot{y} + z\dot{z}}{\sqrt{|a|\mu}}$$

$$p = \frac{r^2v^2 - (x\dot{x} + y\dot{y} + z\dot{z})^2}{\mu}$$

$$D = \frac{x\dot{x} + y\dot{y} + z\dot{z}}{e\mu}$$

$$\dot{D} = \frac{e \cos E}{er}$$

$$H = \frac{1}{e\sqrt{\mu p}}(r - p)$$

$$\dot{H} = \frac{1}{e\sqrt{\mu p}} \frac{\dot{x}\dot{x} + y\dot{y} + z\dot{z}}{r}$$

$$P_{x} = \dot{D}x - D\dot{x}$$

$$P_y = \dot{D}y - D\dot{y}$$

$$P_z = \dot{D}z - D\dot{z}$$

$$Q_{x} = \dot{H}x - H\dot{x}$$
, etc

$$n = \sqrt{\frac{\mu}{a^3}}$$

 $M = E - e \sin E$ (for elliptic orbits)

M = e sinh E - E (for hyperbolic orbits)

$$E = \tan^{-1} \frac{e \sin E}{e \cos E}$$

(for hyperbolic orbits)

3.3 OBSERVATION DATA

Although in previous TRACE program models all observations were transformed to R, A, E, and \dot{R} , all observations used in the TRACE-D orbit-determination process are retained in the same coordinate system in which they are input. In general, input is in units of feet, seconds, and degrees, and computations are carried out in earth radii, minutes, and radians. The details of units conversion have been omitted from this section.

It should be noted that the coordinate systems shown in Section 3.3 also are pertinent to the discussion of partials presented in Section 3.4.

3. 3. 1 Station Coordinates

Station coordinate system relationships are shown in Figure 3-8,

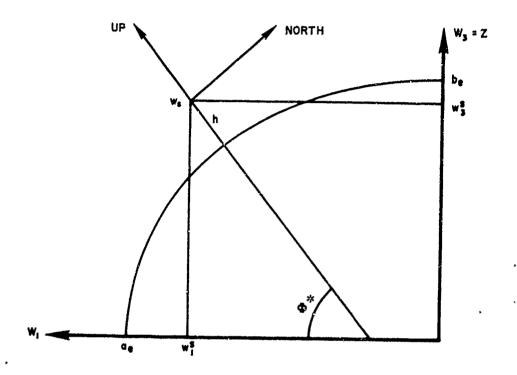


Figure 3-8. Station Coordinates

where

 $\Phi^* = geodetic latitude$

a_e = semi-major axis of the earth (equatorial radius)

b_e = semi-minor axis of the earth (polar radius)

h = station altitude with respect to reference ellipsoid

 $W^{S} = station position in W-coordinate system = (<math>w_{1}^{S}$, 0, w_{3}^{S})

3.3.2 Azimuth and Elevation Angles

Azimuth and elevation angle coordinate system relationships are shown in Figure 3-9,

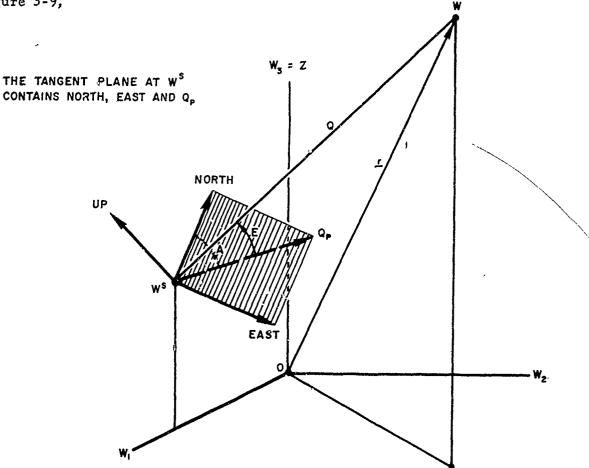


Figure 3-9. Azimuth and Elevation in Station Coordinate System

where

W = vehicle position

W^S = station position

 $Q_p = projection of Q = W - W^s onto tangent plane at W^s$

R = |Q| = slant range

<u>r</u> = geocentric radius vector

3.3.3 Topocentric Angular Measurement

Coordinate system relationships of topocentric angular measurements are shown in Figure 3-10,

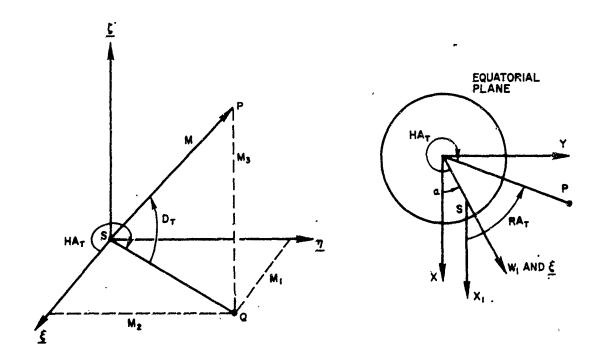


Figure 3-10. Right Ascension, Declination, and Hou-Angle in Station-Centered Coordinate System

where

 $\underline{\xi}$, $\underline{\eta}$, $\underline{\zeta}$, are parallel to W_1 , W_2 , W_3 , respectively

 $SQ = projection of M onto \xi, \eta plane$

 HA_{γ} = topocentric hour angle (measured westward in the ξ , η plane)

 $RA_T = \text{topocentric right ascension} = \alpha - HA_T$

 D_{T} = topocentric declination

R = |M|

a = right ascension of station

3.3.4 Interferometer Data

In Figure 3-11, S, $\mathbf{S_{P}},$ and $\mathbf{S_{Q}}$ are a network of stations reporting range and

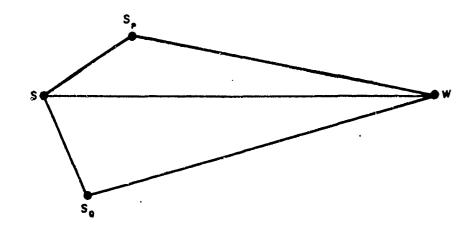


Figure 3-11. Station Network for Interferometer Data range-rate differences. Letting R = |W - S|, $R_P = |W - S_P|$, and $R_Q = |W - S_Q|$, then

$$P = R - R_{P}$$

$$Q = R - R_{Q}$$

$$\dot{P} = \dot{R} - \dot{R}_{P}$$

$$\dot{Q} = \dot{R} - \dot{R}_{Q}$$

3.3.5 Horizon-Sensor Angles

Horizon-sensor angles related to an earth-centered inertial coordinate system are shown in Figure 3-12,

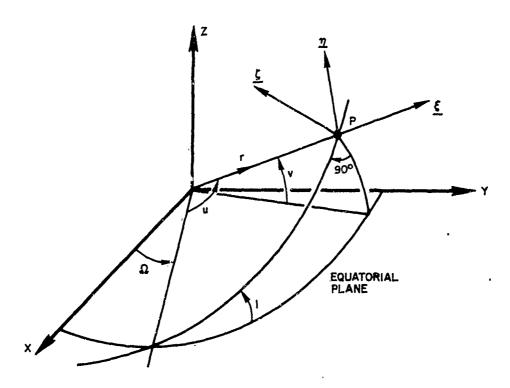


Figure 3-12. Horizon-Sensor Angles u, v in Earth-Centered Inertial Coordinate System

where, assuming $\underline{\zeta}$, $\underline{\eta}$, and $\underline{\xi}$ are unit vectors,

$$N_2 = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \times \underline{\zeta}$$

 $N_1 = N_2 / |N_2|$

$$u = \sin^{-1} |M_1 \times \underline{\xi}|$$

$$u = \cos^{-1}(N_1 \cdot \underline{\xi})$$

$$v = tan^{-1} (sin u tan i)$$

3.3.6 Other Observation Measurements

3.3.6.1 Geocentric Right Ascension and Declination

Observed values of these angles, which can be input to the orbit-determination process, are identical to α and δ as previously defined in Section 3.1.1.2.

3.3.6.2 Height Measurements

Height observations are assumed to be measured along the geocentric radius vector above the oblate earth (see Section 3.5.9 for specific equation).

3.3.6.3 Rectangular Geocentric Data

 $\stackrel{\wedge}{x}$, $\stackrel{\wedge}{y}$, $\stackrel{\wedge}{z}$ data points are measured in a coordinate system with origin at the center of the earth, the $\stackrel{\wedge}{z}$ axis along the spin axis, and the $\stackrel{\wedge}{x}$ axis along the Greenwich meridian.

3.3.6.4 Range Rate and Doppler

Equations for R and Δf data are given in following Sections 3.4.5 and 3.4.7.

3.4 PARTIAL DERIVATIVES OF OBSERVATION DATA

In tracking and data studies it is necessary to compute partial derivatives of observation data with respect to the parameters of initial conditions, differential equations, station locations, observation biases, and observation scale factors. For the purposes of this section, it will be assumed that the integrated position of the vehicle in earth-centered inertial rectangular coordinates and the partial derivatives of these coordinates with respect to the first two types of parameters are known.

The following notation is applicable to the derivations presented in this section:

 p_i (i = 1, 2, ..., n) = the ordered list of initial conditions and differential equation parameters for which partials are to be computed $\frac{\partial x}{\partial p_i}$, $\frac{\partial y}{\partial p_i}$, ..., $\frac{\partial \dot{z}}{\partial p_i}$ = partial derivatives of x, y, ..., \dot{z} with respect to the p_i

e = longitude of station

φ* = geodetic latitude of station

h = height of station

 $a = a_g + \omega_e(t - t_g) + l \text{ (Ref. Sec. 3.1.1.2)}$

 w_j , \dot{w}_j (j = 1, 2, 3) = position and velocity of vehicle in the station-dependent W system

w₁, w₃ = position of station in station-dependent W system

e = ellipticity of reference ellipsoid

a_e = semi-major axis of the earth

 $b_e = a_e(1 - \epsilon)$ = semi-minor axis of the earth

K_R = range scale factor

K_D = range-rate scale factor

3. 4. 1 Position and Velocity in the W System and Associated Preliminary Computations

$$w_1 = x \cos a + y \sin a$$

$$w_2 = -x \sin a + y \cos a$$

$$w_3 = z$$

$$\dot{w}_1 = (\dot{x} + \omega_e y) \cos a + (\dot{y} - \omega_e x) \sin a$$

$$\dot{w}_2 = -(\dot{x} + \omega_e y) \sin a + (\dot{y} - \omega_e x) \cos a$$

$$\dot{w}_3 = \dot{z}$$

The following derivation develops quantities that are necessary for transforming the partial derivatives of the earth-centered inertial (ECI) rectangular coordinates to the station-dependent W system. By differentiating the foregoing six expressions it becomes apparent that a simple substitution of $\partial w_j/\partial p_i$ for w_j and $\partial \dot{w}_j/\partial p_i$ for \dot{w}_j , where j=1,2,3, and of $\partial x/\partial p_i$, $\partial y/\partial p_i$, ..., $\partial z/\partial p_i$ for x,y,\ldots , \dot{z} yields

$$\frac{\partial w_1}{\partial p_i} = \frac{\partial x}{\partial p_i} \cos \alpha + \frac{\partial y}{\partial p_i} \sin \alpha$$

$$\frac{\partial w_2}{\partial p_i} = \frac{-\partial x}{\partial p_i} \sin \alpha + \frac{\partial y}{\partial p_i} \cos \alpha$$

etc

Also, differentiating with respect to ℓ , since $\partial \alpha / \partial \ell = 1$,

$$\frac{\partial w_1}{\partial \ell} = -x \sin \alpha + y \cos \alpha = w_2$$

$$\frac{\partial w_2}{\partial t} = -x \cos \alpha - y \sin \alpha = -w_1$$

$$\frac{\partial \dot{\mathbf{w}}_1}{\partial t} = \dot{\mathbf{w}}_2$$

$$\frac{\partial \dot{w}_2}{\partial t} = -\dot{w}_1$$

To find the station position in the W system, the expressions

$$w_1^s = (a_e A_s + h) \cos \Phi^*$$

$$w_3^s = (b_e B_s + h) \sin \Phi^*$$

are used, where

$$A_{s} = \left(\cos^{2}_{\Phi^{*}} + \frac{b_{e}^{2}}{a_{e}^{2}} \sin^{2}_{\Phi^{*}}\right)^{-1/2}$$

$$B_{s} = \left(\sin^{2}\bar{\Phi}* + \frac{a_{e}^{2}}{b_{o}^{2}}\cos^{2}\bar{\Phi}*\right)^{-1/2}$$

Differentiating the expressions for w_1^s and w_3^s with respect to Φ^* and h, then,

$$\frac{\partial w_1^s}{\partial \Phi^*} = -w_3^s - a_e(2\epsilon - \epsilon^2) A_s B_s^2 \sin^3 \Phi^*$$

$$\frac{\partial w_3^s}{\partial \Phi^*} = w_1^s - a_e (2\epsilon - \epsilon^2) A_s^3 \cos^3 \Phi^*$$

$$\frac{\partial w_1^s}{\partial h} = \cos \Phi^*$$

$$\frac{\partial w_3^s}{\partial h} = \sin \Phi^*$$

It is convenient to introduce the three intermediate vectors \boldsymbol{Q} , \boldsymbol{U} , and \boldsymbol{V} and the quantity \boldsymbol{R}_1 , where

 $Q = W - W^8$ = vehicle position relative to the station

with

$$q_1 = w_1 - w_1^s$$

 $q_2 = w_2$
 $q_3 = w_3 - w_3^s$

U = Q/R = a unit vector in the direction of Q, wherein $R = |Q| = \sqrt{q_1^2 + q_2^2 + q_3^2}$,

with

$$u_1 = q_1/R$$
 $u_2 = q_2/R$
 $u_3 = q_3/R$

V = vector U referred to the East/North/Up system

with

$$v_1 = u_2$$
 $v_2 = -u_1 \sin \Phi^* + u_3 \cos \Phi^*$
 $v_3 = u_1 \cos \Phi^* + u_3 \sin \Phi^*$

 $R_1 = vR$

with

$$v = \sqrt{v_1^2 + v_2^2}$$

Then,

$$v_3 = \sin E$$

$$v = \cos E$$

$$\frac{v_2}{v} = \cos A$$

$$\frac{\mathbf{v_1}}{\mathbf{v}} = \sin \mathbf{A}$$

The expression for \dot{v} that is needed to determine $\partial A/\partial t$ and $\partial E/\partial t$ may be obtained by computing $\dot{U} = 1/R[\dot{W} - U\dot{\lambda}] = 1/R[\dot{W} - (U \cdot \dot{W})U]$ whereby

$$\dot{\mathbf{v}}_1 = \dot{\mathbf{u}}_2$$

$$\dot{\mathbf{v}}_2 = -\dot{\mathbf{u}}_1 \sin \Phi^* + \dot{\mathbf{u}}_3 \cos \Phi^*$$

$$\dot{\mathbf{v}} = \frac{\mathbf{v}_1 \dot{\mathbf{v}}_1 + \mathbf{v}_2 \dot{\mathbf{v}}_2}{\mathbf{v}}$$

3.4.2 Range Partials

Differentiating R = $\sqrt{q_1^2 + q_2^2 + q_3^2}$ results in

$$\frac{\partial R}{\partial p_{i}} = U \cdot \frac{\partial Q}{\partial p_{i}} = u_{1} \frac{\partial q_{1}}{\partial p_{i}} + u_{2} \frac{\partial q_{2}}{\partial p_{i}} + u_{3} \frac{\partial q_{3}}{\partial p_{i}}$$

$$\frac{\partial \mathbf{R}}{\partial \Phi^*} = \mathbf{u}_1 \mathbf{w}_3^s - \mathbf{u}_3 \mathbf{w}_1^s$$

$$\frac{\partial \mathbf{R}}{\partial t} = \mathbf{u}_1 \mathbf{w}_2 - \mathbf{u}_2 \mathbf{w}_1$$

$$\frac{\partial R}{\partial h} = -u_1 \cos \Phi^* - u_3 \sin \Phi^*$$

$$\frac{\partial R}{\partial R_{\text{bias}}} = 1$$

$$\frac{\partial R}{\partial K_R} = R$$

$$\frac{\partial \mathbf{R}}{\partial t} = \dot{\mathbf{R}} = (\mathbf{U} \cdot \dot{\mathbf{W}})$$

3.4.3 Azimuth Partials

Differentiating $A = \tan^{-1}(v_{1}/v_{2})$,

$$\frac{\partial A}{\partial p_{i}} = \frac{1}{R_{1}} \left[\frac{\partial w_{2}}{\partial p_{i}} \cos A - \left(-\frac{\partial w_{1}}{\partial p_{i}} \sin \phi * + \frac{\partial w_{3}}{\partial p_{i}} \cos \phi * \right) \sin A \right]$$

$$\frac{\partial A}{\partial \Phi^*} = \frac{\sin A}{R_1} \left(w_1 \cos \Phi^* + w_3 \sin \Phi^* \right)$$

$$\frac{\partial A}{\partial \ell} = \frac{-w_1 \cos A + w_2 \sin \phi^* \sin A}{R_1}$$

$$\frac{\partial A}{\partial h} = 0$$

$$\frac{\partial A}{\partial A_{\text{bias}}} = 1$$

$$\frac{\partial A}{\partial t} = \frac{1}{v^2} (v_2 \dot{v}_1 - v_1 \dot{v}_2)$$

3.4.4 Elevation Partials

Differentiating $E = \sin^{-1} v_3 = \cos^{-1} v$,

$$\frac{\partial E}{\partial p_{i}} = \frac{1}{R_{1}} \left(\frac{\partial w_{i}}{\partial p_{i}} \cos \Phi^{*} + \frac{\partial w_{3}}{\partial p_{i}} \sin \Phi^{*} - \frac{\partial R}{\partial p_{i}} \sin E \right)$$

$$\frac{\partial E}{\partial \Phi^*} = \frac{1}{R_1} \left(w_3 \cos \Phi^* - w_1 \sin \Phi^* - \frac{\partial R}{\partial \Phi^*} \sin E \right)$$

$$\frac{\partial E}{\partial \ell} = \frac{1}{R_1} \left(w_2 \cos \Phi^* - \frac{\partial R}{\partial \ell} \sin E \right)$$

$$\frac{\partial E}{\partial h} = \frac{-1}{R_1} \left(1 + \frac{\partial R}{\partial h} \sin E \right)$$

$$\frac{\partial E}{\partial E_{\text{bias}}} = 1$$

$$\frac{\partial E}{\partial t} = \frac{\dot{u}_1 \cos \phi^* + \dot{u}_3 \sin \phi^*}{\cos E}$$

3.4.5 Range Rate Partials

Differentiating $\dot{R} = (U \cdot \dot{W})$,

$$\frac{\partial \dot{\mathbf{R}}}{\partial \mathbf{p_i}} = \left(\frac{\partial \mathbf{W}}{\partial \mathbf{p_i}} \cdot \dot{\mathbf{U}}\right) + \left(\mathbf{U} \cdot \frac{\partial \dot{\mathbf{W}}}{\partial \mathbf{p_i}}\right)$$

$$\frac{\partial \dot{\mathbf{R}}}{\partial \mathbf{\hat{\Phi}}^*} = \mathbf{w}_3^* \dot{\mathbf{u}}_1 - \mathbf{w}_1^* \dot{\mathbf{u}}_3$$

$$\frac{\partial \dot{R}}{\partial \ell} = (w_2 \dot{u}_1 - w_1 \dot{u}_2) + (\dot{w}_2 u_1 - \dot{w}_1 u_2)$$

$$\frac{\partial \dot{R}}{\partial h} = -\dot{u}_1 \cos \Phi^* - \dot{u}_3 \sin \Phi^*$$

$$\frac{\partial \dot{R}}{\partial \dot{R}_{bias}} = 1$$

$$\frac{\partial \dot{\mathbf{R}}}{\partial \mathbf{K_D}} = \dot{\mathbf{R}}$$

$$\frac{\partial \dot{R}}{\partial t} = \dot{R} = (\dot{U} \cdot \dot{W}) + (U \cdot \dot{W})$$

where

$$\dot{\mathbf{W}} = -\left(\omega_{e}^{2}\mathbf{J} + \frac{\mu}{|\mathbf{X}|^{3}}\mathbf{I}\right)\mathbf{W} + 2\mathbf{L}\dot{\mathbf{X}}$$

$$\mathbf{J} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$L\dot{X} = \begin{pmatrix} -\omega_{e}\dot{x} \sin \alpha + \omega_{e}\dot{y} \cos \alpha \\ -\omega_{e}\dot{x} \cos \alpha - \omega_{e}\dot{y} \sin \alpha \\ 0 \end{pmatrix}$$

$$|X| = \left(\sum_{i=1}^{3} w_i^2\right)^{1/2}$$

3.4.6 P, Q, P, Q, Partials

These partial derivatives are obtained by differencing the R, \dot{R} partials, using the appropriate station locations.

3.4.7 Doppler (Δf) Partials

Differentiating $\Delta f = -K_{\vec{D}} \dot{R}(1 - \dot{R}/c)$ with respect to \dot{R} ,

$$\frac{\partial(\Delta f)}{\partial \dot{R}} = -K_D \left(1 - \frac{2\dot{R}}{c}\right)$$

Then,

$$\frac{\partial(\Delta f)}{\partial p_{\hat{i}}} = \frac{\partial(\Delta f)}{\partial \hat{R}} \cdot \frac{\partial \hat{R}}{\partial p_{\hat{i}}}$$

$$\frac{\partial(\Delta f)}{\partial \phi^*} = \frac{\partial(\Delta f)}{\partial \hat{R}} \cdot \frac{\partial \hat{R}}{\partial \phi^*}$$

$$\frac{\partial(\Delta f)}{\partial l} = \frac{\partial(\Delta f)}{\partial \hat{R}} \cdot \frac{\partial \hat{R}}{\partial l}$$

$$\frac{\partial(\Delta f)}{\partial h} = \frac{\partial(\Delta f)}{\partial \hat{R}} \cdot \frac{\partial \hat{R}}{\partial h}$$

$$\frac{\partial(\Delta f)}{\partial t} = 1$$

$$\frac{\partial(\Delta f)}{\partial t} = \frac{\partial(\Delta f)}{\partial \hat{R}} \cdot \frac{\partial \hat{R}}{\partial t}$$

$$\frac{\partial(\Delta f)}{\partial t} = -\hat{R} \left(1 - \frac{\hat{R}}{c}\right)$$

3.4.8 <u>Topocentric Right Ascension Partials</u>

Differentiating $RA_T = tan^{-1}L_2/L_1 = tan^{-1}(y - y_s)/(x - x_s)$,

$$\frac{\partial RA_{T}}{\partial p_{i}} = \frac{\partial RA_{T}}{\partial x} \frac{\partial x}{\partial p_{i}} \div \frac{\partial RA_{T}}{\partial y} \frac{\partial y}{\partial p_{i}}$$

$$\frac{\partial RA_{T}}{\partial x} = \frac{-L_{2}}{L_{1}^{2} + L_{2}^{2}}$$

$$\frac{\partial \mathbf{R} \mathbf{A}_{\mathbf{T}}}{\partial \mathbf{y}} = -\frac{\mathbf{L}_1}{\mathbf{L}_2} \frac{\partial \mathbf{R} \mathbf{A}_{\mathbf{T}}}{\partial \mathbf{x}}$$

$$\frac{\partial RA_{T}}{\partial \Phi^{*}} = \frac{(y \cos a - x \sin a) \frac{\partial W_{1}^{2}}{\partial \Phi^{*}}}{L_{1}^{2} + L_{2}^{2}}$$

$$\frac{\partial \text{RA}_{\text{T}}}{\partial \ell} = \frac{-(\mathbf{x}_{\text{s}} \mathbf{L}_{1} + \mathbf{y}_{\text{s}} \mathbf{L}_{2})}{\mathbf{L}_{1}^{2} + \mathbf{L}_{2}^{2}}$$

$$\frac{\partial RA}{\partial h} = \frac{(y \cos a - x \sin a)\cos \Phi^*}{L_1^2 + L_2^2}$$

$$\frac{\partial RA_{T}}{\partial RA_{T}} = 1$$

$$\frac{\partial RA_{T}}{\partial t} = \frac{L_{1}(\dot{y} - \omega_{e}x_{s}) - L_{2}(\dot{x} + \omega_{e}y_{s})}{L_{1}^{2} + L_{2}^{2}}$$

3.4.9 Topocentric Declination Partials

Differentiating $D_T = \sin^{-1}L_3/R = \sin^{-1}(z - z_s)/[(x - x_s)^2 + (y - y_s)^2 + (z - z_s)^2]^{1/2}$

$$\frac{\partial \mathbf{D_T}}{\partial \mathbf{p_i}} = \frac{\partial \mathbf{D_T}}{\partial \mathbf{x}} \frac{\partial \mathbf{x}}{\partial \mathbf{p_i}} + \frac{\partial \mathbf{D_T}}{\partial \mathbf{y}} \frac{\partial \mathbf{y}}{\partial \mathbf{p_i}} + \frac{\partial \mathbf{D_T}}{\partial \mathbf{p_i}} + \frac{\partial \mathbf{D_T}}{\partial \mathbf{z}} \frac{\partial \mathbf{z}}{\partial \mathbf{p_i}}$$

$$\frac{\partial D_{T}}{\partial x} = \frac{-L_{1}L_{3}}{R^{2}\left(L_{1}^{2} + L_{2}^{2}\right)^{1/2}}$$

$$\frac{\partial \mathbf{D_T}}{\partial \mathbf{y}} = \frac{\mathbf{L_2}}{\mathbf{L_1}} \frac{\partial \mathbf{D_T}}{\partial \mathbf{x}}$$

$$\frac{\partial \mathbf{D_T}}{\partial \mathbf{z}} = \frac{\left(\mathbf{L_1^2 + L_2^2}\right)^{1/2}}{\mathbf{p}^2}$$

$$\frac{\partial \mathbf{D_T}}{\partial \boldsymbol{\Phi}^*} = \frac{\left(\mathbf{w_1} - \mathbf{w_1^s}\right) \mathbf{L_3} \frac{\partial \mathbf{w_1^s}}{\partial \boldsymbol{\Phi}^*} + \left(\mathbf{L_1^2} + \mathbf{L_2^2}\right) \frac{\partial \mathbf{w_3^s}}{\partial \boldsymbol{\Phi}^*}}{\mathbf{R^2 \left(\mathbf{L_1^2} + \mathbf{L_2^2}\right)^{1/2}}}$$

$$\frac{\partial D_{T}}{\partial t} = \frac{L_{3} \left(x_{s} y - y_{s} x \right)}{R^{2} \left(L_{1}^{2} + L_{2}^{2} \right)^{1/2}}$$

$$\frac{\partial D_{T}}{\partial h} = \frac{1}{R^{2} (L_{1}^{2} + L_{2}^{2})^{1/2}} \left\{ -R^{2} \sin \bar{\Psi}^{*} + L_{3} \left[(w_{1} - w_{1}^{s}) \cos \bar{\Phi}^{*} + (w_{3} - w_{3}^{s}) \sin \bar{\Phi}^{*} \right] \right\}$$

$$\frac{\partial D_{T}}{\partial D_{T(bias)}} = 1$$

$$\frac{\partial D_{T}}{\partial t} = \frac{- L_{3} [L_{1}\dot{x} + L_{2}\dot{y} + (xy_{x} - yx_{s})\omega_{e}] + \dot{z}(L_{1}^{2} + L_{2}^{2})}{R^{2}(L_{1}^{2} + L_{2}^{2})^{1/2}}$$

3. 4. 10 Topocentric Four Angle Partials

Differentiating $HA_T = a - RA_T$,

$$\frac{\partial \mathbf{H} \mathbf{A}_{\mathbf{T}}}{\partial \mathbf{p_i}} = -\frac{\partial \mathbf{R} \mathbf{A}_{\mathbf{T}}}{\partial \mathbf{p_i}}$$

$$\frac{\partial \text{HA}_{\text{T}}}{\partial \Phi^*} = -\frac{\partial \text{RA}_{\text{T}}}{\partial p_{\xi}}$$

$$\frac{\partial HA_{T}}{\partial \ell} = 1 - \frac{\partial RA_{T}}{\partial \ell}$$

$$\frac{\partial \mathrm{HA}_{\mathrm{T}}}{\partial \mathrm{h}} = -\frac{\partial \mathrm{RA}_{\mathrm{T}}}{\partial \mathrm{h}}$$

$$\frac{\text{AHA}_{\text{T}}}{\text{AHA}_{\text{T}}} = 1$$

$$\frac{\partial HA_{T}}{\partial t} = \omega_{e} - \frac{\partial RA_{T}}{\partial t}$$

3. 4. 11 Geocentric Right Ascension Partials

Differentiating $a = \tan^{-1}(y/x)$,

$$\frac{\partial a}{\partial p_i} = \frac{\partial a}{\partial x} \quad \frac{\partial x}{\partial p_i} + \frac{\partial a}{\partial y} \quad \frac{\partial y}{\partial p_i}$$

Also,

$$\frac{\partial a}{\partial x} = \frac{-y}{x^2 + y^2}$$

$$\frac{\partial \alpha}{\partial y} = \frac{x}{x^2 + y^2}$$

$$\frac{\partial a}{\partial a \text{(bias)}} = 1$$

$$\frac{\partial a}{\partial t} = \frac{x\dot{y} - y\dot{x}}{x^2 + y^2}$$

3.4.12 Geocentric Declination Partials

Differentiating $\delta = \tan^{-1} \left(z / \sqrt{x^2 + y^2} \right)$,

$$\frac{\partial \delta}{\partial \mathbf{p_i}} = \frac{\partial \delta}{\partial \mathbf{x}} \frac{\partial \mathbf{x}}{\partial \mathbf{p_i}} + \frac{\partial \delta}{\partial \mathbf{y}} \frac{\partial \mathbf{y}}{\partial \mathbf{p_i}} + \frac{\partial \delta}{\partial \mathbf{z}} \frac{\partial \mathbf{z}}{\partial \mathbf{p_i}}$$

where

$$\frac{\partial \delta}{\partial x} = \frac{-xz}{(x^2 + y^2)^{1/2}(x^2 + y^2 + z^2)}$$

$$\frac{\partial \delta}{\partial y} = \frac{-yz}{(x^2 + y^2)^{1/2}(x^2 + y^2 + z^2)}$$

$$\frac{\partial \delta}{\partial z} = \frac{(x^2 + y^2)^{1/2}}{x^2 + y^2 + z^2}$$

Also,

$$\frac{\partial \delta}{\partial \delta}$$
 = 1

$$\frac{\partial \delta}{\partial t} = \frac{z(x\dot{x} + y\dot{y}) + \dot{z}(x^2 + y^2)}{(x^2 + y^2)^{1/2}(x^2 + y^2 + z^2)}$$

3.4.13 Horizon Scanner Angle (u) Partials

Differentiating $u = \sin^{-1}(N_1 \times \xi)$

$$\frac{\partial \mathbf{u}}{\partial \mathbf{p_i}} = \frac{\partial \mathbf{u}}{\partial \mathbf{X}} \frac{\partial \mathbf{X}}{\partial \mathbf{p_i}}$$

$$\frac{\partial \mathbf{u}}{\partial \mathbf{X}} = \frac{\mathbf{n}^{\mathrm{T}}}{\mathbf{R}}$$

$$\frac{\partial \mathbf{u}}{\partial \mathbf{u}(\text{bias})} = 1$$

$$\frac{\partial \mathbf{u}}{\partial \mathbf{t}} = \frac{\partial \mathbf{u}}{\partial \mathbf{X}} \dot{\mathbf{X}}$$

3.4.14 Horizon Scanner Angle (v) Partials

Differentiating $v = tan^{-1} (sin u tan i)$,

$$\frac{\partial \mathbf{v}}{\partial \mathbf{p_i}} = \frac{\partial \mathbf{v}}{\partial \mathbf{X}} \frac{\partial \mathbf{X}}{\partial \mathbf{p_i}}$$

Also,

$$\frac{\partial \mathbf{v}}{\partial \mathbf{X}} = \frac{\mathbf{\Sigma}^{\mathbf{T}}}{\mathbf{R}}$$

$$\frac{\partial \mathbf{v}}{\partial \mathbf{v}} = 1$$

$$\frac{\partial \mathbf{v}}{\partial \mathbf{t}} = \frac{\partial \mathbf{v}}{\partial \mathbf{X}} \dot{\mathbf{X}}$$

3.4.15 Height (h) Partials

$$\frac{\partial \mathbf{h}}{\partial \mathbf{p_i}} = \frac{\partial \mathbf{h}}{\partial \mathbf{x}} \frac{\partial \mathbf{x}}{\partial \mathbf{p_i}}$$

Also,

$$\frac{\partial \mathbf{h}}{\partial \mathbf{X}} = \left(\frac{\partial \mathbf{h}}{\partial \mathbf{x}}, \frac{\partial \mathbf{h}}{\partial \mathbf{y}}, \frac{\partial \mathbf{h}}{\partial \mathbf{z}}\right)$$

where

$$\frac{\partial h}{\partial x} = \frac{x}{r} \left\{ 1 - \frac{a_e \epsilon (2 - 3\epsilon + \epsilon^2) z^2}{\left[r^2 - (2\epsilon - \epsilon^2)(x^2 + y^2)\right]^{3/2}} \right\}$$

$$\frac{\partial h}{\partial y} = \frac{y}{r} \left\{ 1 - \frac{a_e \epsilon (2 - 3\epsilon + \epsilon^2) z^2}{\left[r^2 - (2\epsilon - \epsilon^2)(x^2 + y^2)\right]^{3/2}} \right\}$$

$$\frac{\partial h}{\partial z} = \frac{z}{r} \left\{ 1 - \frac{a_e \epsilon (2 - 3\epsilon + \epsilon^2)(x^2 + y^2)}{\left[r^2 - (2\epsilon - \epsilon^2)(x^2 + y^2)\right]^{3/2}} \right\}$$

$$\frac{\partial h}{\partial h_{(bias)}} = 1$$

$$\frac{\partial \mathbf{h}}{\partial \mathbf{t}} = \frac{\partial \mathbf{h}}{\partial \mathbf{X}} \dot{\mathbf{X}}$$

3, 4, 16 Cartesian Earth-Fixed (x, y, z) Partials

Differentiating $\hat{x} = x \cos a + y \sin a$,

$$\frac{\partial_{\mathbf{x}}^{\wedge}}{\partial \mathbf{p_i}} = \cos \alpha \, \frac{\partial_{\mathbf{x}}}{\partial \mathbf{p_i}} + \sin \alpha \, \frac{\partial_{\mathbf{y}}}{\partial \mathbf{p_i}}$$

$$\frac{\partial \dot{x}}{\partial t} = \dot{x} \cos a + \dot{y} \sin a + \omega_{e}(y \cos a - x \sin a)$$

Differentiating $\mathring{y} = y \cos a - x \sin a$,

$$\frac{\partial \hat{y}}{\partial p_{i}} = -\sin \alpha \frac{\partial x}{\partial p_{i}} + \cos \alpha \frac{\partial y}{\partial p_{i}}$$

$$\frac{\partial \dot{y}}{\partial t} = -\dot{x} \sin a + \dot{y} \cos a - \omega_{e}(x \cos a + y \sin a)$$

Also, since $\hat{z} = z$,

$$\frac{\partial \mathbf{z}^{\wedge}}{\partial \mathbf{p_i}} = \frac{\partial \mathbf{z}}{\partial \mathbf{p_i}}$$

$$\frac{\partial_{\mathbf{z}}^{\Lambda}}{\partial \mathbf{p}_{t}} = \dot{\mathbf{z}}$$

3.4.17 Å, È Partials

The TRACE-D program does not accept A and E as observations, but can calculate these quantities for the benefit of tracking stations and can compute the variance of the quantities A, E, R, A, E, and R, given a covariance matrix for the trajectory parameters. The partial derivatives of A and E, which are required for calculation of these variances, may be written as

$$\begin{split} &\frac{\partial \dot{A}}{\partial p_{i}} = \frac{1}{Rv} \left\{ \cos A \left[\frac{\partial \dot{w}_{2}}{\partial p_{i}} + \dot{A} \left(\frac{\partial w_{1}}{\partial p_{i}} \sin \Phi^{*} - \frac{\partial w_{3}}{\partial p_{i}} \cos \Phi^{*} \right) \right] \right\} \\ &+ \sin A \left[\left(\frac{\partial \dot{w}_{1}}{\partial p_{i}} \sin \Phi^{*} - \frac{\partial \dot{w}_{3}}{\partial p_{i}} \cos \Phi^{*} \right) - \dot{A} \frac{\partial w_{2}}{\partial p_{i}} \right] - (\dot{R}v + R\dot{v}) \frac{\partial A}{\partial p_{i}} \end{split}$$

and

$$\frac{\partial \dot{\mathbf{E}}}{\partial \mathbf{p_i}} = \frac{1}{Rv} \left[\frac{\partial \dot{\mathbf{w}_1}}{\partial \mathbf{p_i}} \cos \Phi^* + \frac{\partial \dot{\mathbf{w}_3}}{\partial \mathbf{p_i}} \sin \Phi^* - \frac{\partial \dot{\mathbf{R}}}{\partial \mathbf{p_i}} \sin \mathbf{E} - \dot{\mathbf{E}} \frac{\partial \mathbf{R}}{\partial \mathbf{p_i}} \cos \mathbf{E} \right]$$
$$- (\dot{\mathbf{R}}\mathbf{v} + \mathbf{R}\dot{\mathbf{v}}) \frac{\partial \mathbf{E}}{\partial \mathbf{p_i}}$$

3.5 DATA GENERATION CALCULATIONS

The formulas for computing data for the data generation function are a subset of the formulas presented in Sections 3.1 through 3.4, except as otherwise noted in Sections 3.5.1 through 3.5.12.

3.5.1 Rise-Set Prediction

The expression

$$\underline{r} \cdot R_s - rR_s \cos\left(\frac{\pi}{2} - E_m - \sin^{-1}\frac{R_s \cos E_m}{r}\right) = 0$$

where

r = vehicle position vector

R_s = station position vector

E = elevation angle

E_m = input minimum elevation or input maximum elevation, whichever applicable

holds when the elevation E is equal to E_m in a two-body model. This expression is positive when $E > E_m$ and negative when $E < E_m$. Preliminary values of rise-set times are generated by converting the above expression to a function of eccentric anomaly, θ , stepping from θ_0 to $\theta_0 + 2\pi$, and noting the times of the appropriate sign changes.

3.5.2 Rise and Set Times

The actual rise-set times may be computed from the integrated trajectory by use of the expressions

$$t_{\text{(rise or set)}} = t_n + \Delta t$$

$$\Delta t = -\left[\frac{v_3 - \sin(E_m)}{\dot{u}_1 \cos \Phi^* + \dot{u}_3 \sin \Phi^*}\right]$$

where

t_n = current time

 v_3 , \dot{u}_i = values as defined in Section 3.4.1

3.5.3 Elevation Angle Refraction Correction

The computed elevation angles (E) are corrected for atmospheric refraction effects by means of the expressions

$$E' = E + \eta_{si} \cot E$$
 ($E \ge 0.1 \text{ radian}$)

E' = E +
$$\frac{1}{1000} \cdot \frac{\eta_{si} \times 10^6}{12 + 1000E} - \frac{80}{6 + 1000E}$$
 (E < 0.1 radian)

where

E = geometric elevation angle

E' = elevation angle measured by radar (data generation output quantity)

 $\eta_{si} = \text{appropriate refractivity index from REFR table}$ (if $\eta_{si} = 0$, no refraction correction is applied)

3.5.4 Observations with Normally Distributed Random Noise

For observations accompanied by normally distributed random noise,

$$o = o_c + r_n$$

where

o = observation output on data generation run

o_c = nominal computed observation

 $r_n = added noise$

and

$$r_n = n_{\sigma_{sj}} + \beta_{sj}$$

where

 σ_{sj} = appropriate sigma for Type j, Station s

 β_{sj} = appropriate bias (if any)

n = a random element from a set of numbers with mean zero and unity standard deviation

3.5.5 Aspect Angles

Aspect angles Φ and θ as shown in Figure 3-13 are defined respectively as the angle between the negative yaw axis and the projection of the range vector

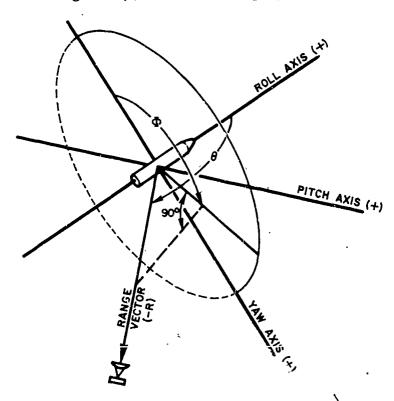


Figure 3-13. Aspect Angles with Respect to Vehicle-Centered Coordinates

in the roll plane, and as the angle between the positive roll axis and the range vector. The (+) roll direction is the in-track direction and the yaw axis is coincident with the geocentric radius vector.

To compute these angles, the vector from the vehicle to the station first is transformed from the basic coordinate system to the vehicle-centered system. It should be noted that the range vector is taken in the sense opposite to the convention adopted for the TRACE-D program for consistency with radar antenna pattern conventions (Ref. 7). Thus,

$$R_1 = A_{1, 2}(-R)$$

where

$$A_{1,2} = \begin{bmatrix} -(\sin A \sin \alpha & (\sin A \cos \alpha + \cos A \sin \delta \cos \alpha) & -\cos A \sin \delta \sin \alpha) & \cos A \cos \delta \\ -(\cos A \sin \alpha & (\cos A \cos \alpha - \sin A \sin \delta \cos \alpha) & +\sin A \sin \delta \sin \alpha) & -\sin A \cos \delta \\ -\cos \delta \cos \alpha & -\cos \delta \sin \alpha & -\sin \delta \end{bmatrix}$$

and wherein A is the inertial azimuth angle, α is right ascension, and δ is geocentric declination of the vehicle.

The vector is then further transformed through the yaw, pitch, and roll angles which describe the instantaneous attitude of the vehicle, or

$$R_2 = A_{2,3}R_1$$

where

$$A_{2,3} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{\mathbf{r}} & \sin\theta_{\mathbf{r}} \\ 0 & -\sin\theta_{\mathbf{r}} & \cos\theta_{\mathbf{r}} \end{bmatrix} \begin{bmatrix} \cos\theta_{\mathbf{p}} & 0 & -\sin\theta_{\mathbf{p}} \\ 0 & 1 & 0 \\ \sin\theta_{\mathbf{p}} & 0 & \cos\theta_{\mathbf{p}} \end{bmatrix} \begin{bmatrix} \cos\theta_{\mathbf{y}} & \sin\theta_{\mathbf{y}} & 0 \\ -\sin\theta_{\mathbf{y}} & \cos\theta_{\mathbf{y}} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

and wherein θ_y , θ_p , θ_r are the instantaneous yaw, pitch, and roll angles as calculated from input attitude-control data.

If then

$$R_{2} = \begin{bmatrix} R_{2x} \\ R_{2y} \\ R_{2z} \end{bmatrix}$$

the desired angles are given by

$$\cos \Phi = \frac{-R_{2z}}{\sqrt{R_{2y}^2 + R_{2z}^2}}$$

$$\sin \Phi = \frac{R_{2y}}{\sqrt{R_{2y}^2 + R_{2z}^2}}$$

$$\cos \theta = \frac{R_{2x}}{\sqrt{R_{2x}^2 + R_{2y}^2 + R_{2z}^2}}$$

3.5.6 Look Angle

The look-angle computation is similar to that for θ above, or

$$\cos \theta_{L} = \frac{R \cdot b}{|R|}$$

where

R = station-to-vehicle range vector
(The components of b are the direction cosines of one of the missile axes in the basic coordinate system. The b components are completely arbitrary and independent of the aspect-angle computations.)

3.5.7 Observation Variances

The uncertainties in observations which are due to trajectory uncertainties that in turn result from uncertainties in the initial conditions and differential equation parameters can be computed by

$$C(O_t) = \left(\frac{\partial O_t}{\partial X_t}\right) \left(\frac{\partial X_t}{\partial P_o}\right) C(P_o) \left(\frac{\partial X_t}{\partial P_o}\right)^T \left(\frac{\partial O_t}{\partial X_t}\right)^T$$

where

 $C(O_t)$ = covariance matrix of generated observations (diagonal)

\frac{\partial}{\partial} = \text{matrix of partial derivatives of observations with respect to trajectory position}

\frac{\partial}{\partial} = \text{matrix of trajectory partial derivatives or solutions} \text{of variational equations}

C(P_o) = a priori covariance matrix of initial-condition and differential-equation parameters

Only variances (not covariances) are computed, and these only for the quantities R, A, E, \dot{R} , \dot{A} , \dot{E} .

3.5.8 Surface Range

The surface range equation is

$$R_{surf} = cos^{-1}[sin \delta sin \phi + cos \delta cos \phi cos(\ell - \lambda)]$$

where

$$\phi = \tan^{-1}[(1 - \epsilon)^2 \tan \Phi^*]$$

 δ = géocentric declination of intersection of radius vector and ellipsoid

 Φ * = geodetic latitude of station

1 = longitude of station

 λ = longitude of vehicle (east from Greenwich)

 ϵ = ellipticity of reference ellipsoid

3.5.9 Height

The equation for height is

h = r -
$$\frac{a_e(1 - \epsilon)}{\left[1 - (2\epsilon - \epsilon^2)\frac{x^2 + y^2}{r^2}\right]^{1/2}}$$

where

r = geocentric radius to vehicle

a = equatorial radius of the earth

 ϵ = ellipticity of reference ellipsoid

3.5.10 Kappa (K)

Kappa, or the angle between the slant-range vector and the geocentric radius vector to a vehicle, is given by

$$K = \cos^{-1} \left[\frac{r^2 + R^2 - (w_1^s)^2 - (w_3^s)^2}{2rR} \right]$$

where

R = slant range

r = geocentric distance to vehicle

 w_1^s , w_3^s = station position in W system

3.5.11 Doppler

The doppler frequency shift is computed by

$$\Delta f = -K_{\hat{D}}\dot{R}\left(1 - \frac{\dot{R}}{c}\right)$$

where

 $K_D = an input constant(C(29))$

c = speed of light (INTEG(40))

3.5.12 Attenuation

Attenuation is obtained from

$$A = -40 \log_{10} R$$

where

A = amplitude attenuation in decibels

R = slant range in feet

3.6 TRAJECTORY

The position and velocity components X = (x, y, z) and $\dot{X} = (\dot{x}, \dot{y}, \dot{z})$ of the vehicle and their partial derivatives X_{p_i} and \dot{X}_{p_i} (i = 1, 2, 3, ..., n) with respect to the trajectory initial-condition and differential-equation parameters are functions of time defined by their differential equations and appropriate initial conditions. The equations are integrated numerically, and at each observation or print time all the quantities X, \dot{X} , \dot{X}_{p_i} and \dot{X}_{p_i} (i = 1, 2, 3, ..., n) are obtained by interpolation in the integrated results. From these the computed radar observations and their partial derivatives and the trajectory output are obtained (see Section 3.3 and 3.4).

3. 6. 1 Differential Equations

The equations of motion of the vehicle follow from

$$\ddot{X} = \frac{-\mu X}{r^3} + F$$

where

 μ = gravitational constant (GM) of the earth

$$r = |X| = (x^2 + y^2 + z^2)^{1/2}$$

F = F₁ + F₂ + F₃ + F₄ = perturbative acceleration due to asphericity of the earth, extraterrestrial gravitational forces, atmospheric drag, and low thrust, respectively.

The initial conditions $X(t_0)$ and $X(t_0)$, if not given directly, are computed from the initial spherical coordinates or elliptic elements (see Section 3.2 for applicable formulas).

The perturbative acceleration F_1 due to the asphericity of the earth is derived from the assumed potential function

$$U = \frac{\mu}{r} \left[1 - \sum_{n=2}^{n_1} J_n \left(\frac{a_e}{r} \right)^n P_n(\sin \phi) + \sum_{n=2}^{n_2} \sum_{m=1}^{n} J_{nm} \left(\frac{a_e}{r} \right)^n P_n^m(\sin \phi) \cos m(\lambda - \lambda_{nm}) \right]$$

where

μ = product (GM) of the Newtonian gravitational constant and mass of the earth

r, ϕ , λ = geocentric distance, geocentric latitude, and (east) longitude of a point

a = mean equatorial radius of the earth

J_n, J_{nm} = numerical coefficients

 $P_n = Legendre polynomial of the first kind of degree <math>n < n_1$

P_n^m = associated Legendre function of the first kind of degree n<n₂ and order m

 λ_{nm} = longitudes associated with the J_{nm}

In the local horizontal coordinate system, in which the coordinate axes are directed Up (along the radius vector), East, and North, the F_l force components g_U , g_E , and g_N are given by

$$g_{U} = \frac{\partial U}{\partial r}$$

$$= -\frac{\mu}{r^{2}} \left[1 - \sum_{n=2}^{n} (n+1) J_{n} \left(\frac{a_{e}}{r} \right)^{n} P_{n}(\sin \phi) + \sum_{n=2}^{n} \sum_{m=1}^{n} (n+1) J_{nm} \left(\frac{a_{e}}{r} \right)^{n} P_{n}^{m}(\sin \phi) \cos m(\lambda - \lambda_{nm}) \right]$$

$$g_E = \frac{1}{r \cos \phi} \frac{\partial U}{\partial \lambda}$$

$$=-\frac{\mu}{r^2}\sum_{n=2}^{n}\sum_{m=1}^{n}mJ_{nm}\left(\frac{a_e}{r}\right)^n\frac{P_n^m(\sin\phi)}{\cos\phi}\sin m(\lambda-\lambda_{nm})$$

and

$$g_N = \frac{1}{r} \frac{\partial U}{\partial \phi}$$

$$= -\frac{\mu}{r^2} \left[\sum_{n=2}^{n_1} J_n \left(\frac{a_e}{r} \right)^n P'_n (\sin \phi) \cos \phi \right]$$

$$-\sum_{n=2}^{n} \sum_{m=1}^{n} J_{nm} \left(\frac{a_e}{r}\right)^n P_n^{m'} (\sin \phi) \cos \phi \cos m(\lambda - \lambda_{nm})$$

Also, the Legendre functions and their derivatives are computed from the recursion formulas

$$P_{n}(\sin \phi) = \frac{-(n-1)P_{n-1}(\sin \phi) + (2n-1)\sin \phi P_{n-1}(\sin \phi)}{n}$$

$$P_{\tilde{n}}^{1}(\sin \phi) = \sin \phi P_{\tilde{n}-1}^{1} (\sin \phi) + nP_{\tilde{n}-1}(\sin \phi)$$

$$\frac{P_n^m(\sin\phi)}{\cos\phi} = \frac{-(n+m-1)\frac{P_{n-2}^m(\sin\phi)}{\cos\phi} + (2n-1)\sin\phi\frac{P_{n-1}^m(\sin\phi)}{\cos\phi}}{n-m}$$

$$\frac{P_{m}^{m}(\sin \phi)}{\cos \phi} = 1 \cdot 3 \cdot \dots (2m-1)(\cos \phi)^{m-1}$$

and

$$P_n^{m'}(\sin\phi)\cos\phi = (n+1)\sin\phi \frac{P_n^{m}(\sin\phi)}{\cos\phi} - (n-m+1)\frac{P_{n+1}^{m}(\sin\phi)}{\cos\phi}$$

wherein the initial values are

$$P_{O}(\sin \phi) = P'_{1}(\sin \phi) = 1$$

$$P_{1}(\sin \phi) = \sin \phi,$$

$$\frac{P_{m-1}^{m} (\sin \phi)}{\cos \phi} = 0$$

The force vector in the ECI coordinate system is then

$$\begin{bmatrix} g_x \\ g_y \\ g_z \end{bmatrix} = \begin{bmatrix} \cos \phi \cos \alpha & -\sin \alpha & \sin \phi \cos \alpha \\ \cos \phi \sin \alpha & \cos \alpha & -\sin \phi \sin \alpha \\ \sin \phi & 0 & \cos \phi \end{bmatrix} \begin{bmatrix} g_U \\ g_E \\ g_N \end{bmatrix}$$

where

$$\alpha = \alpha_g + \omega_e(t - t_g) = right ascension$$

The gravitational attraction of other bodies contributes the effect

$$F_2 = -\mu \sum_{j=1}^k m_j \left(\frac{x - x_j}{|x - x_j|^3} + \frac{x_j}{|x_j|^3} \right)$$

where

m; = mass relative to the earth of jth body

X. = vector position of jth body as obtained from the JPL/STL planetary coordinate tapes.

In connection with the JPL/STL planetary tapes (Ref. 8) it should be noted that the tabular planetary coordinates are with respect to the Mean Equator and Equinox 1950.0 coordinate system whereas TRACE-D program calculations are referred to 0 hour GMT of start day. The planetary coordinates are transferred to the TRACE-D coordinate system before F₂ is calculated (Refs. 9 and 10).

The effect of atmospheric arag is expressed by

$$\mathbf{F}_3 = -\rho \left(\frac{\mathbf{V}_A}{2}\right) \left(\frac{\mathbf{C}_D^A}{\mathbf{W}}\right) \dot{\mathbf{x}}_A$$

where

 ρ = density at height h above the oblate earth

with

$$h = r - \frac{a_e(1-\epsilon)}{\left[1 - (2\epsilon - \epsilon^2)\frac{x^2 + y^2}{r^2}\right]^{1/2}}$$

 $\frac{C_D^A}{W} = \text{drag coefficient (reciprocal of "ballistic coefficient")}$

 \dot{X}_{A} = vehicle velocity vector relative to rotating atmosphere

with

$$\dot{x}_{A} = \dot{x} + \omega_{a}y$$

$$\dot{y}_{A} = \dot{y} - \omega_{a}x$$
(where ω_{a} is the rotation rate of the atmosphere)
$$\dot{z}_{A} = \dot{z}$$

$$V_{A} = |\dot{X}_{A}|$$

The atmospheric density is computed from an atmosphere model or certain combinations of models (Refs. 11 and 12).

The low-thrust term F₄, which simulates only a special form of acceleration such as might be due to the influence of residual gases, may be expressed as

$$F_4 = T_1 e^{-T_2(t-t_s)} \frac{\dot{x}}{|\dot{x}|} \qquad (for t_s \le t \le t_f)$$

or

$$F_4 = 0$$
 (otherwise)

where

T₁ = initial magnitude of acceleration

T₂ = time constant for thrust decây

 t_s , t_f = start and finish times

X = inertial velocity vector

It should be recognized that arbitrary velocity impulses, or "kicks," also may be inserted into a trajectory profile. These velocity increments are described by the time of application t_K of the magnitude K of the kick, and by the deflections θ_p and θ_y in pitch and yaw, respectively, of the direction of the kick from the in-track vector. θ_p and θ_y are referenced to the in-track vector in accordance with the coordinate conventions previously specified in Figure 3-7.

The vector velocity increment then is

$$\Delta \underline{\mathbf{v}} = \mathbf{K} (\sin \theta_{\mathbf{p}} \mathbf{X}_{\mathbf{y}} + \cos \theta_{\mathbf{p}} \cos \theta_{\mathbf{y}} \mathbf{X}_{\mathbf{r}} + \cos \theta_{\mathbf{p}} \sin \theta_{\mathbf{y}} \mathbf{X}_{\mathbf{p}})$$

where

$$X_y$$
 = yaw axis = $\frac{X}{|X|}$ = unit vector in radial direction
 X_p = pitch axis = $\frac{X \times \dot{X}}{|X \times \dot{X}|}$ = unit vector normal to orbit plane
 X_r = roll axis = $X_p \times X_v$ = unit vector in in-track direction

3.6.2 frajectory Partial Derivatives

The partial derivatives of vehicle position and velocity with respect to trajectory parameters either can be approximated analytically or can be obtained by a simultaneous numerical integration of the variational equations.

3. 6. 2. 1 Variational Equations

The variational equation for an initial-condition parameter à is

$$\ddot{X}_{\alpha} = \left[\frac{\partial}{\partial X} \left(-\frac{\mu X}{r^3} \right) + \frac{\partial F}{\partial X} \right] X_{\alpha} + \frac{\partial F}{\partial \dot{X}} \dot{X}_{\alpha}$$

with initial conditions $X_a(t_o) = (\partial X/\partial a)t_o$, $\dot{X}_a(t_o) = (\partial X/\partial a)t_o$. Also, for any differential-equation parameter β , except the specific case where the parameter is μ (i.e., GM) (see Section 3.6.2.3), the variational equation is

$$\ddot{\mathbf{x}}_{\beta} = \left[\frac{\partial}{\partial \mathbf{x}} \left(-\frac{\mu \mathbf{x}}{\mathbf{x}} \right) + \frac{\partial \mathbf{F}}{\partial \mathbf{x}} \right] \mathbf{x}_{\beta} + \frac{\partial \mathbf{F}}{\partial \dot{\mathbf{x}}} \dot{\mathbf{x}}_{\beta} + \frac{\partial \mathbf{F}}{\partial \beta}$$

with initial conditions $X_{\beta}(t_0) = \dot{X}_{\beta}(t_0) = 0$.

In the foregoing expressions for \ddot{X}_{α} and \ddot{X}_{β} , $\ddot{X}_{\alpha} = \partial X/\partial \alpha$, $\dot{X}_{\alpha} = \partial \dot{X}/\partial \alpha$, and \ddot{X}_{β} , \dot{X}_{β} and $\partial F/\partial \beta$ are all 3-component vectors. The contents of the square brackets and $\partial F/\partial \dot{X}$ are 3 × 3 matrices. The system is solved for each parameter, and all the numerical integrations are carried out simultaneously.

The matrix in square brackets is calculated as the sum V + T, where

$$V = \frac{\partial}{\partial x} \left(-\frac{uX}{r^3} \right) + \frac{\partial F_1}{\partial x}$$

$$T = \frac{\partial F_3}{\partial X}$$

represent the dependence of the gravitational and drag accelerations, respectively, upon the position of the vehicle. The other-body term $\partial F_2/\partial X$ is ignored (see Appendices B and C for derivations of the V and T matrices). The matrix $\partial F/\partial \dot{X}$ then is

$$\frac{\partial \mathbf{F}_3}{\partial \dot{\mathbf{X}}} + \frac{\partial \mathbf{F}_4}{\partial \dot{\mathbf{X}}}$$

where

$$\frac{\partial \mathbf{F}_{3}}{\partial \dot{\mathbf{X}}} = -\frac{1}{2} \rho \mathbf{V}_{A} \frac{\mathbf{C}_{D}^{A}}{\mathbf{W}} \left(\frac{\dot{\mathbf{X}}_{A} \mathbf{X}_{A}^{T}}{\mathbf{V}_{A}^{2}} + \mathbf{I} \right)$$

$$\frac{\partial F_4}{\partial \dot{x}} = \left(T_1 e^{-T_2(t-t_s)}\right) \quad \frac{\partial}{\partial \dot{x}} \left(\frac{\dot{x}}{|\dot{x}|}\right) = \frac{T_1 e^{-T_2(t-t_s)}}{|\dot{x}|} \quad \left[I - \frac{\dot{x}\dot{x}^T}{|\dot{x}|^2}\right]$$

It should be noted that for the two initial-condition parameters a (right ascension) and Ω (right ascension of the ascending node), analytic solutions for the variational equations are available when the forces upon the vehicle are symmetric about the polar axis. The solutions for a,

$$\frac{\partial x}{\partial a} = -y$$

$$\frac{\partial \dot{x}}{\partial a} = -\dot{y}$$

$$\frac{\partial \dot{y}}{\partial a} = \dot{x}$$

$$\frac{\partial \dot{z}}{\partial a} = 0$$

$$\frac{\partial \dot{z}}{\partial a} = 0$$

and similarly those for Ω are employed in TRACE-D. The additional terms arising from the tesseral harmonics in the geopotential and longitudinal density variations are ignored (see Appendix D for derivation of foregoing equations).

3.6.2.2 Variational-Equation Initial Conditions

Paragraphs 3. 6. 2. 2. 1 through 3. 6. 2. 2. 3 define initial conditions $X_{\alpha}(t_0)$ and $X_{\alpha}(t_0)$ for the variational equations for the parameters of initial position and velocity in rectangular and spherical coordinates and in elliptic orbital elements.

3.6.2.2.1 Rectangular Coordinates

$$\begin{pmatrix} \frac{\partial X}{\partial X} \end{pmatrix}_{t_{0}} = \begin{pmatrix} \frac{\partial \dot{X}}{\partial \dot{X}} \end{pmatrix}_{t_{0}} = I \qquad \text{(the 3 × 3 identity matrix)}$$

$$\begin{pmatrix} \frac{\partial X}{\partial \dot{X}} \end{pmatrix}_{t_{0}} = \begin{pmatrix} \frac{\partial \dot{X}}{\partial X} \end{pmatrix}_{t_{0}} = 0$$

3.6.2.2.2 Spherical Coordinates

a (Right ascension)

(Initial conditions are not required for this parameter due to the fact that an analytic solution of the variational equation for α is employed.)

δ (Declination)

$$\frac{\partial \mathbf{x}}{\partial \delta} = -\mathbf{r} \sin \delta \cos \alpha$$

$$\frac{\partial y}{\partial \delta} = -r \sin \delta \sin \alpha$$

$$\frac{\partial z}{\partial \delta} = r \cos \delta$$

$$\frac{\partial \dot{x}}{\partial \delta} = -\dot{z} \cos \alpha$$

$$\frac{\partial \dot{y}}{\partial \delta} = -\dot{z} \sin \alpha$$

$$\frac{\partial \hat{z}}{\partial \delta} = v (\cos \beta \cos \delta - \cos A \sin \beta \sin \delta)$$

β (Flight path angle)

$$\frac{\partial x}{\partial \beta} \sim \frac{\partial y}{\partial \beta} = \frac{\partial z}{\partial \lambda} = 0$$

$$\frac{\delta \dot{x}}{\delta \dot{\beta}} = -v \left[(\sin \beta \cos \delta + \cos A \cos \beta \sin \delta) \cos \alpha + \sin A \cos \beta \sin \alpha \right]$$

$$\frac{\partial \dot{y}}{\partial \beta} = -v \left[(\sin \beta \cos \delta + \cos A \cos \beta \sin \delta) \sin \alpha \right]$$
$$-\sin A \cos \beta \cos \alpha$$

$$\frac{\partial \dot{z}}{\partial \beta} = v (\cos A \cos \beta \cos \delta - \sin \beta \sin \delta)$$

A (Azimuth)

$$\frac{\partial \mathbf{x}}{\partial \mathbf{A}} = \frac{\partial \mathbf{y}}{\partial \mathbf{A}} = \frac{\partial \mathbf{z}}{\partial \mathbf{A}} = 0$$

$$\frac{\partial \dot{x}}{\partial A} = v \left(\sin A \sin \delta \cos \alpha - \cos A \sin \alpha \right) \sin \beta$$

$$\frac{\partial \dot{y}}{\partial A} = v (\sin A \sin \delta \sin \alpha + \cos A \cos \alpha) \sin \beta$$

$$\frac{\partial \dot{z}}{\partial A} = -v \left(\sin A \cos \delta \sin \beta \right)$$

r (Magnitude of radial vector)

$$\frac{\partial x}{\partial r} = \frac{x}{r}$$

$$\frac{\partial y}{\partial r} = \frac{y}{r}$$

$$\frac{\partial z}{\partial r} = \frac{z}{r}$$

$$\frac{\partial \dot{x}}{\partial r} = \frac{\partial \dot{y}}{\partial r} = \frac{\partial \dot{z}}{\partial r} = 0$$

y (Velocity)

$$\frac{\partial \mathbf{x}}{\partial \mathbf{v}} = \frac{\partial \mathbf{y}}{\partial \mathbf{v}} = \frac{\partial \mathbf{z}}{\partial \mathbf{v}} = 0$$

$$\frac{\partial \dot{\mathbf{x}}}{\partial \mathbf{v}} = \frac{\dot{\mathbf{x}}}{\mathbf{v}}$$

$$\frac{\partial \dot{y}}{\partial v} = \frac{\dot{y}}{v}$$

$$\frac{\partial \dot{z}}{\partial y} = \frac{\dot{z}}{y}$$

3.6.2.2, 3 Elliptic Orbital Elements

The equations for the partial derivatives of position and velocity components with respect to the elliptic orbital elements are used both to compute initial conditions at time to for the variational equations for the elliptic-element parameters and to estimate analytically the trajectory partial derivatives.

a (Semi-major axis)

$$X_a = \frac{1}{a}(X - \frac{3M}{2n} \dot{X})$$

$$\dot{x}_{a} = \frac{1}{a}(\dot{x} - \frac{3M}{2n}\ddot{x} - \frac{3}{2}\dot{x})$$

$$\ddot{X} = -\frac{\mu X}{r^3}$$

e (Eccentricity)

$$X_e = -\left[a + \frac{y_\omega^2}{r(1 - e^2)}\right]P + \frac{x_\omega y_\omega}{r(1 - e^2)}Q$$

$$\dot{X}_{e} = -\frac{1}{r(1-e^{2})^{1/2}} \left[\frac{y_{\omega}}{(1-e^{2})^{1/2}} \dot{y}_{\omega} + n \left(\frac{a}{r}\right)^{2} x_{\omega} y_{\omega} \right] P$$

$$+ \frac{1}{r(1-e^{2})^{1/2}} \left[\frac{y_{\omega}}{(1-e^{2})^{1/2}} \dot{x}_{\omega} + n \left(\frac{a}{r}\right)^{2} x_{\omega}^{2} \right] Q$$

i (Inclination)

$$X_i = \frac{z}{(P_z^2 + Q_z^2)^{1/2}} W$$

$$\dot{X}_{i} = \frac{\dot{z}}{(P_{z}^{2} + Q_{z}^{2})^{1/2}} W$$

where

$$W = P \times Q$$

 Ω (Langitude of ascending node)

(Initial conditions are not required for this parameter due to the fact that an analytic solution of the variational equation for Ω is employed.)

ω (Argument of perigee)

$$X_{\omega} = -y_{\omega}P + x_{\omega}Q$$

$$\dot{\mathbf{X}}_{\omega} = -\dot{\mathbf{y}}_{\omega} \mathbf{P} + \dot{\mathbf{x}}_{\omega} \mathbf{Q}$$

τ (Time of perigee passage)

$$X_{\tau} = -\dot{X}$$

$$\dot{X}_{\tau} = \frac{\mu X}{r^3}$$

Initial conditions for the variational equation for epoch time are $X_{t_0}(t_0) = -X(t_0)$ and $X_{t_0}(t_0) = -X(t_0)$.

The following "delayed initial conditions", corresponding to the time of a kick, must be applied in the applicable variational equations for the the partial derivatives of trajectory position and velocity with respect to kick parameters.

K (Kick magnitude)

$$X_K = 0$$

$$X_{K} = \sin \theta_{p} X_{y} + \cos \theta_{p} \cos \theta_{y} X_{r} + \cos \theta_{p} \sin \theta_{y} X_{p}$$

θ_p (Pitch deflection).

$$X_{\theta_{D}} = 0$$

$$\dot{X}_{\theta_{p}} = K(\cos \theta_{p} X_{y} - \sin \theta_{p} \cos \theta_{y} X_{r} - \sin \theta_{p} \sin \theta_{y} X_{p})$$

 θ_{v} (Yaw deflection)

$$x^{\theta^{\Lambda}} = 0$$

$$\dot{\mathbf{X}}_{\theta_{\mathbf{y}}} = \mathbf{K}(-\cos\theta_{\mathbf{p}}\sin\theta_{\mathbf{y}}\mathbf{X}_{\tau} + \cos\theta_{\mathbf{p}}\cos\theta_{\mathbf{y}}\mathbf{X}_{\mathbf{p}})$$

3.6.2.3 Differential Equation Parameter Non-homogeneous Terms

The non-homogeneous terms $\frac{\partial F}{\partial \beta}$ for the differential-equation parameter variational equations are:

CDA/W (Drag coefficient)

$$\frac{\partial \mathbf{F}}{\partial \left(\frac{\mathbf{C}_{\mathbf{D}}^{\mathbf{A}}}{\mathbf{W}}\right)} = \mathbf{F}_{3} \left(\frac{\mathbf{C}_{\mathbf{D}}^{\mathbf{A}}}{\mathbf{W}}\right)^{-1}$$

μ (Gravitational constant)

$$\frac{\partial \ddot{X}}{\partial \mu} = \frac{F_1 + F_2}{\mu} - \frac{X}{3}$$

 J_{i} , J_{ik} , λ_{ik} (Oblateness parameters)

Denoting the perturbative force components in the Up/East/North system (see Section 3.6.1) by

$$g_U = -\frac{\mu}{r^2} \left[\sum_{n=2}^{n_1} A_n + \sum_{n=2}^{n_2} \sum_{m=1}^{n} B_{nm} \cos m (\lambda - \lambda_{nm}) \right]$$

$$g_{E} = -\frac{\mu}{r^{2}} \left[\sum_{n=2}^{n} \sum_{m=1}^{n} \left[C_{nm} \sin m \left(\lambda - \lambda_{nm} \right) \right] \right]$$

 $g_N = -\frac{\mu}{r^2} \left[\sum_{n=2}^{n_1} D_n + \sum_{n=2}^{n_2} \sum_{m=1}^{n} E_{nm} \cos m (\lambda - \lambda_{nm}) \right]$

then

$$\frac{\partial g_{U}}{\partial J_{i}} = \frac{-\mu}{r^{2}} \frac{A_{i}}{J_{i}}$$

$$\frac{\partial g_{E}}{\partial J_{i}} = 0$$

$$\frac{\partial g_{N}}{\partial J_{i}} = \frac{\mu}{r^{2}} \frac{D_{i}}{J_{i}}$$

$$\frac{\partial g_{U}}{\partial J_{ik}} = \frac{\gamma_{ik}}{r^{2}} \frac{B_{ik} \cos k (\lambda - \lambda_{ik})}{J_{ik}}$$

$$\frac{\partial g_{E}}{\partial J_{ik}} = \frac{-\mu}{r^{2}} \frac{C_{ik} \sin k (\lambda - \lambda_{ik})}{J_{ik}}$$

$$\frac{\partial g_N}{\partial J_{ik}} = \frac{-\mu}{r^2} \frac{E_{ik} \cos k (\lambda - \lambda_{ik})}{J_{ik}}$$

$$\frac{\partial g_U}{\partial \lambda_{ik}} = \frac{-\mu}{z^2} kB_{ik} \sin k (\lambda - \lambda_{ik})$$

$$\frac{\partial g_E}{\partial \lambda_{ik}} = \frac{\partial \mu}{\partial x_i} k C_{ik} \cos k (\lambda - \lambda_{ik})$$

$$\frac{\partial g_{N}}{\partial \lambda_{ik}} = \frac{-\mu}{r^{2}} kE_{ik} \sin k (\lambda - \lambda_{ik})$$

The component terms are then rotated to the ECI system by the matrix given in Section 3. 6. 1.

T₁, T₂ (Thrust parameters)

$$\frac{\partial \mathbf{F}}{\partial \mathbf{T}_1} = e^{-\mathbf{T}_2(\mathbf{t} - \mathbf{t}_s)} \frac{\dot{\mathbf{X}}}{|\dot{\mathbf{X}}|} = \frac{\mathbf{F}_4}{\mathbf{T}_1}$$

$$\frac{\partial F}{\partial T_2} = -T_1(t - t_s) e^{-T_2(t - t_s)} = -(t - t_s) F_4$$

 ω_{A} (Atmosphere rotation rate)

$$\frac{\partial \mathbf{F}}{\partial \omega_{\mathbf{A}}} = -\frac{1}{2} \rho \frac{C_{\mathbf{D}}^{\mathbf{A}}}{W} V_{\mathbf{A}} \left[(\dot{\mathbf{E}}\mathbf{X}) + \frac{\dot{\mathbf{X}}_{\mathbf{A}}^{\mathbf{T}} (\dot{\mathbf{E}}\mathbf{X})}{V_{\mathbf{A}}^{2}} \dot{\mathbf{X}}_{\mathbf{A}} \right]$$

where

$$EX = \begin{pmatrix} y \\ -x \\ 0 \end{pmatrix}$$

3.6.3 Integration Methods

Numerical integration for TRACE-D program purposes, including integration of the differential equations itemized in Sections 3.6.1 and 3.6.2, is accomplished by means of the DE6F subroutine, which is based on the widely known Gauss-Jackson method. This subroutine incorporates variable-step predictor-corrector automatic local truncation-error control as well as double-precision accumulation features, and uses the Runge-Kutta method for obtaining starting values (Ref. 13).

The Gauss-Jackson method, which utilizes 6th differences, has proved to be remarkably effective in the integration of most satellite trajectories, and in some restricted but well-controlled tests involving application of the method to the equations of motion has produced results comparing favorably in both speed and accuracy with more sophisticated special perturbation methods (Ref. 14). A recent simple refinement, wherein rounded values of the dependent variables instead of only their most significant portions are used in calculation of the derivatives, has nearly halved the integration errors previously accumulated in 15 revolutions.

3.6.4 Interpolation

Whenever the position, velocity, and related partial derivatives of a vehicle are required, the applicable quantities X, X, X and X are obtained by Hermite interpolation (Ref. 15) between integration steps. This technique permits an uninterrupted numerical integration, is comparatively rapid, and, as used in this connection, is quite accurate. In particular, function values and their first and second derivatives at two adjacent integration steps are retained to permit 5th and 3rd degree interpolations for position and velocity, respectively.

3.6.5 Trajectory Output

The position and velocity vectors X and X of a vehicle constitute the basis of the trajectory output in that evaluations of these quantities as obtained by interpolation from the results of the numerical integration permit computation of both the spherical coordinates a, δ , β , A, r, v of the vehicle (see Section 3.2.2) and of its geodetic latitude Φ^* , longitude f, and height h. Expressions for the latter three quantities may be written

$$\Phi^* = \tan^{-1} \left[\frac{z}{(x^2 + y^2)^{1/2} (1 - \epsilon)^2} \right]$$

$$\ell = \alpha - \alpha_g - \omega_e (t - t_g)$$

$$h = r - \frac{a_e (1 - \epsilon)}{\left[1 - (2\epsilon - \epsilon^2) \frac{x^2 + y^2}{2} \right]^{1/2}}$$

Also, sub-vehicle latitude $\Phi_{_{\mathbf{V}}}$ is given by

$$\Phi_{v} = \delta + \sin^{-1} \left[\frac{\epsilon \sin 2\delta}{r} + \left(\frac{\epsilon^{2}}{4r} \right) \left(\frac{4}{r} - 1 \right) \sin 4\delta \right]$$

Optionally, the elements of the osculating ellipse also are output. Included among these are the elements a, e, i, Ω , ω , and τ (see Section 3.2.4) and also the following: (Ref. 16)

M (Mean anomaly, deg)

$$M = E - e \sin E$$

where

$$E = \cos^{-1}\left(\frac{1 - \frac{r}{a}}{e}\right)$$

f (True anomaly, deg)

$$f = 2 \tan^{-1} \left[\left(\frac{1+e}{1-e} \right)^{1/2} \tan \frac{E}{2} \right]$$

 Ω (Regression of the node, deg/day)

$$\hat{\Omega} = \frac{3J_2 a_e^2 \sqrt{\mu}}{2a^{3/2} p^2} \cdot \cos i$$

ω (Advance of line of apsides, deg/day)

$$\dot{\omega} = \frac{3J_2 a_e^2 \sqrt{\mu}}{a^{3/2} p^2} \left(1 - \frac{5}{4} \sin^2 i\right)$$

where

1

$$p = \frac{r^2 v^2 \sin^2 \beta}{\mu}$$

r_a (Radius of apogee, n mi)

$$r_a = \pi(1 + e)$$

rp (Radius of perigee, n mi)

$$r_p = a(1 - e)$$

PK (Keplerian period. min)

$$P_{K} = \frac{2\pi a^{3/2}}{\sqrt{\mu}}$$

PA (Anomalistic period, min)

$$P_{A} = P_{K} \left[1 - \frac{\frac{3}{2}J_{2}a_{e}^{2}}{a^{2}} \left(\frac{a}{r} \right)^{3} (1 - 3 \sin^{2} \delta) \right]$$

where

 δ = declination

P_N (Nodal period, min)

$$P_{N} = P_{A} - P_{K} \left[\frac{3J_{2}a_{e}^{2}(1 - 5/4 \sin^{2}i)}{\sqrt{p} a^{2}(1 + e \cos \omega)^{2}} \right]$$

3.6.6 Initial Orbit Condition Derivation (Gaussian Method)

On option, initial conditions of an orbit may be calculated from two sets of range/azimuth/elevation (RAE) observations in accordance with the following adapted procedure (Ref. 17). Letting

 X_1 = Cartesian vector associated with first RAE observation point

X₂ = Cartesian vector associated with second RAE observation point

$$W = \frac{X_1 \times X_2}{|X_1 \times X_2|} = \text{unit vector perpendicular to observation plane}$$

$$U_1 = \frac{X_1}{|X_1|} = \text{unit vector parallel to } X_1$$

 $V_1 = W \times U_1 = unit vector perpendicular to U_1 and W$

values are computed for

$$f = \frac{1}{2} (v_2 - v_1) = \frac{1}{2} \arccos \frac{X_1 \cdot X_2}{|X_1| |X_2|}$$

$$g_1 = \frac{\sqrt{2\mu} (t_2 - t_1)}{[2(|X_1| |X_2|)^{1/2} \cos f]^{3/2}}$$

$$g_2 = \frac{|x_1| + |x_2|}{2(|x_1| |x_2|)^{1/2} \cos f}$$

Setting $g^{(0)} = f$, g may then be found by means of the iteration

$$g_3 = \sin g^{(i)}$$
 $g_4 = \cos g^{(i)}$
 $g_5 = \sin^3 g^{(i)}$
 $g_6 = \sin^4 g^{(i)}$
 $g_7 = g_2 - g_4$
 $g_8 = \sqrt{g_7}$
 $g_9 = (g_7)^2$

Also,

$$\Delta g = \frac{\frac{1}{g_7} \left(1 - \frac{g_1}{g_8}\right) + \frac{1}{g_5} (g^{(i)} - g_3 g_4)}{\frac{g_3}{g_9} \left(\frac{3g_1}{2g_8} - 1\right) - \frac{1}{g_6} [g_5 + 3(g^{(i)}g_4 - g_3)]}$$

and

$$g^{(i+1)} = g^{(i)} - \Delta g$$

Iteration is continued until $|\Delta g| \le \epsilon$.

The Keplerian elements are then given by the relationships

$$a = \frac{|X_1| + |X_2| - 2\sqrt{|X_1|} |X_2| \cos g \cos f}{2 \sin^2 g}$$

$$e \cos E_1 = 1 - \frac{|X_1|}{a}$$

$$e \cos E_2 = 1 - \frac{|X_2|}{a}$$

e
$$\sin E_1 = \frac{\cos 2g}{\sin 2g}$$
 [e $\cos E_1$ - (cos 2g)(e $\cos E_2$)]

$$E_1 = \tan^{-1} \frac{e \sin E_1}{e \cos E_1} \qquad (0 \le E_1 < 2\pi)$$

$$e = [(e \cos E_1)^2 + (e \sin E_1)^2]^{1/2}$$

$$T = t_1 - (E_1 - e \sin E_1) - \frac{a^{3/2}}{\sqrt{\mu}}$$
 (a > 0)

$$i = cos^{-1}W_z$$

$$(0 \leq i < \pi)$$

$$\Omega = \tan^{-1} \frac{W_x}{-W_y}$$

$$(0 \leq \Omega < 2\pi)$$

$$\cos v_1 = \frac{\cos E_1 - e}{1 - e \cos E_1}$$

$$\sin v_1 = \frac{\sqrt{1 - e^2} \sin E_1}{1 - e \cos E_1}$$

$$P = U_1 \cos v_1 - V_1 \sin v_1$$

$$Q = U_1 \sin v_1 + V_1 \cos v_1$$

$$\omega = \tan^{-1} \frac{P_z}{Q_z} \qquad (0 \le \omega < 2\pi)$$

3.7 <u>DIFFERENTIAL CORRECTION AND</u> ASSOCIATED COMPUTATIONS

The basic problem of differential correction is determination of the change or correction of a given set of parameters that is necessary to permit some specified result to be achieved. For the present case the goal is to minimize the weighted sum of the squares of the differences between the observed radar data and the corresponding quantities computed from the observational model, which of course includes the trajectory and observation parameters to be corrected.

In this discussion, matrices and vectors in general are denoted by Roman capitals and their components by corresponding lower-case letters with subscripts where appropriate. The following notation and nomenclature als are applicable:

n = number of observed quantities

m = number of parameters

k = number of effective parameters (m minus the number of constraint equations)

o; = ith observation

σ = radar sigma (multiplicative weighting factor) to be applied to data-type j from station s

 β_{sj} = radar bias (additive weighting factor) to be applied to data-type j from station s

Omc = vector of weighted residuals (differences between observed and computed radar quantities)

P = vector of parameters

 ΔP = correction vector for P

G = diagonal matrix representing bounds on solution ΔP

A = matrix of partial derivatives:

$$a_{ij} = \frac{\partial o_i}{\partial P_j}$$
; $i = 1, 2, ..., n$; $j = 1, 2, ..., m$

 $A^{T} = A \text{ transpose}$

W = n × n weighting matrix, diagonal except for 3 x 3 matrices on the diagonal, where the rows correspond to correlated observations. The complete matrix is never formed but is input in inverse form, where observation sigmas are the square roots of the reciprocal diagonal elements and the input observation covariance matrices are the inverse of the 3 x 3 sub-matrices.

B = constraint matrix

3.7.1 Sigmas, Covariances, and Biases

Usually some information is available concerning the characteristics of the observations in terms of random noise, biases, and, in specific cases, correlations. Such information may be included in the least-squares process in the following manner.

If it is known or suspected that a certain set of data exhibits a constant bias in either data or time, the β_{sj} are applied to the appropriate components of O_{mc} before weighting. Biases may be included as parameters to be differentially corrected. It so, the derived value is automatically applied on each subsequent iteration. If a constant bias is to be applied, the parameter may be selected, the desired value entered as the estimate, and the bound set to zero.

The most common form of weighting involves use of a priori standard deviations; in general, one value for each type of data from each station. Under this option the elements of A and O are simply divided by the appropriate sigma. In the case of correlated observations (at most three observations of the same set taken at the same time), the weighting is accomplished by means of the inverse of an input 3 × 3 covariance matrix.

3.7.2 The Unconstrained Normal

In its simplest form, differential correction involves the solution of the linearized problem $(A^TWA)\Delta P = A^TWO_{mc}$. A^TWA is the normal matrix. In TRACE-D procedure, if $A^TA = 0$ initially, the normal is formed by accumulating $A^TWA = A^TWA + a^Twa$ and $A^TWO_{mc} = A^TWO_{mc} + a^TwO_{mc}$, where a represents one row of the A matrix and the Wisthe a priori weighting sigma in the case of an uncorrelated observation. Where covariances among observations are encountered, a is a 3×3 matrix formed with the three appropriate rows of A, and w is the inverse of the appropriate input 3×3 covariance matrix.

The weights and biases as defined in Section 3.7.1 and introduced into the notation of Section 3.7.2 also are implicit in connection with all operations with A and O_{mc} in Sections 3.7.3 through 3.7.7.

3.7.3 The Contrained Normal

It is often desirable to impose linear constraints of the form $\Delta P = B(AP') + C$, where P' is some subset of P and C is a vector of constants, on the solution. For example, if it is assumed that the parameters to be solved for are $F = S_1$ (latitude), $F_2 = S_1$ (longitude), $F_3 = S_2$ (latitude), $F_4 = S_2$ (longitude), and $F_5 = S_2$ (range bias), where F_1 , F_2 are two radar stations, the requirement that the positions of the stations relative to each other remain fixed is equivalent to the matrix equation

$$\begin{bmatrix} \Delta P_1 \\ \Delta P_2 \\ \Delta P_3 \\ \Delta P_4 \\ \Delta P_5 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \Delta P_1 \\ \Delta P_2 \\ \Delta P_5 \end{bmatrix} + [0]$$

$$\Delta P \qquad B \qquad \Delta P \qquad C'$$

The problem then effectively becomes one of solving the reduced system $(AB)^T(AB)(\Delta P') = (AB)^TO_{mc}$. Thus if a_i is a row of A and if $A^TA \equiv 0$ initially, the constrained normal is formed by accumulating $A^TA = A^TA + (a_iB)^T(a_iB)$.

3.7.4 Bounds

Given a set of bounds g_i , the corrections Δp_i to the components of P are either less in absolute value than g_i if $g_i > 0$, zero if $g_i = 0$, or unrestricted if $g_i < 0$ for $i = 1, 2, \ldots$, m In cases where constraints are to be applied, the bounds are adjusted accordingly. For example, letting

$$h_j = \sum_{i=1}^m \frac{(\text{sign } g_i)}{(g_i)^2} b_{ij}$$
 (j = 1, 2, ..., k)

k new bounds, g_{j}^{\prime} , are formulated by the program where

$$g'_j = \frac{1}{h_j}$$
 if $h_j > 0$

$$g'_j = 0 \text{ if } h_j = 0$$

$$g_{j}' < 0 \text{ if } h_{j} < 0$$

It should be noted that $g'_j = g_i$ for a variable not appearing in any constraint equation and also that specifying bounds equal in magnitude but opposite in sign for two parameters to be corrected by equal increments will result in a zero correction to both.

3.7.5 Solution of the Normal Equations

With the $m \times m$ matrix A^TA , the vector A^TO_{mc} , and a set of bounds g_i given, and assuming m parameters p_1 , p_2 , and p_3 to be corrected, the problem

is to minimize $||A\Delta P - O_{mc}||^2$ under the side condition that $\sum (\Delta p_i/g_i)^2 \le 1$, with the sum taken over all i for which $g_i > 0$.

It may be assumed without loss of generality that $g_i \neq 0$, inasmuch as $g_i = 0$ implies that Δp_i . 0 and also that the i^{th} row and column of the normal matrix may be ignored, which simply reduces the dimension of the problem. Letting G be the diagonal matrix, such that $G_{ii} = 1/g_i$ if $g_i > 0$ and $g_{ii} = 0$ if $g_i \leq 0$, the requirement is to find such a value of z that the solution $\Delta P'(z)$ of the linear system $(A^TA + zG^2) \Delta P = A^TO_{mc}$ satisfies the given side condition. This involves the two processes of choosing the best value for z and accomplishing the actual solution of the system.

It is important to recognize that for the constrained case the only change required in the notation given in the following Sections 3.7.5.1 through 3.7.5.4 is substitution of k (the number of effective parameters) for m.

3.7.5.1 Determination of z

The first step in the determination of z is to obtain $\Delta P'(0)$, or the solution to $(A^TA)\Delta P = A^TO_{mc}$. If then $\Sigma(\Delta p_i/g_i)^2 \le 1 + \epsilon_1$, the problem is solved. If not, $y(z) = \Sigma(\Delta p_i(z)/g_i)^2 - 1$ must be defined. Noting that $y(0) > \epsilon_1$, computation of y(h), y(10h), and y(100h), where h is some preset constant, is carried out until either a value of z = kh is found such that $-\epsilon_2 \le y(z) \le \epsilon_1$, in which case $\Delta P(z)$ is the solution, or two values of z are found such that $y(z_1) > \epsilon_1$ and $y(z_2) < -\epsilon_2$, whereby the required value of z is bracketed. In the latter case a value z_3 is chosen between z_1 and z_2 in accordance with $z = 0.8z_1 + 0.2z_2$, wherein the coefficients 0.8 and 0.2 are fairly arbitrary and z_1 and z_2 may have been interchanged to bring z_3 closest to the value of z giving the smallest y(z).

If $-\epsilon_2 \le y(z_3) \le \epsilon_1$, $\Delta P'(z_3)$ then is the solution. Otherwise, inverse quadratic interpolation is used to obtain a new guess, z_4 . Similarly, if $-\epsilon_2 \le y(z_4) \le \epsilon_1$, $\Delta P'(z_4)$ is the solution, but if not, the two values of z from the set $\{z_1, z_2, z_3, z_4\}$ which bracket the solution most tightly are chosen and the process is

repeated. If more than twenty solutions of the linear system are required, the process is abandoned.

In the foregoing, ϵ_1 and ϵ_2 are suitably small positive constants.

3.7.5.2 Solution of the Linear System - Matrix Operations.

In the expression $(A^TA + zG^2)\Delta P = A^TO_{mc}$, which defines the linear system to be solved, let the term $A^TA + zG^2 = C$.

It is then desired to find a matrix S such that $SCS^T = D$ where S is lower triangular with (-1) on the diagonal and D = diag (d_1, \ldots, d_n) .

$$C' = \begin{pmatrix} C & d \\ d^T & a \end{pmatrix}$$

Since S' must be lower triangular with (-1) on the diagonal and of the same order as C', it must be of the form

$$S' = \begin{pmatrix} S & 0 \\ W^T & -1 \end{pmatrix}$$

and the requirement $S'S'^T = D'$ is equivalent to solving for a vector W and a scalar b such that

$$\begin{pmatrix} S & 0 \\ W^{T} & -1 \end{pmatrix} \quad \begin{pmatrix} C & d \\ d^{T} & \alpha \end{pmatrix} \quad \begin{pmatrix} S^{T} & W \\ 0 & -1 \end{pmatrix} = \begin{pmatrix} D & 0 \\ 0 & b \end{pmatrix} = E'$$

It is easily verified that $W = S^T D^{-1} S d$ and $b = a - W^T d$ satisfy the foregoing equation.

The computations are carried out in accordance with the above outline, starting with the 2×2 matrix C_{ij} , i = 1, 2, ; j = 1, 2 and continuing until the decomposition

$$\begin{pmatrix} S & 0 \\ W^{T} - 1 \end{pmatrix} \begin{pmatrix} A^{T}A + zG^{2} & A^{T}O_{mc} \\ O_{mc}^{T}A & O_{mc}^{T}O_{mc} \end{pmatrix} \begin{pmatrix} S^{T} & W \\ 0 & -1 \end{pmatrix} = \begin{pmatrix} D & 0 \\ 0 & \alpha \end{pmatrix}$$

has been found. Completion of the multiplication indicated on the left side of this equation shows that the m-dimensional vector W is the solution to the linear system.

3.7.5.3 Residuals Prediction

The predicted RMS of the residuals

$$\|O_{mc}^{p}\| = \|A\Delta P - O_{mc}\|$$

is computed from the augmented normal matrix

$$\|A\Delta P - O_{mc}\|^2 = [(A^T A\Delta P) \cdot \Delta P] - 2[(A^T O_{mc}) \cdot \Delta P] + O_{mc}^T O_{mc}$$

3.7.5.4 The Inverse Normal

$$(A^TA)^{-1} = S^TD^{-1}S$$

wherein S and D are as defined in paragraph 3.7.5.2.

3.7.6 Convergence of the Differential Correction Process

The $\|O_{mc}\|$ is a measure of how well an orbit computed on the basis of a given set of parameters P fits corresponding observed data. $\|O_{mc}^P\|$ computed in accordance with paragraph 3.7.5.3 is an approximation to $\|O_{mc}\|$ which would be obtained by replacing P by P + Δ P. This approximation would be exact if the least squares problem were linear, which is equivalent to P being in a sufficiently small neighborhood of the minimum point.

Convergence therefore is reached when further corrections to P would produce no significant decrease in $\|O_{mc}\|$, or no over-all improvement of the residuals. The criterion is either

$$\frac{\|\mathbf{S}_{\mathrm{mc}}\| - \|\mathbf{O}_{\mathrm{mc}}^{\mathrm{p}}\|}{\|\mathbf{O}_{\mathrm{mc}}\|} \leq \epsilon_{\mathrm{I}} \ .$$

or

2

$$\|O_{mc}\| \cdot n^{-1/2} \le \epsilon_{II}$$

where

n = number of observations $\epsilon_{I}, \epsilon_{II} = input quantities$

If $\|O_{mc}\|$ is decreasing with each iteration, the process is converging and the bounds are expanded at each step by a multiplicative factor β_1 to permit faster convergence. On the other hand, if $\|O_{mc}\|$ is increasing from one iteration to the next, the process is diverging and the last corrections are presumed to have altered P too drastically. In this situation the previous values of P and the corresponding normal matrix are retrieved and resolved with tighter bounds g_i' such that the weighted length $\|G' \cdot \Delta P''\|$ of the solution is reduced to β_2 times its previous value. β_1 and β_2 are input constants.

3.7.7 The Correlation Matrix

It has been shown in Section 2 that if the mathematical model is exact, if the observations are linear functions of the parameters, if the observation errors have mean zero and are independent, and if the input values of σ_{sj} are correct, the inverse of the normal matrix then is the variance-covariance matrix of the parameters that arises because of the random errors in the observations. If the elements of this matrix are given as c_{ij} , the corresponding correlation matrix has elements

$$c'_{ij} = \frac{c_{ij}}{\sqrt{c_{ii}c_{jj}}}$$
 (i, j, = 1, 2, ..., m)

If all the assumptions noted above are true except that all σ_{sj}^2 values are in error by a constant multiplicative factor, then the values in the variance-covariance matrix will also all be in error by the same factor.

3.7.8 The Scatter Coefficient

The scatter coefficient (Ref. 18) may be expressed by

$$S = \left[\det |c_{ij}|\right]^{1/2} = \left[\frac{\det |A^{T}A^{-1}|}{\Pi\sigma_{i}^{2}}\right]^{1/2}$$

where

c_{ij} = correlation matrix for the least squares parameters

[A^TA]⁻¹ = usual normal matrix inverse or variance-covariance matrix

 σ_i^2 = diagonal elements of $[A^TA]^{-1}$

3.8 OTHER TRACKING CALCULATIONS

3.8.1 Proximity Testing

Input quantities are denoted by the set

$$\{\hat{\varphi}_{i}^{*}, \lambda_{i}, h_{i}, R_{e_{i}}^{*}\}$$

where

φ* = geodetic latitude

 $\lambda = east longitude$

h = altitude (height)

R* = range to be tested against (critical range)

 $i = 1, 2, 3, = number of site designated by <math>\Phi^*, \lambda, h$

3.8.1.1 Input Conversion (INCNI)

Input units must first be converted to working units, wherein degrees and feet/nautical miles are expressed in terms of radians and earth radii, respectively. The input set thus is converted to a set of working parameters denoted by

$$\{X_i^{}, \Psi_i^{}, \lambda_i^{}, R_{o_i}^*\}$$

where X_i , Ψ_i are site (i) coordinates. X_i , Ψ_i are then computed from the relations

$$X_{i} = \left\{ \frac{a_{e}}{\left[\left(1 - \epsilon^{2}\right) \sin^{2} \Phi_{i}^{*}\right]^{1/2}} + h \right\} \cos \Phi_{i}^{*}$$

and

$$\Psi_{i} = \left\{ \frac{a_{e}(1 - \epsilon^{2})}{\left[(1 - \epsilon^{2}) \sin^{2} \phi_{i}^{*} \right]^{1/2}} + h_{i} \right\} \sin \phi_{i}^{*}$$

where

a_e = semi-major axis of the earth

€ = ellipticiy of reference ellipsoid

3.8.1.2 Proximity Test

After the inertial-coordinate components of a site (i) position vector at time t have been computed, the position vector \underline{r}_{s_i} is determined by

$$\underline{\underline{r}}_{s_{i}} = \begin{cases} x_{s_{i}}^{(t)} = \dot{X_{i}} \cos \alpha \\ y_{s_{i}}^{(t)} = \dot{X_{i}} \sin \alpha \\ y_{s_{i}}^{(t)} = \dot{Y_{i}} \sin \alpha \end{cases}$$

where :

$$a_{s_i} = a_g + \omega_e(t - t_o) + \lambda_i$$

a_s = right ascension of site (i) at time t

ag = right ascension of Greenwich at midnight of epoch

 ω_{e} = rotational rate of the earth

t_o = epoch time in minutes

 λ_{i} = east longitude of site (i).

The proximity indicator is printed if the satellite of interest is within the sphere of influence at a proximity-testing time (integration-step time). It is therefore apparent that a necessary and sufficient condition to print this indicator is

$$|R_i^*| \le R_{o_i}^*$$

where

$$R_{i}^{*} = \text{magnitude of range vector from site (i) to satellite}$$

$$= \underline{r} - \underline{r}_{s_{i}}$$

$$= [x(t), y(t), z(t)] - [X_{s_{i}}(t), Y_{s_{i}}(t), Z_{s_{i}}(t)]$$

$$R_{o_{i}}^{*} = \text{critical range from site (i)}$$

3.8.1.3 Output Quantities

If proximity with respect to site (i) is detected at time t, the quantities listed in Table 3-1 will be printed.

Table 3-1. Computer Output Quantities for Proximity Condition

Quantity	Computer Symbol	Units
Satellite range from site (i)	R*(i)	nautical miles
Date	XX/YY/ZZ	month/day/year
Time	Т	minutes from midnight of day of epoch
Geodetic latitude	LAT(GD)	degrees
East longitude	LONG	degrees
Altitude	ALT	nautical miles
Inertial azimuth of velocity vector	AZ	degrees

3.8.2 Elevation-Angle Refraction Correction

Input elevation-angle observations are corrected for atmospheric refraction effects by

$$E' = E - \eta_{si} \cot E$$
 (E \ge 0.1 radian)

or

E' = E -
$$\frac{1}{1000}$$
 · $\frac{\eta_{si} \times 10^6}{12 + 1000E}$ + $\frac{80}{6 + 1000E}$ · (E < 0.1 radian)

where

E = input angle

 η_{si} = appropriate refractivity index from REFR table (no correction is made if η_{si} = 0)

3.8.3 Vehicle Height

The height observation and all vehicle-altitude computations are obtained from

$$h = r - \frac{a_e(1 - \epsilon)}{\left[1 - (2\epsilon - \epsilon^2)\frac{x^2 + y^2}{r^2}\right]^{1/2}}$$

3.8.4 Propagation Time Correction

A correction for propagation time may be made for the usual cases of radar observations wherein reported observation times are the times when pulses are sent or received at the station. This adjustment to the input observation time is

$$\Delta t = \frac{R_c}{c}$$

where

R_c = computed range

c = propagation speed with appropriate algebraic sign

In the case of height data,

$$\Delta t = \frac{h}{c}$$

3.9 RESIDUALS ANALYSIS

3.9.1 Orbit-Plane Residuals

The basic purpose of the residuals-analysis link that is presently available in the TRACE-D program is to permit resolution of residual vectors into the orbit-plane coordinate system. At this time, capability exists for resolving three types of residual vectors having the following related data types:

- a. $\stackrel{\wedge}{x}$, $\stackrel{\wedge}{y}$, $\stackrel{\wedge}{z}$ (rotating earth-centered)
- b. a_T , δ_T (topocentric right ascension and declination)
- c. R, A, E (range, azimuth, elevation)

The vector and matrix products necessary to obtain the desired orbit-plane resolution for the \hat{x} , \hat{y} , \hat{z} data types are

$$\hat{X}^{T} = \hat{x}, \hat{y}, \hat{z}$$

and

$$\Delta \hat{X}^{T} = \Delta \hat{x}, \Delta \hat{y}, \Delta \hat{z}$$

Resolution into the orbit-plane system may then be obtained by

$$\Delta(OP) = M^T A \Delta X$$

where

$$A = \begin{bmatrix} \cos a_g & -\sin a_g & 0 \\ \sin a_g & \cos a_g & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

(ag = right ascension of Greenwich)

$$M = \begin{bmatrix} r_{x} & t_{x} & c_{x} \\ r_{y} & t_{y} & c_{y} \\ r_{z} & t_{z} & c_{z} \end{bmatrix} \quad (\underline{r} = X/|X|; \ \underline{c} = (X \times \dot{X})/(|X \times \dot{X}|); \ \underline{t} = \underline{c} \times \underline{r})$$

In the case of the $\alpha_{\rm T},~\delta_{\rm T}$ data types, the calculated slant range R is necessary. Letting

$$S^{T} = [R, \alpha_{T}, \delta_{T}]$$

$$\Delta S^{T} = \left[\Delta R, \ \Delta \alpha_{T}, \ \Delta \delta_{T} \right]$$

wherein ΔR usually will be 0, then for resolution,

$$\Delta(OP) = M^T B \Delta S$$

where, dropping the T subscript,

$$B = \begin{bmatrix} \cos a \cos \delta & -R \sin a \cos \delta & -R \cos a \sin \delta \\ \sin a \cos \delta & R \cos a \cos \delta & -R \sin a \sin \delta \\ \sin \delta & 0 & R \cos \delta \end{bmatrix}$$

For the R, A, E data types, letting

$$U^{T} = [R, A, E]$$

$$\Delta U^{T} = [\Delta R, \Delta A, \Delta E]$$

then for resolution,

$$\Delta(OP) = M^T DEF \Delta U^T$$

where

$$F = \begin{bmatrix} \cos A \cos E & -R \sin A \cos E & -R \cos A \sin E \\ \sin A \cos E & R \cos A \cos E & -R \sin A \sin E \\ \sin E & 0 & R \cos E \end{bmatrix}$$

$$\mathbf{E} = \begin{bmatrix} 0 & \sin (\Phi^* - \phi) & \cos (\Phi^* - \phi) \\ 1 & 0 & 0 \\ 0 & \cos (\Phi^* - \phi) & -\sin (\Phi^* - \phi) \end{bmatrix}$$

 $(\Phi^* = \text{station geodetic})$ latitude, $\phi = \text{station}$ declination)

$$D = \begin{bmatrix} \cos \alpha \cos \delta & -\sin \alpha & -\cos \alpha \sin \delta \\ \sin \alpha \cos \delta & \cos \alpha & -\sin \alpha \sin \delta \\ \sin \delta & 0 & \cos \delta \end{bmatrix}$$

3.9.2 Time Residuals

The observation-time adjustment which would cause a residual to go to zero may be estimated by

$$\Delta t_{i} = \frac{\Delta R_{i}}{\dot{R}_{i}}$$

where

 ΔR_i = representation for any unweighted residual

R. = time derivative of the same observation type computed at the observation time

 $\Delta t_i = time residual$

The residuals analysis link automatically performs this computation for data types \hat{x} , \hat{y} , \hat{z} , α_T , δ_T , and R, A, E if they are entered and outputs the corresponding time residuals in units of seconds.

3.9.3 Propagation Time Correction

The propagation-time adjustment to observation times in RESIDUE is the same as in the orbit determination links (see Section 3.8.4).

3.9.4 Residual Vector Magnitude

The magnitude of the residual vector for a set of three observations is given by

$$R_T = [\xi^2 + \eta^2 + \zeta^2]^{1/2}$$

where

 ξ , η , ζ = radial, in-track, and cross-track vector components

SECTION 4

TRACE-D PROGRAM STRUCTURE

4.1 GENERAL

The TRACE-D program is written in the FORTRAN-II language, which is intended to be used with the IBM 7094 FORTRAN Monitor System. The basic TRACE-D program structure consists of a series of eleven major independent links connected by the CHAIN feature of FORTRAIN-II. Each link in turn incorporates a series of large blocks, or major subroutines, each of which makes use of many smaller subroutines. TRACE-D consequently is an extremely flexible program that not only is easily expanded and modified but also whose flow of computation is easily understood.

The single factor restricting TRACE-D use to the IBM 7094 computer unit is occasional utilization of FAP, which includes the FINP-input, ARDC-1959-atmosphere, numerical-integration, and gravity subroutines.

A general TRACE-D program flow chart is presented in Figure 4-1.

4.2 PROGRAM LINKS

4. 2. 1 CHAIN

CHAIN is the only link that must be executed regardless of the mode of TRACE-D program usage. This link reads basic data, prints a header, sets several options to their nominal values, and computes the Julian date and the orientation of the earth.

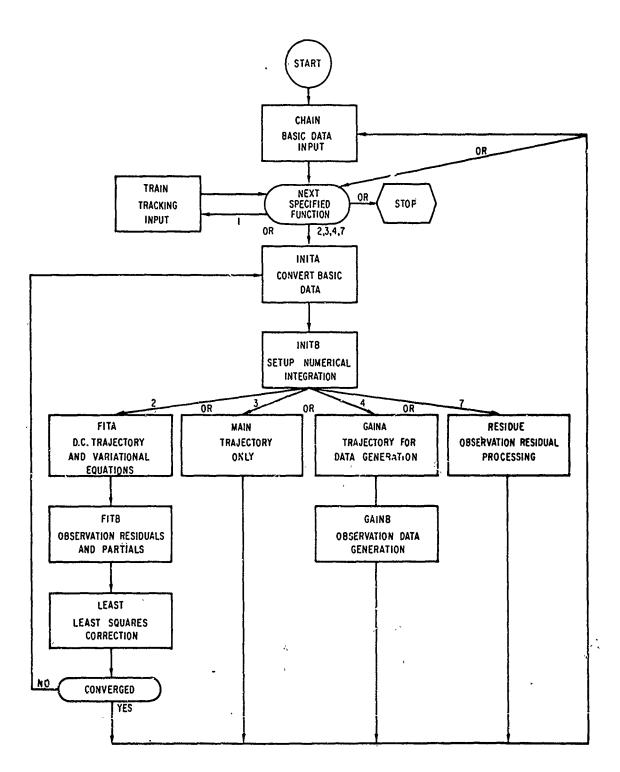


Figure 4-1. General Flow Chart for TRACE D

4.2.2 TRAIN

The TRAIN tracking input link reads radar station location and observation data, which may be on the BCD input tape produced by the IBM 1401 or on a binary tape previously written by TRAIN. The observations not only are sorted chronologically, but a compacted list of the observations is produced which eliminates storage corresponding to blanks in the information reported. In this way approximately two hundred observation times can be handled in core on a 32K machine without resorting to intermediate tapes.

The binary tape produced by TRAIN containing the sorted and compacted observation data may be used either on successive runs or for the next case of the same run. All units of this data will have been converted to an earth-radii/minutes/radians system, with observation times reduced to minutes from midnight of epoch. TRAIN also prints the tracking input and decodes and prints input concerning parameters to be solved for by differential correction.

4.2.3 INITA

The four modes of operation included in INITA are trajectory-only, orbit determination, data generation, and residuals analysis. The trajectory-only mode converts and prints the input initial conditions, sets up the print times specified by the input, and determines the parameters for which the variational equations are to be integrated. In the orbit determination mode, INITA must be entered at the beginning of each iteration. For the first iteration only, the initial conditions are converted and printed and the n_{σ} editor is cleared. For all iterations, the tapes are set to their correct positions and the low thrust is reset. In the data generation mode, the initial conditions are converted and printed. In the residuals analysis mode, the tapes to be used are set to the correct position.

4.2.4 INITB

INITB includes the four operational modes noted above for INITA -- trajectory-only, orbit determination, data generation, and residuals analysis.

In the trajectory-only mode, the numerical integration is initialized for the orbit and the variational equations. In the orbit determination mode, the numerical integration is initialized for the orbit and variational equations, certain radar station location quantities are computed, and the no editor is reset, except on the first iteration. In the data generation mode, station locations and data specifications are read and the numerical integration is initialized. In the residuals analysis mode, certain radar station location quantities are computed.

4.2.5 FITA

The function of FITA is to read the compacted data tape produced by TRAIN, perform the necessary numerical integration to obtain vehicle position and velocity at the observation times, and write a trajectory tape to be used by FITB and RESIDUE.

4.2.6 FITB

The function of FITB is to read the compacted radar data tape and the trajectory tape, compute the radar residuals and partials, and accumulate the ${\bf A}^{\rm T}{\bf A}$ to be used in LEAST.

4.2.7 LEAST

The function of LEAST is to determine and print the corrections to be made in the differential correction procedure.

4.2.8 MAIN

The function of MAIN is to integrate the orbit and variational equations for the trajectory-only option. MAIN interpolates and prints output at the times specified by the input print vector.

4.2.9 GAINA

The function of GAINA is to perform the numerical integration and to write a trajectory tape for the data generation computations that are to be accomplished in GAINB.

4,2.10 GAINB

The function of GAINB is to read the tape produced by GAINA and to compute, sort, and print the radar data observations specified.

4.2.11 RESIDUE

RESIDUE performs a variety of functions associated with error analysis of remaining residuals (i.e., residuals which remain after convergence of the least-squares fitting process). It also performs certain differencing operations which allow for comparison of ephemerides, measured observations, etc.

4.3 STORAGE MAPS

4.3.1 Tab Listings of Key Storage Area Functions

Figures 4-2 through 4-12 illustrate various TRACE-D program tab listings which describe the functions of certain key storage areas. Although these listings are of primary interest to the TRACE-D programmer, they also provide insight into the operating logic of the program and in some cases serve as a summary of input cell usage (see Appendix A for description of INTEG and C storage areas). The listings presented in Figures 4-2 through 4-12 refer to the following storage areas:

- a. NUMB
- h. TEMP (as used for integration)
- b. IFLAG
- i. TEMP (as used by Subroutine FILL in Link FITB)
- c. DRAG
- j. TUMP
- d. CNDT
- k. PUSH
- e. DPRAM

KIND

- 1. COMMON
- g. XTRA

f.

It should be noted that storage area blocks within the COMMON storage area

(Item 1.) that are needed for all links, for fit and data generation links, and for fit links only are listed respectively in Figures 4-13. In these listings the given columns represent the symbolic designation, dimension, and deci-

mal and octal origin of each of the storage area blocks noted.

UMB	NUMBER OF	
		SET I PUT
,	RADAR STATIONS	IN NAME TRAIN
2	OBSERVATION TIMES	TRAIN
	OR STATIONS REQUIRING SIGHTING EPHENERIS DATA	DUM
	OR STATIONS REQUIRING SIMULATION DATA	DUM
3	WORDS IN COMPACTED RADAR OBSERVATION LIST - TOTAL	TRAIN
4 5	WORDS OF COMPACTED RADAR OBSERVATIONS IN CORE NOW DIFFERENTIAL EQUATION PARAMETERS TO BE SOLVED FOR	TRAIN CHAIN
6	INITIAL CONDITION PARAMETERS TO BE SOLVED FOR	CHAIN
7	RADAR STATION PARAMETERS TO BE SOLVED FOR	KING
8	RADAR OBSERVATION PARAMETERS TO BE SOLVED FOR	KING
9	PROGRAM TAPE UNIT	REIN - PTAPE
10	MAXIMUM ITERATIONS ALLOWED	CHAIN- MAXET
11	TOTAL PARAMETERS (SUM OF 5.6.7 AND 8) TRAJECTORY PARAMETERS (SUM OF 5 AND 6)	TRAIN TRAIN
13	OBSERVATIONS (TOTAL NUMBER OF MEASUREMENTS)	TRAIN
14	PRESENT ITERATION	MAIN
15	BASIC TYPES OF OBSERVATIONS	CHAIN
16	SIZE OF BUFFERS IN DEAN (Q DATA) - IF = 0. SET TO 5000	DEAN
17	TOTAL RADAR PARAMETERS (SUM OF 7 AND 8)	TRAIN',
18	TAPE UNIT FOR PLANETARY COORDINATE TAPE	CHAIN- CTAPE
19	SECOND ORDER DIFFERENTIAL EQUATIONS BEING INTEGRATED	INCN
20	(3*(1+NUMB(12)*IFLAG(8))) POSSIBLE KINDS OF RADAR PARAMETERS	CHAIN
LU	(LAT+ LONG+ HEIGHT+, AND BIASES)	CUMIN
21	WORDS IN CORE FOR SIGHTING EPHEMERIS BUCKET	CHAIN
22	POSSIBLE KINDS OF SIGHTING DATA	CHAIN
23	DATA NOISE CONTROL (ZERO FOR NO NOISE, NON-ZERO STARTS	CHAIN- NOISE
	RANDOM NUMBER GENERATOR FOR DATA NOISE)	
24	POSITION IN ITIN LIST OF FUNCTION BEING EXECUTED	ITIĄ
25	EFFECTIVE PARAMETERS BEING SOLVED FOR	CHAIN- KNST
	(NUMB(11)-(NO+OF CONSTRAINTS))	
26	TAPE UNIT FOR GENERATING BCD STATION AND OBSERVATION TAPE (IF ZERO, NO TAPE GENERATED)	CHAIN- ETAPE
27	FLOCKS OF DATA	TRAIN
28	TAPE UNIT FOR ECLIPSE COORD TAPE	CHAIN
29	(NOT USED)	C.I.I.Z.I.
30	ELEMENTS IN ATA	MIAR
31	TAPE UNIT FOR NOMINAL TRAJ. FOR DIFFERENCING RUN	INPAL- NTAPE
	(LOGICAL NO.) MUST BE ON CHANNEL B. IF NOT INPUT.	•
	(LOGICAL NO.) MUST BE ON CHANNEL B. IF NOT INPUT. SET = 15 IN SUBROUTIN INPAL WHEN IFLAG(15) NOT = 0.	
32	TAPE UNIT FOR DIFFERENCED TRAJ. FOR DIFFERENCING RUN	INPAL- DTAPE
	(LOGICAL NO.) MUST BE ON CHANNEL A FOR AUTOMATIC	
33	PLOTTING. IF NOT INPUT, SET =14, WHEN IFLAG(15) NON-ZERO MAXIMUM NUMBER OF 2ND DIFFERENCE EDITOR ITERATIONS) .
34	NUMBER OF 4 COLUMN PARAMETERS	
35	NO. OF PERMANENT STATIONS - INPUT POSITIVE IF VARIABLE	
,,	STATIONS ARE USED. INPUT NEGATIVE IF ALL STATIONS	
	ARE VARIABLE STATIONS	
36	MULTIPLE SATELLITE INDICATOR	TRAIN.
		INITA:FITA
37	(USED INTERNALLY)	
38	RESIDUALS ANALYSIS INTERMEDIATE TAPE (LOGICAL NUMBER) -	
10	MUST BE ON CHANNEL B.	
39	RESIDUALS ANALYSIS DATA TAPE (LOGICAL NUMBER) - MUST BE ON CHANNEL A.	
4 0	(USED INTERNALLY)	
41	ZERO, INDICATES DATA TYPE 7 HAS R-DOT RADAR DATA IN FIE	LD 1.
	NON-ZERO, INDICATES DATA TYPE 7 HAS DELTA-F DATA IN FIE	.0 1.
42	CONVERSION CONSTANT FOR DISTANCES GENERATED IN GAIN.	
	MUST BE INPUT = 3443.9336 NM/ER OR 6975.246 KYD/ER	
43	LOGICAL TAPE NUMBER FOR ANOTHER COMPACTED DATA TAPE TO	BE
	GENERATED IN TRAIN FOR DESIDUALS ANALYSIS.	
44	LOGICAL TAPE NUMBER FOR TRAJECTORY TAPE TO BE USED TO OBTAIN CALCULATED OBSERVATIONS AND REFERENCE ORBIT FOR	
	RESIDUAL'S - MUST BE ON CHANNEL B.	
45	LOGICAL TAPE NUMBER FOR TRAJECTORY TAPE TO BE USED TO	
·-	OBTAIN MEASURED OBSERVATIONS FOR RESIDUALS ANALYSIS -	
	MUST BE ON CHANNEL B.	
46	NON-ZERO INDICATES SPECIAL TRAJECTORY TAPE GENERATION	TTAPE
	=1. FIRST OF MULTIPLE CASES	
	=2. OTHER THAN FIRST OR LAST CASE	
	#3. GNLY CASE	
		,
47-50	=4. LAST OF MULTIPLE CASES (NOT USED)	

Figure 4-2. NUMB Storage Area

T (** A	CO . MÖRTAN TUNTALTENA	ž ni	
11.10	G - OPTION INDICATORS	Control many days (Sidding control material section and section an	<u>Inant</u>
ŀ	CURRENT FUNCTION BEING EXECUTED	at. roeta	- NAME
×	CONSENT FORCITOR DELING EXECUTED	AT TOACH	\-
an Three miles areas	de destructuramente de la completa del la completa del la completa de la completa del la comple	*2. TRACKING EJ: TRAJECTORY	
	•	*4+ GAIN	
		7 RESTONE	
2	RESTORE (1) LAST GOOD SOLUTION		
3	CURRENT LINK BEING EXECUTED		* *
4	REASON FOR EXIT FROM MAIN (1-HA	xinum number of iterations.	
Annual California	2-CONVERGED, 3-TRAJECTORY COM	PLETEDI	Andrew Company
5	CORRECTIONS ARE HITTING BOUNDS		-
6	= 0, COMPLETÉ SIGHTING EPHÉMERI	5 PRINTER	
	F L, ONLY RISE, SET, MAXIMUM EL	evation teres printed	
7	(USED INTERNALLY)		
<u> </u>	ANALYTIC TRAJECTORY PARTIALS (O		
	BOUNDS PROVIDED FOR LEAST SOUAR	FR POPOLYDIK (T) PR WO BOOWDS (C	PP
12	(NOT USED)	010	- THE WE
11	T-MATRIX OPTION IF#C. NO T-MAT	HOSHPHIKFOT NO EARTH-ELATTEND	TEATX
		HOSH HIRHO, USE TARTH FLATTERE	
	=2, CALC. DR	HOOM HICKORY NO SARTH ELATTERIN	16.
-	ES. CALC. DR	HODH-HIRHOF USE EARTH FEATTERLY	-
12	PARAMETER SPECIFYING SEQUENCE OF		- LTIN
13	PERFORMED		
34	TUSED IN GETAL THE DE SCRI COTE	UT - NON-ZERO, DU NOT BORT	
15	TRAJECTORY COMPARISON 2PTION	• • · · · · · · · · · · · · · · · · · ·	101kk
	IF LOIFF *D. REGULAN TRAJECTORY		
		ECTORY AS REFERENCE OF HISPE	
		FERENCES WALTTEN ON DTAPE	
	*3 OTHER THAN FIRST O	R LAST COMPARISON CASES	7
	EH. FOR ONE AND GHLY	COMPARISON SASE	
	#5. LAST COMPARISON	W O. W. C	
16	TAPE UNIT FOR TRAJECTORY TAPE &		and the same of th
17	SET NON-ZERO IN TEET IF TO IS A		
18	NON-ZEROVÁCCUMJENTE ATA IN DOLB		
70	TFOR ATA LESS THAN 27461	merchant and management of the second	بتبيخ فيستنه فنفتست
1/3	USED INTERNALLY!		in the second of
20	IF NON-ZERO. OPERATE IN 3 PTS.A	PASS MODE	and the st
71	UNITED THE TOTAL TOWN THE ZHE DIFFER	CHCE EULIUKS CONTROLS EULIUNG	وب سبب ب
,			
معيد ويصفر بد ذهاميرية	FIRST 2 AND LAST 2 POINTS		
\$\$	HO A AND E RESIDUALS ARE NOT IN	icluded in rae restouals analys	lá <i>c</i> i s 7_c
عدند	FL. INCLUDE RESIDUALS.		
33	(USED THYERNALLY)		
24	LUSED INTERNAULYL		
25 26	SET IN TSEY IF ALPITA PARTIALS	WE TO BE COMBRIED.	The second secon
	AFTER COMPLETING FIFA. CALL PST	Erab ok no sext boscitouser o	121
28	IUSED INTERMALLYS	y the first of the contract of	-15 THE THE
29	IF NOW ZEROE BEFOU MATEICES ARE	connection with althe detailed of	numers -
many of the same	SUL CULL SELVE SELVE	Carrent Es VACA KENT LESIANTIGHT	the second second
प्रके	EF MON ZERO. THE OLD TRACE ST	V HATELY ROOM! ATTOM- TE TIEFE !	cuerv
- (T)	SOUT OREYS	. Simme excelentarities by about	withings the
was seemed and	نها يو وسينس من	واستنبار في المستنب المناف والتناف وال	and the second of the second of the second

Figure 4-3. IFLAG-Storage Area

DRAG		I NPU
1	CDA/W	NAME
;	ATMOSPHERE OPTION, IF = 0, ARDC 1959	
	= 1, LOCKHEED	
3	D1 = 6.63 (LOCKHEED)	
4	D2 = -15.684 (LOCKHEED)	
5	INOT USED)	
6	INPUT DRHOCH+H/RHO FOR H SETWEEN 76 AND 108 N.MI (-8.6)	
7	INPUT DRHODH#H/RHO FOR H BETWEEN 108 AND 376 M MI (-5.55)	
8	CALCULATED DRHODH*H/RHO (SEE IFLAG(11))	
9	USED INTERNALLY TO STORE THE INTERPOLATED VALUE OF CD FROM CD TABLE	ES
10	IF NON-ZERO, USE DRAG TABLE. =1.0RAG TABLE VS ALT AND MACH NO	
	#2,DRAG TABLE VS TIME	
11	CRITICAL ALTITUDE. ABOVE - USE ALT TABLE	
	BELOW - USE MACH NO TABLE	
	DRAG TABLE - CDAYW VS ALT OR TIME	
36-59	- CDA/W VS MACH NO	
	RESERVED FOR LATER USE INPUT REVOLUTION NUMBER FOR ITIN = 3	REV

Figure 4-4. DRAG Storage Area

1-6	INITIAL CONDITIONS
7	T-ZERO
9	CDA/W
9	GM
10-18	J2-J10
13-38	J21-J66 QRDERED J21-J31-J41J6-J66
39-53	LAMBDA21-LAMBDAG6 SAME
59	LUSED INTERNALLY)
60	OMEGASUBA - ATHOSPHERE ROTATION RATE
51	T1 THRUST STIPEXPFS-122-TS
62	72
68-75	ICS, TO, AND DRAG FOR SATELLITE NO. 2
8Ç-87	ics, to, and drag for satelilite no. 3
92-99	IGS, TO, AND DRAG FOR SKIELLIVE NO. 4
116-123	ICS. TO, AND DRAG FOR SAMELLITE HOL &

Figure 4-5. CNDT (Parameter List) Storage Area

DPRAM	CODE	LI	57									F	POSITION	INPUT
													IN	NAME
												(INDT LIST	
	1	2	3	4	5	6	7	8	9	10	11	12		
DOPRAM	CDA/V	GM	J2	٧3	J4	J5	J6	J7	J8	J9	J10	J21	3~19	
D3	J22	J31	J32	J33	J41	J42	J43	J44	J51	J52	J53	J54	20-31	
D5	J55	J61	J52	J63	J64	J65	J66	L21	L22	L31	L32	L33	32-43	
D7	L41	L42	L43	144	L51	L52	L53	L54	L55	L61	L62	L63	44-55	
D9	L64	L65	L66		OA	T1	T2						56-67	
D11 *	ALPH	DELT	BETA	A	R	V	TO	CDA/W					68-79	PSAT2
D13 *	ALPH			A	R	V	10	CDA/W					80-91	PSAT3
015 *		DELT		A	R	V	TO	CDA/W					92-103	PSAT4
D17 *	ALPH	DELT	BETA	A	R	٧	TO	CDA/W					104-115	PSAT5
D19 *			BETA	A	R	V	10	CDA/W					116-127	PSAT6

^{*} REFERS TO SATELLITES 2-6

Figure 4-6. DPRAM (Code List) Storage Area

KIN	D - MISCELLANEOUS FIXED POINT INPUT	I NPUT NAME
1	UNIT FOR INPUT BCD RADAR DATA TAPE	18C01
2	UNIT FOR INPUT BINARY COMPACTED RADAR DATA TAPE	IBINI
2	USED INTERNALLY	
4 _	EPOCH DATE - YEAR	YEAR
5	HTMCM - ,	HTMM
6	, - DAY	DAY
7	PRCDE - DUIPUT CONTROL	PRODE
3	PARAMETER	
9	FLOCK FLAG	

Figure 4-7. KIND (Miscellaneous Fixed Point Input) Storage Area

INPUT
TZNE
HR
MIN
SEC
ANOML
(2)
(3)
(4)
ANOMZ
A NOM3

Figure 4-8. XTRA (Miscellaneous Floating Point Input) Storage Area

USE OF TEMP FOR IN	TEGRATION (DAUX AND PERT)	
(1)	T	
(21-(4)	X	
(5)-(7)	PSI(P1)	
(3K+2)-(3K+4) (185)	PSI(PK) DELTA-T	
(186)-(168)	X-DCT	
(189)-(191)	PSI-DOT(P1)	
(3<+186)-(3K+186)	PSI-DOT(PK)	
(369)-(371) (372)-(374)	X-DOUBLE DOT PSI-DOUBLE DOT(P1)	
(3K+369)-(3K+371)_	PSI-DCUBLE DOT(PK)	
(552)		
(553)	R R#¤2	
(554) (555)	R**3	
(556)	R**5	
(257)	R	GRAV CALLING SEQUENCE
(558) (559)	SIN(PHI) CDS(PHI)	GRAV CALLING SEGUENCE GRAV CALLING SEGUENCE
(560)	SIN(ALPHA(G))	GRAV CALLING SEGUENCE
(561)	COS(ALPHA(G))	GRAV CALLING SEGUENCE
(562)	SIN(ALPHA)	GRAV CALLING SEGUENCE
(563) (564-566)	COS(ALPHA) F(1)	GRAV CALLING SEQUENCE
(567-569)	GLH	GRAV CALLING SEQUENCE
(570-578)	ROT MATRIX	GRAV CALLING SEGUENCE
(579)	U POTENTIAL	GRAV CALLING SEQUENCE
(580-588) (589-608)	A B	GRAV CALLING SEQUENCE GRAV CALLING SEGUENCE
(507-628)	-	GRAV CALLING SEQUENCE
(629-637)	D	GRAV CALLING SEQUENCE
(638-657)	E	GRAV CALLING SEGUENCE
(658-677) (678-697)	SIN(M(LAMBDA-LAMBDA(MN))) COS(M(LAMBDA-LAMBDA(MN)))	
(698-706)	DFDX(1) V-MATRIX	CKAT CKEEING SEGOCIACE
(707-715)	DFDX(2) T-MATRIX	
(716-724)	DFDXD U-MATRIX	
(725-727) (728-730)	DF/DX*(PSI(PK)) DF/DXDOT*(PSI-DOT(PK))	
(731-910)	DF/DB RHO (DENSITY)	
(917)	NIO (DENSITY)	
(918)	H (ALTITUDE)	
(919)	A (VEL OF SOUND)	
(920) (921 ~ 923)	M (MACH NUMBER)	
(924)	D/V(A) = XHO/2*V(A)*CDA/W	······································
(925-927)	F(3)	
(928) (935-937)	ABSF(X-DOT) = V(A) F(4) THRUST FORCE	
(938-943)	ABSF(X(J))**3	
(944-949)	ABSF(X-X(J))	_
(950-955)	ABSF(X-X(J)) **3	
(956-961) (962-964)	ABSF(X-X(J))**5 X-X(1)	
(965-967)	X-X(2)	
(968-970)	X-X(3)	
(971~973)	X-X(4)	
(974-976) (977-979)	X-X(5) X-X(6)	
(980-982)	F(2) · ·	13
(983-1000)	INTERPOLATED VELOCITIES OF	FOTHER BODIES
•		

Figure 4-9. TEMP Storage Area (As Used for Integration)

(1-552)	POSITION, VELOCITY, ACCELERATION
(553)	W1
(554)	W2
(555)	W3
(556-735)	DW1DP1_THRU_DW3DP60
(736)	WIDOT
(737)	W2DOT
(738)	W3DOT
(739-918)	DWIDOTDP1 THRU DW3DOTDP60
(919)	U1
(920)	U2
(921)	Ú3
(922)	R
(923)	V1
(924)	V2
(925)	V3
(926)	V

Figure 4-10. TEMP Storage Area (As Used by Subroutine FILL in Link FITB)

					INPUT
CELLS	ROUTINES	TYPE	USAGE	EGUIA	NAME
(1)	CSCP	TEMP			
(1-2)	TSET	TEMP	WHEN COMPUTING ELEMENTS (XY2A)		
(1-5)	CHAIN, INCN1,	TEMP	WHEN COMPUTING JULIAN DATE		
	TRAJ3.TROUT		,		
	INCN				
(51)	PTRAJ,TRAJ3	PERM	ASCENDING NODE AND SPEC PRINT FLAG	ASCFL	
(52)	MAIN, PTRAJ	PERM	REV NO (FIXED PT)	IREV	
(53)	PTRAJ,TRAJ3	PERM	NODAL CROSSING TIME	ECTIM	
(59-100)		PERM	FOR LATITUDE, LONGITUDE PRINT TABLES		
(59)	INCN+LATPR		NUMBER OF LATITUDES (FIXED PT)	NLAT	LATPR
(60-69)	INCN		LATITUDES IN DEGREES	ELAT	(2-11)
(70-79)	INCN+LATPR		LATITUDES IN RADIANS	FLAT	
(80)	INCN, LATPR		NUMBER OF LONGITUDES (FIXED PT)	NLAM	LONPR
(81-90)	INCN		LONGITUDES IN DEGREES	ELAM	(2-11)
(91-100)	INCN+LATPR		LONGITUDES IN RADIANS	FLAK	
(1-100)	FITB	PERM	USED THROUGHOUT THE LINK		
(1-100)	RESIDUE	PERM	USED THROUGHOUT THE LINK		
(1-100)	PLAIN	PERM	USED THROUGHOUT THE LINK		*

Figure 4-11. TUMP Storage Area

CELLS	ROUTINES	USAGE	I NPUT NAME
~~~	NOUT THES		MARIE
(1-5)		EXPONENTIAL THRUST	
(1)	INITA,INCN, INCN1,INPUT	T1	THRST
(2)	INITA, INCN, INCN1	72	
(3-4)	INITA , INCN1 ,	START AND STOP TIMES, IN SECONDS, FROM	
	KTIM,TRAJF, TRAJ3,TRAJ4	MIUNIGHT OF EPOCH	
(5)	INITA . INCN1 .	THRUST INDICATOR + = 0 WHEN NO THRUSTING	
	PERT+TRAJF+ REINT	# RESULTANT OTHERWISE	
(6-19)		(NOT USED)	
(20)	*CMPR.FILL *FILLR.ORES	RANGE REFRACTION CORRECTION	RREFC
(21)	TRAJF,TRAJ3,	FLAG SET IN TRAJF. TRAJ3 AND TESTED IN	
422.00	TSET1+TSET2	TSET1/TSET2	-
(22–28) (29)	INCN+INCNI+	(NOT USED) INTERNAL COUNT OF ORBIT ADJUSTS FROM XKICK	
1671	KTIM, REINT,	ATTENDAL COURT OF ORDER ADJUSTS FROM ARICK	
	TRAJF,TRAJ3		
(30)	INCN.INCN1.	INPUT NUMBER OF ORBIT ADJUSTS (KICKS) IN	NXK
	INPUT, KTIM,	XKICK - MUST BE LESS THAN 51	
	TRAJ3		
(31-130)	INCN.INCN1.	BLOCK WHERE ORBIT ADJUSTS ARE INPUT AS FOLLOWS	XKICK
	REINT, TRAJE,	XKICK = TIME OF KICK(1) IN SEC FROM MIDNIGHT OF EPOCH	
	TRAJ3	(2) = DELTA VEL(1) IN FT/SEC	
		(3) = TIME OF KICK(2) IN SEC FROM	<del></del>
		MIDNIGHT OF EPOCH	
		(4) = DELTA VEL(2) IN FT/SEC	
		*	
		(2*NXK-1) = TIME OF KICK(NXK) (2*NXK) = DELTA VEL(NXK)	
(131-200)	TRAIN, INPUT	INITIAL CONDITIONS FOR MULTIPLE SATELLITES	
(131-144)		SATELLITE 2	SAT2
(145-158)		SATELLITE 3	SATE
1159-172		SATELLITE 4 "	SAT4
(173-186		SATELLITE 5	SAT5
(187-200)		SATELLITE 6 SATJ (J=2,3,6) INPUT IS AS FULLOWS	SAT6
		ISATJ = YEAR	·
		1 2 = MTMOM = 1 2 I	
		4 = HOUR	
		5 × MINUTES 6 * SECONDS	
		5 = SECONDS	
		8-13 = INITIAL CONDITIONS	
		14 = DRAG	

Figure 4-12. PUSH Storage Area

	11.5	77461	17460	77457	11913	77271	77201	77111	76651	1,5647	16503	76433	76243	76217	76205	76741	76011	75770	75732	75655	75557	75545	75463	75401	7387	75272	74762	74743	74742	14141	74162	73112	72746	12564
	8722 CELLS	00.1	:	•	ı	1	1	ı	,	1	ı		1	ı	1		ı	1		•	,		ı	:		,	•		1	•		,	•	ļ,
	BLOCKS NEEDED FOR ALL LINKS -	32561	32560	32526	32439	32441	32385	32329	32169	32167	32067	32027	10615	31887	31877	31717	31753	31736	31706	31661	31599	31589	31539	31489	31439	31418	31218	31203	31202	31201	30834	30282	30182	36106
	FOR A	EQU	1		ţ	•	:	1	,	,	1	;	٠	ı	1	,	•	:			ı		ı	•	,	ı	1		1	•		ŧ	ŧ	•
	CKS NEEDED		-	100	3,6	5.5	26	160	2	001	40	120	02	10	100	57	17	30	45	29	10	20	50	20	172	200	13	1	-	367	595	001	20	1000
	COMMON À - BLO	ALPH	AUS	ادا	נט	ខ	13	CNGT	CPRAM	DAVE	DPRAM	DRAG	ELL	FIC	FLEE	HEAD	IDTAPE	FFLAG	TTEMP I	ITRCD	X IND	NUMB	PARINT	PAICK	PRIIN	PUSH	100 M	Sus	SUSP	TRAJX	INCAL	TCRP	XTRA	LEND
(	<b>(</b>																																	

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* ***

いれていてき、これを見ることを持ちているがあり、これのでは、人間できているのでいるのでは、大きなないないでは、大きなないのでは、大きなないのでは、

COMMON Storage Area Blocks Needed for (A) All Links, (B) Fit and Data Generation Links, and (C) Fit Links Only Figure 4-13.

									V-24														
0 CF1 S											*												
LINKS - 430					_		_									· ;							
ATION	1	52517	5235	52207	52043	51057	50713	50547	50237	50073							}						
GENER	1	3 1	,		•		,	•										•					
COMMON B - BLOCKS NEEDED FOR FIT AND DATA GENERATION LINKS - 4300 CEISS	91716	21639	21739	21639	21539	21035	20439	20839	56932	20539			·										
. g	DEC	3 1		ı	•	,	•	1	ľ	1 1													
OCKS NEEDED	1800	100	BQ.	100	500	001	CSI	200	100	130			×					,					•
OMMON 8 - BL	GCK	BIAS	OPAR	ונפרכ	IPACD	9181	SHIPA	RPRAM	SIGGA	STAT											***************************************		
(B)				-									•								-		
												,								•			
				,																		,	

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大きない ちょうかいろう からから

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COMMON Storage Area Blocks Needed for (A) All Links, (B) Fit and Data Generation Links, and (C) Fit Links Only (Continued) Figure 4-13.

300 DEC 19339 DCT 45613 100 - 19039 - 44773 100 - 18739 - 44462 100 - 18738 - 44462 10 - 18638 - 44462 10 - 18638 - 44515
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COMMON Storage Area Blocks Needed for (A) All Links, (B) Fit and Data Generation Links, and (C) Fit Links Only (Concluded) Figure 4-13.

# 4.3.2 Use of TREG For Integration (Subroutine COW)

If n is the total number of initial condition and differential equation parameters, then the quantities X,  $X_{pi}$ ,  $\dot{X}$ ,  $\dot{X}_{pi}$ ,  $\dot{X}$ , and  $\dot{X}_{pi}$  will be located in storage area as specified in Table 4-1.

Table 4-1. Locations of Quantities Used by Subroutine COW

Quantity	Location
x	TREG(K) to TREG(K-2)
X _{pi}	TREG(K-3i) to TREG(K-3i-2)
×	TREG(K-NEQ) to TREG(K-NEQ-2)
$\dot{\textbf{x}}_{\mathtt{pi}}$	TREG(K-NEQ-3i) to TREG(K-NEQ-3i-2)
ÿ	TREG(K-2NEQ) to TREG(K-2NEQ-2)
Х _{рі}	TREG(K-2NEQ-3i) to TREG(K-2NEQ-3i-2)
NEQ	TREG(K+3) (scaled at B35, set by COW)
Т	TREG(K+2) (current time)
ΔΤ	TREG(K+1) (current integration step size)

#### Notes:

- 1. NEQ = 3 (n + 1) (n = total number of initial condition and differential equation parameters)
- 2. K = dimension of TREG 3 (The dimension of TREG must be 90 (m + 1) + 3, where m = maximum number of initial condition and differential equation parameters.)

# 4. 3. 3 Initial-Condition and Differential-Equation Parameter Code List (ITRCD)

Table 4-2 specifies the coding whereby initial condition and differential equation parameter (ITRCD) storage locations are identified.

Table 4-2. ITRCD Storage Locations

Sequential Locations	Symbol	Description
1	ÎC	Initial condition parameter type (from CPRAM)
2	n	Total number of initial condition and differential equation parameters
3	Pi	Parameter Code No. 1
4	P ₂	Parameter Code No. 2
5	P ₃	Parameter Code No. 3
•		
•		
•	•	
n+2	P _n	Parameter Code No. n

#### Notes:

- 1. The P. correspond to locations in the CNDT list of parameters to be corrected in the PKICK list in the case of an orbit-adjust parameter.
- 2. The maximum number of initial condition and differential equation parameters is  $6\hat{0}$ .

#### SECTION 5

#### USAGE

Section 5 describes the input data, data-deck arrangement, tape requirements, sense-switching controls, and output associated with TRACE-D program applications, and is intended to resolve most questions pertaining to program usage. To facilitate reference to the following information, input-data characteristics have been separately considered with respect to each of the major program functions of trajectory generation, tracking, data generation, and residuals analysis (see Section 1.3 for explanation of these functions).

# 5. 1 INPUT DATA

(· 0)

Input data intended for use in connection with TRACE-D program operation fall into five categories of basic data that are common to the trajectory generation, tracking, data generation, and residuals analysis program functions and into specialized data that are applicable to each of these four functions individually. Section 5.1 presents a detailed description of the features characterizing each of these five principal input data categories.

The FINP, station-location and -identification data, observation data, and data generation specification load sheets are the four types of load sheets used for input by the TRACE-D program. Sample load sheets are included in the following discussions of applicable input data. Use of the FINP load sheets is facilitated by consideration of the following information:

a. Although the load sheet imposes an order on program input, the actual order of the cards is almost immaterial. The only restriction on card order is that cards without symbolic locations must follow the last card carrying the appropriate symbolic location. In the case where the same location symbol appears twice in succession, the last value read constitues the effective input.

- b. A prefix appearing in Columns 1, 19, 37, and 55 (Fig. 5-1) determines the mode of input. A blank indicates that the following value is to be read as a floating point number, an I as a fixed point integer, a D as BCD (Hollerith) information, a B as an octal number, and M as a matrix array. The END cards are used because the prefix E terminates the FINP reading function.
- c. Any card for which no value appears may be omitted. Blank fields are ignored except for the D prefix (BCD).
- d. No plus signs or commas are permitted,
- e. A decimal point should appear in each value unless it is an integer, in which case there must be no decimal point.

#### 5.1.1 Basic Data

The term basic data is defined as the data that are common to all the principal TRACE-D program functions. In addition to a list of the functions to be performed, the required basic data also include the specification of the trajectory (date, time, and initial conditions), the force model assumed, and the constants and parameters to be used in the trajectory integration. Although the force model and the trajectory-integration constants and parameters are "required" data, standard values are provided, so that replacement of these quantities thus is "optional" (see Appendix A for a list of the standard values). Certain options common to all functions relating to identification information, specification of the ballistic (drag) coefficient and the atmosphere model, selection of other-body perturbations, low-level thrusting, and orbit adjusts also are contained in the basic input.

Sections 5.1.1.1 and 5.1.1.2 present a line-by-line explanation of the TRACE-D basic data load sheet shown in Figure 5-1.

# 5.1.1.1 Required Input

Line 1: Functions to be Performed

Line 1 contains the ordered list of all functions to be performed by TRACE-D during a given run. Selection of functions is governed in accordance with the

TRACE-D Basic Input



GRAMMER,	7		KEYPUNCHED		VERIFIED	DATE		_ PAGE_	OF  73	
*1	<u> </u>		· · · · · · · · · · · · · · · · · · ·		***************************************				<del></del>	
12						<del></del>	<del>~~~~~</del>		<del> </del>	
16										
				•~~					<b>├</b> ──	
									<u> </u>	
		2	<u> </u>	17	Ţ	Input De	escript	ion		
	10	2 20 30 50	27 43 61	20 49 71	1 1 1					
SYMBOL	Į,	LOC.	VALUE	11	HI, HZ ITIN	Headings whi	cn wi	ı appea	r on out	pu
	1		<del></del>	-	1,2:	Itinerary Tracking				
1		ITIN		╁┸	3:	Trajectory				
2	L	YEAR		<u> </u>	4	Data Generat	ion			
3	I.	MNTH		İ	7:	Residuals An				
4		DAY				NTH/DAY/HR		SEC/T	ZNE	
5		TZNE		1		Epoch date a				
6	R	HR		<del> </del>	ICTYP	Type of initia				
7		MIN	·	<b>}</b>	1:	x, y, z, ż, ż				
9.	!	SEC	<del></del>	<del>-</del>	<b>2:</b>	α, δ, β, Α, τ, Ϋ				
				<del></del>	ર્યું કૈં:	$\mathbf{a}, \mathbf{e}, \mathbf{i}, \Omega, \omega, \tau$				
9	ᆛ	ICTYP		+	4:	λ, δ, β, Α, τ, V				
10		IC		╄	5:	Last trajecto				
	<b>.</b>	2		<b>!</b>	6:	Predicted so				
12		3		<u>i .</u>	9:	Same as CPF				15.0
13		4			7 o:	Same as 1, b Self-initializa		inne u	utta	
14		5	` .	T	lic ".	Initial-condit		414		
15		6		1	DRAG	CDA/W (ft ² /	ION MP	ut		
16		DRAG		<b>⁺~</b>	DRAG(2)	Atmosphere		k		
				-	0:	ARDC 1959 n				
17	1	2	}	╂	1:	Lockheed-Ja		L-J) n	nodel	
18_	8	3	<u> </u>	-	DRAG(3)	d1 for L-J m				
19		4		. <b> </b>	DRAG(4)	d2 for L-J m	odel*			
20	B	6			DRAG(6)	Density slope	for L	-J mod	le1,low-a	alt
21	8	7			DRAG(7)	Density slope		-à mod	lel,high-	al
22	1.	XTAMT	,	T	TMATX	T-matrix opt				
23	. 1	CTAPE	<u> </u>	T	CTAPE	Other body p		ations		
24		PRCDE		ΉΤ.	PRCDE	Print options				
	_			4	l: 2:	Ephemeris			station	pri
25	•	THRST	<del> </del>	+	3:	Residuals Partials		cial p		
<u> 26</u>	<b>.</b>	2		╂	4:	ATA.		ements des on	at rece	£20;
27	<b>-</b>	3		+	5:	Variational 1				<b>.</b>
Z8		5		<del> </del>	4 -	equations		des on		В
29	<b>.</b>	PKICK		<u> </u>	6:				not vsed	)
30	<b></b>	2		1	THRST	T1 (amplitude				•
31	<u>.</u>	3			THRST(2)	T2 (time con	stant)	min "		
32		4	<u> </u>	<u> </u>	THRST(3)	Start time (6	c from	n miðin	ight	
33.	1	NXK			THRST(4)	Stop time Joi	epoch	date	•	_
34		XKICK		1	PKICK -	Time (sec fro	om mi	inight o	ncogo. 1c	ď2
35		2	<u> </u>	T-	PKICK(2)	ΔV (ft/sec)				
36		3		1	PKICK(3)	by (deg)			****	,
		2	<del>                                     </del>	<del>  ``</del>	PKICK(4)			<u>.</u>	£ 4	
37	<b>5</b> -	<del></del>		<del>\~`</del>	NXK XKICK	Number of ex			wast, "	
38	<b>1</b> _	5		Į	DALFG	Time, $\Delta V$ , ti			اشية	-
39	<b>.</b>	6		Ĺ		True equinox				
40		DALFG	i	1	IFinout val	ues included i	n atan	daystie.		de

Figure 5-1. TRACE-D Basic Input Data Load Sheet

Code Numbers 1, 2, 3, 4, or 7, corresponding respectively to tracking data input, tracking computations, trajectory only, data generation, and residuals analysis.

Up to twelve functions may be selected. When this sequence is exhausted, TRACE-D will reset certain standard options, prepare to run another sequence of functions, read basic data, or stop if none is present. The foregoing example would be for a tracking case (Functions 1 and 2) followed by a data generation case (Function 4).

Lines 2 through 8: Epoch

	,		
2	I	YEAR	1963
3	I	MNTH	6
4	I	DAY	15
<b>. 5</b>		TZNE	0
6		HR	12
		MIN	45
8		SEC	15.5

In the usual case, wherein the year, month, and day are input with the year positive, the X-axis is directed to the vernal equinox (see Section 3.1.1). Alternatively, if the year is input negative, the X-axis would be directed to the longitude of Greenwich. The hour, minute, and second entries refer to midnight of zone time. GMT is Time Zone 0.

Lines 9 through 15: Initial Conditions

9	I	ICTYP	2
10		IC	126. 1
11		2	31.23
12		3	89
13		4	14.
14		5	22600Î14
15		6	25117.3

Line 9 indicates which of the ten IC types (1, 2, ..., 9, 0) are entered in Lines 10 through 15. The alternative ICTYP entries are characterized as follows:

- a. IC Type I Earth-centered inertial cartesian coordinates (x, y, z, x, y, z in units of feet and feet per second) (see Section 3.1.1.1).
- b. IC Type 2 Spherical coordinates (a, δ, β, A, r, v) in units of degrees, feet, and feet per second (see Section 3.1.1.2). In Line 14, negative r is interpreted as height above the earth's surface in feet. In Line 15, if v is negative, circular velocity is computed and used.
- c. IC Type 3 Orbital elements (a, e, i,  $\Omega$ ,  $\omega$ ,  $\tau$ ) in units of feet, degrees, and minutes (see Section 3.1.1.3).
- d. IC Type 4 Same as Item b. above, with longitude  $\lambda$  replacing right ascension a.
- e. IC Type 5 No IC's input. The last trajectory point of the immediately preceding case is used.
- f. IC Type 6 No IC's input. The corrected initial conditions from the last previous tracking run are used.
- g. IC Type 8 Either Type 1 or 2 above, but in units of earth radii, minutes, and radians. Type number is entered at CPRAM (see Section 5.1.2.2).
- h. IC Type 9 Same as Type 1 above, but in units of earth radii and earth radii perminute.
- i. IC Type 0 No IC's input. For a tracking run, two R, A, E sets are used from the data to calculate a set of initial conditions (see Section 3.6.6).

### 5.1.1.2 Optional Input

Lines 16 through 22: DRAG and T Matrix

16		DRAG	. 01	
17	I	2	1	
18_		3 ⁻		
19		4		
20		6	-8.6	
21		7	-5.55	
22	I	TMATX		

Line 16 contains the drag parameter  $C_D^A/W$  in square feet per pound and Line 17 contains the atmosphere model specification (ARDC 59 or Lockheed/Jacchia). The ARDC model will be used when DRAG (2) is 0 and the Lockheed/Jacchia model when DRAG (2) is 1. If line 17 is a 1, Lines 18 and 19 contain quantities used in the Lockheed/Jacchia model.

Lines 18 and 19 contain d₁ and d₂, respectively. (See Appendix C.) These are values of certain constants in the Lockheed-Jacchia atmospheric density expressions.

An entry in Line 22, TMATX, will cause the T matrix to be used in the variational equations in accordance with the following options:

- a. TMATX = 0 T matrix is not used.
- b. TMATX = 1 Input  $\partial \rho / \partial h$  is used with no earth flattening.
- c. TMATX = 2 Input  $\partial \rho / \partial h$  is used with earth flattening.
- d. TMATX = 3  $\partial \rho / \partial h$  is calculated with no earth flattening.
- e. TMATX = 4  $\partial \rho / \partial h$  is calculated with earth flattening.

Also, with TMATX non-zero, Lines 20 and 21 should contain input values for  $\partial \rho / \partial h$ . Lines 20 and 21 contain  $\partial \rho / \partial h$  for altitudes between 76 and 108 n mi and between 108 and 376, respectively, (see Appendix C). It should be noted that input values for  $\partial \rho / \partial h$  must be used with the ARDC 1959 model.

³The notation LLLLL(n) used in this section specifies storage location within an array. The LLLLL portion of the symbol is associated with the first cell in the array and the (n) indicates the  $n^{th}$  cell (i. e., Location LLLLL + n - 1).

If a variable  $C_D$  term is desired, the drag table option may be utilized. In this case the drag parameter may be considered to consist of the product of two terms,  $(C_DA/W)\times C_D'$ , wherein  $C_DA/W$  is a constant which can be differentially corrected by the use of the variational equation and  $C_D'$  may be considered a function of Mach number below a certain altitude and as a function of altitude at points above that altitude. Alternatively,  $C_D'$  may be considered a function of time. In either case, use of the drag table is necessary.

When the drag table is not used, input of  $C_D^A/W$  into the DRAG location does not change usual TRACE operation. In this case  $C_D'$  is automatically set equal to 1. If the drag table is used, the following additional inputs are required:

- a. DRAG(10) If DRAG(10) = 0, tables not used.

  If DRAG(10) = 1, Mach and altitude tables used.

  If DRAG(10) = 2, time table only used.
- b. DRAG(11) Altitude above which altitude table is used and below which Mach table is used (needed if (DRAG(10) = 1).
- c. DRAG(12) = 0 Used by interpolation routine.
  - DRAG(13) Altitude table, or time table if DRAG(10) = 2 through (35)  $(h_1, C'_D(h_1), h_2, C'_D(h_2), \dots, h_n, C'_D(h_n), 0, 0$  or  $t_1, C'_D(t_1), t_2, C'_D(t_2), \dots, t_n, C'_D(t_n), 0, 0$ .
- DRAG(36) = 0 Used by interpolation routine.
   DRAG(37) Mach table (stored as noted in Item c. above). through (59)

Line 23: Other-Body Perturbations

# 23 I CTAPE 7

If perturbations due to other bodies in the solar system are to be included in the trajectory calculations, a planetary coordinate tape must be mounted and the logical-tape unit number must be entered at CTAPE.

#### Line 24: Print Code

# 24 D PRCDE 1 2 3 4 5 6 7 8 9 10 1112

The print-code entry consists of two BCD words accommodating six character positions each. Entry of an X at any of these twelve positions will initiate corresponding outputs in accordance with the following:

- a. (1) Trajectory (trajectory only option)
- b. (2) Residuals (tracking only option)
- c. (3) Partials (tracking only option)
- d. (4) A^TA after each iteration (tracking only option)
- e. (5) Variational equations (trajectory only option)
- f. (6) Orbital elements (trajectory only option)
- g. (7) Do not print station locations (tracking and data generation)
- h. (8) Not used
- i. (9) Special trajectory prints⁴
- j. (10) Orbital elements at ascending nodes only (trajectory only option)
- k. (11) Not used
- 1. (12) Suppress all trajectory print except ascending nodes (trajectory only option)⁵

Lines 25 through 28: Exponential Thrust

	غيستيسب		
L.	25	THRST	
	26	2	
	27	3	
	28	4	

If an exponential thrust is to be used, the quantities  $T_1$  in units of force/
mass =  $\tilde{\pi}/\sec^2$ ,  $T_2$  in units of  $\tilde{m}\tilde{n}^{-1}$ , and  $t_s$  and  $t_f$  in seconds from midnight

⁴Prints will occur at times of maximum and minimum altitude above the oblate earth, at times when the flight-path angle equals 90 degrees and at special latitudes and longitudes if values are entered (see Section 5.1.2.2).

⁵If the option to write a binary trajectory tape (B7) has been selected, the writing of that tape is controlled by the PRTIM entries (see Section 5.1.2.1).

of epoch date must be input at THRST, THRST(2), THRST(3), and THRST(4) locations, respectively.

Lines 29 through 32: Instantaneous Orbit Adjusts

	فبسنتال		فالمراجع والمستون والمستون والمستون والمستون	
29		PKICK	89020.31	'
30		2	200.	
31		3	0	
32		4	62.	

Instantaneous orbit adjusts are input at PKICK. Line 29 contains  $t_1$  (time of first orbit adjust,  $OA_1$ ) in seconds from midnight of epoch, Line 30 contains K (magnitude of velocity change of  $OA_1$ ) in feet per second, Line 31 contains  $\theta_y$  (yaw angle for  $OA_1$ ) in degrees, and Line 32 contains  $\theta_p$  (pitch angle for  $OA_1$ ) in degrees.

The TRACE-D program will accommodate up to six orbit adjusts. Additional cards may be added as necessary for  $OA_2$  through  $OA_6$ .

Lines 33 through 39: Extra Kicks

	•		•	
33	I	NXK	3	
34		XKICK	63456	
35		2	.2	
36		3	88721	
37		4	10.	
38		5	101018	
39		6	. 02	

Up to fifty fixed orbit adjusts (i.e., instantaneous changes of the in-track velocity component) may be input at XKICK. It should be noted that these orbit adjusts are not parameters for differential correction, but are applied in the equations of motion only and are independent of the PKICK inputs. The number of extra kicks ( $\leq 50$ ) is input at NXK, and the table of times and  $\Delta V$  values is input beginning at XKICK. The format is time,  $\Delta V$ , time,  $\Delta V$ , etc., in units of seconds from midnight of epoch day and feet per second, respectively.

# Line 40: Equinox Precession Corrections

	·		7
40	DALFG .0	1002	1
40	DALFG	1002	1
The same of the sa			-

The rotational position of the earth with respect to the inertial system is characterized by the right ascersion of Greenwich at midnight on the day of epoch  $(a_g)$  and is computed with respect to the mean equinox of epoch date. An additional factor for correcting to true equinox of epoch date optionally may be input at DALFG in units of degrees.

## 5.1.2 Trajectory Only

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Since for purposes of this document the terms "trajectory" and "ephemeris" are essentially equivalent, these designations will be used interchangeably, with the selection in a particular context usually historically motivated.

A similar situation exists for the terms "tracking" and "orbit determination."

Detailed description of the TRACE-D trajectory input load sheet shown in Figure 5-2 is presented in Sections 5.1.2.1 and 5.1.2.2.

#### 5.1.2.1 Required Input

Lines 1 through 7: Print Time Vector

	1		I	PRTIM	*	T
n	2		Ι	2	,	T
to	3			3		Τ
$\Delta^{t_1}$	4			4		I
$\mathtt{T}_{\mathbf{l}}$	5			5		I
$\Delta t_2$	6			6		Τ
$T_2$	7	•		7_		
			,			T

The above sequence of print times is for outputs selected by PRCDE entries (Line 24, Fig. 5.1). As many as nine sets of print intervals may exist (Line 2). In the case of the ith set, output is from  $t_{i-1}$  to  $t_i$  at intervals of  $\Delta t_i$ , with all times in minutes from midnight of epoch date if PRTIM = 1 or from epoch if PRTIM = 0. Additional cards may be inserted if  $3 \le n \le 9$ . It should be noted that a normal print at epoch is automatic.

Figure 5-2. TRACE-D Trajectory Input Load Sheet

# 5.1.2.2 Optional Input

Lines 8 through 15: Variational-Equation Partial Derivatives

8	D	CPRAM								
9	D	DPRAM								
10	$\mathbf{g}$	3			Ŀ					
11	D	5				*				
12	D	7								
. 13	D	9								Ц
14	D	KPRAM							L	Ц
15	D	3					Ĺ			

An X entered in any CPRAM, DPRAM, or KPRAM character position causes the corresponding variational equation to be solved. Printout of the partial derivatives will occur only if an X is entered at Character Position 5 in the PRCDE print cede entry location. The ordering of entries in the CPRAM, DPRAM, and KPRAM character position boxes is as follows:

#### a. CPRAM (Initial Condition Parameters) (Line 8)

The first position specifies which one of three types of initial conditions is applicable, and succeeding positions indicate the particular parameters that are desired in each case. Ordering of CPRAM parameter entries for initial condition (IC) Types 1, 2, and 3 is shown in Figure 5-3.

	(IC Type	)						-			
(either)	ı	×	у	z	×	ý	ż	to			
(or)	2	a	δ	β	Α	r	v	t _o			
(or)	3	a	e	i	Ω	ω	т	tc	;		

Figure 5-3. Ordering of CPRAM IC Parameter Entries

# b. DPRAM and KPRAM (Differential Equation Parameters) (Lines 9 through 15)

The ordering of DPRAM and KPRAM parameter entries is shown in Figure 5-4, wherein  $T_1$  and  $T_2$  are the exponential thrust parameters and  $a_i$ ,  $K_i$ ,  $\theta_{y_i}$ , and  $\theta_{p_i}$  are the OA number  $(1, 2, \ldots, 6)$ ,  $\Delta V$  magnitude, yaw angle, and pitch angle, respectively.

Sixty differential equation parameters is the maximum number which may be selected for any one run.

DPRAM	Drag	μ	Ĵ ₂	J ₃	J ₄	J ₅	J ₆	J ₇	J ₈	J ₉	^J 10	J ₂₁
3	J ₂₂	J ₃₁	J ₃₂	J ₃₃	J ₄₁	J ₄₂	J ₄₃	J ₄₄	J ₅₁			J ₅₄
5	J ₅₅	J ₆₁	J ₆₂	J ₆₃	J ₆₄	^J 65	J ₆₆	λ ₂₁	λ ₂₂	λ ₃₁	λ ₃₂	λ ₃₃
7	λ ₄₁	λ ₄₂	λ ₄₃	\ ₄₄	λ ₅₁	հ ₅₂	λ ₅₃	λ ₅₄	λ ₅₅	λ ₆₁	λ ₆₂	λ ₆₃
9	λ ₆₄	λ _{6,5}	^λ .66		³ a	T _{1.}	T ₂		·			
KPRAM	a _l	ĸ ₁	$\theta_{\mathbf{y_l}}$	$\theta_{\mathbf{p_l}}$	a ₂	ĸ ₂	θ _{y2}	θ _{p2}	a ₃	Έκ ₃	θ _{y3}	$\theta_{p_3}$
3	a ₄				a ₅							

Figure 5-4. Ordering of DPRAM and KPRAM Differential Equation Parameter Entries

Lines 16 through 18: Trajectory Comparison Options

	7		
16	IDIFF	1	
17 💌 I	NTAPE	1.5	
18 1	DTAPE	14	

Tape units and case indicators required for the trajectory differencing function are as follows:

A Miner of the Man Man Control of the Man Control o

- a. IDIFF = 0 A regular trajectory run is indicated.
- b. IDIFF = 1 The reference trajectory will be written on the logical tape specified by NTAPE.

  If no entry is input at NTAPE, Logical Tape 15 will be used.
- c. IDIFF = 2 The differences between the present and reference cases are computed and written on the logical tape specified by DTAPE. If no entry is input at DTAPE, Logical Tape 14 will be used. The difference tape specified by DTAPE is rewound at the beginning of the case.
- d. IDIFF = 3 Conditions are the same as when IDIFF = 2 except that the tape specified by DTAPE is not rewound.
- e. IDIFF = 4 The tape specified by DTAPE is rewound at the beginning of the case and unloaded upon completion.
- f. IDIFF = 5 The tape specified by DTAPE is unloaded upon completion of the case.

The significance of the foregoing options is that if a single-comparison case is to be processed, IDIFF = 1 is used for the reference case and IDIFF = 4 for the perturbed case. If a series of perturbed cases are to be processed, IDIFF = 1 is used for the reference case, IDIFF = 2 for the first perturbed case, IDIFF = 3 for all intermediate cases, and IDIFF = 5 for the last perturbed case.

Note that the tapes generated by this option cannot be used in the residuals analysis function.

Line 19: Revolution Number

	<del></del>
10 777	
19 REV	_   -(

If an initial value other than zero is desired for the revolution number, it may be input at the REV location. This value must be reinitialized for each individual case.

## Line 20: Trajectory Tape Generation

1

在我们大小孩子,一点一个孩子不知的一种一种的一种的一种,我们就是我们的一个一种的一个一个我们的一个一个人,我们就是我们的人,我们就是我们的人们的一种,我们们们们

20 I TTAPE 3

If TTAPE is non-zero, a binary trajectory tape will be generated on Logical Tape 15 (physical tape B7) in accordance with the following input options:

- a. TTAPE = 0 Tape will not be generated.
- b. TTAPE = 1 Tape will be rewound before generating but not unloaded after completion. This entry should be used for the first case when more than one case is involved.
- c. TTAPE = 2 Tape will not be rewound before generating and not unloaded after completion. This entry should be used for all intermediate cases.
- d. TTAPE = 3 Tape will be rewound before generating and unloaded atter completion. This entry should be used when only one case is involved.
- e. TTAPE = 4 Tape will not be rewound before generating but will be unloaded after completion. This entry should be used for the last case.

The format of this tape is appropriate for use by the residuals analysis function for differencing trajectories (see Appendix E). However, this tape is not suitable for the trajectory-comparison option of the trajectory-only function.

Lines 21 through 28: Latitude and/or Longitude Prints

nl	21		I	LATPR	3
	22	ì		2	10.
	23			3	15.
	24			4	20.
n ₂	25		1	LONPR	3
	26			2	200.
	27		·	3	100.
	28			4	180.

Line 21 contains  $n_1$  ( $n_1 \le 10$ ), or the number of special latitudes at which trajectory prints are requested, and Lines 22 through 24 contain the special latitudes. Additional cards may be added if  $4 \le n_1 \le 10$ .

Line 25 contains  $n_2$  ( $n_2 \le 10$ ), or the number of special longitudes at which trajectory prints are requested, and Lines 26 through 28 contain the special longitudes. Additional cards may be added if  $4 \le n_2 \le 10$ .

Note that an X must be entered in Character Position 9 of the PRCDE entry if either of the foregoing options are selected.

# 5.1.3 Tracking

Detailed description of the TRACE-D tracking input load sheet shown in Figure 5-5 is presented in Sections 5.1.3.1 and 5.1.3.2.

## 5.1.3.1 Required Input

A tracking run for the purpose of obtaining residuals only with respect to a known orbit would require only the basic data plus station and observation cards. A more typical tracking run, which would involve differential correction of some number of parameters, would require inputs for parameter specification, bounds, sigmas, maximum number of iterations, station cards, and observations as noted in this Section.

## 5.1.3.2 Optional Input

Lines 1 through 14: Initial Conditions for Satellite 2

	_		
Year 1	L	SAT 2	1964
Month 2	I	2	2
Day 3	I	3	10
Hour 4		4	3.
Minute 5		5	30.
Second 6		6	52.
ICTYP 7	I	7	2
IC 8		8	352.
2 9		9	10.
3 10		10	90.05
4 11		11	165.
5 12		12	22580632.
6 13		13	25205.3
DRAG 14		14	. 015

If observations for a second satellite are to be input, Lines 1 through 14 are used for entry of epoch, initial conditions, and drag coefficient for Satellite 2. Lines 1 through 3 contain the year, month, and day, and Lines 4 through 6 contain the hour, minute, and second, Greenwich time. Line 7 indicates the type of initial conditions that may be entered in Lines 8 through 13 (Type 1, 2, 3, 4, 8, or 9). Line 14 contains the drag coefficient ( $C_DA/W$ ).

·養養者 いからいできる

MER ]7			KEYP	J.,,C					DATE PAGE
<del>-  '</del>									
1,	20	7 28					17	]	Input Description
37	38	1						SATZ	Epoch, initial conditions, and
		1	VAL	.UE			EXP	10	for Satellite 2.
1 1						十		CPRAM	Initial-condition parameters for
ĝ I						$\neg$	_	1	Satellite 1.
3 I	3	<del> </del>				$\dashv$		1	
-31 ÷	4	<del> </del>				+		i	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	5	·				+		1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
_5	6					-		1	5 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
_6. P / ∵ I		$\vdash$				-		DPRAM	Differential equation parameter
8	8					-+		<b></b>	
	19	<del>                                     </del>				+		DPRAM	D  u  20 30 40 50 60 70 80 90
_9						-		3	22 31 32 33 41 42 43 44 51 52
70	10					╛		5 7	55 61 62 63 64 65 66 21 22 31 3
<u> </u>	11	<del> </del>				-		<del></del>	41 42 43 44 51 52 53 54 55 61 6 64 65 66 ω _α Τ1 Τ2
12	12	<del>                                     </del>				-		9 :	0 10 2 0 0 Pa 1 1 1 2
	113	<del> </del>				-		D:	Drag for Satellite 1. Numbers
114 <u> </u>	14		-		1-1-	┰┦	_	1	degree and order of zonal coe
	CPRAM		╁╁	╟	╂-	╀	-	1	ficients, tesseral coefficients
16 I	DPRAN	-	╀	H	Н	H	4-	ļ	and tesseral arguments.
	13	144	Н÷	Ц.	Н-	11	4-	ωa	Atmospheré rotation raté Thrust amplitude
	) 5	<del> - - </del> -	<b>├</b>	-	₩	₩	+	T ₁ : T ₂ :	Thrust time constant
	7	144	₩.	╀	₩.	Ш	4	PSAT2/	And dot time Constant
	9	$\downarrow\downarrow\downarrow$	1	4	Ц.	Н	+	PSAT6	
21 [	PSATZ	$\coprod$	┦-	Щ	Ш.	Ц	١.		
<u> 22 I</u>	PSAT3	144	₩.	Ц.	11	11	_	PSATX	a   δ   β   A   r   v   t ₀   D
	PSAT4	Ш	$\bot \bot$	Щ	11	Ц	4		Markey Color ADD ADDrawd Jane
24 I	PSAT5	111	Ш	4	Ц.	Ц	┵	Į	(Note: Only ADBARV and drag parameters are available for
25 ° J	PSAT6	Ш	Ш	Ш	Ш	Ц	ᆚ.	1	Satellites 2-6)
	KPRAN	411	11	LL.	Ш	Ш	1	KPRAM	Orbit-adjust parameters
	) 3	$\bot \bot \bot$	$oldsymbol{\perp}oldsymbol{\perp}$	Ш	ᄔ	Ц			-
28	ENDS	<u> </u>				_		KPRAM	a1 b1 c1 d1 a2 b2 c2 d2 a3 b3
29	2	<u> </u>				_		3	a4 b4 c4 d4 a5 b5 c5 d5 a6 b6
30	3	<del>  </del>				_4		1	
31	4	<del> </del>						a:	Orbit-adjust number (≤6)
32	15					_		b:	ΔV magnitude (K)
33	6	<u> </u>				_		d;	Yaw angle Pitch angle
34	7	<del> </del>				_		BNDS	Differential correction bounds
35	8	<u> </u>							(entered in same sequence as
36	9	<u> </u>							paramèters above)
37	10							]	•
38	111							]	
39	12								
40	13					- 1		1	

Figure 5-5. TRACE-D Tracking Input Load Sheet

<del></del>	<del>'</del>	······				<del></del>	73
	<u> </u>						
	1.	2 20 20	7 20		17 38 83 71		Input Description
			47			RAPAR	Radar parameter array
SYMBOL	<u> </u>	1	{	LUE	EXP		
41	.№	RAPAR	05. 99		-	01. P 03, P	1 2 3 4 5 6 7 8 9 0
	<b></b> -	<del> </del>	ļ		-	04, P	
		<del> </del>		**	┤	1	
42		0101		1113	╁┰	P	Radar parameter number $(1 \le P \le 99)$
43		03.01		<del> </del>	╁┸	Line 1	Boxes 1-2: Station ID
44		04,01	l		1		Boxes 3-4: Pass ID
					$\perp$	] ,, ,	Boxes 5-10: Parameter Designation
45	.D	01.02				Line 2	Bound Estimate
46		03.02				SIGMA	Observation sigmas (weighting facto
47		04.02				isig	Table of codes defining use of SIGM.
	<u>.                                    </u>					4	table entries. For each SIGMA ent
48	D	01.03			44	4	quantity (1001 + K), where I = sigms index (Column 5 of station card) and
49		03, 03			+	-	K = data type, entered a correspon
50	<b>I</b>	04.03			-		ing location of ISIG table.
51		SIGMA			+	CEDIT	Maximum number of iterations Residuals editing (standard entry = 3
52		2			+	REFR	Table of refraction indices
53		3		- <del> </del>	+	1	(standard value built in at REFR)
54		4.				RREFC	Range refraction correction (0 = No, 13 = Yes)
55		5				SLT	Velocity for propagation-time
56		6				]	correction (E.R./min)
57		ISIG				IBCDI IBINI	BCD data-tape input (0 = No, 6 = Yes
58	ĮĮ.				<u> </u>	IDIMI	Compacted data tape input (0 = No, 1 = Yes)
	i.				-	DALFG	Table of additive corrections to
<u>60</u>	Ļ			<del></del> -	<del> </del>	1	initial right ascension of Greenwich
61 62	I I				╁──	1	(one entry per vehicle) (deg)
63		MAXIT			+	1	
64	. 4.	CEDIT			+	1	
65	-	2			1	1	
66	3	3				1	
67		REFR				].	
68		2			<del> </del>	ļ	
<u>69</u>		RREFC			-	1	
70	-	SLT		<del></del>	1	l	
71		IBCDI	<del></del>		<del></del>	{	
72	I	IBINI			1	1	
74	-	DALFG	·····		4	i	

Figure 5-5. TRACE-D Tracking Input Load Sheet (Continued)

TRACE-D
Tracking Input (3)

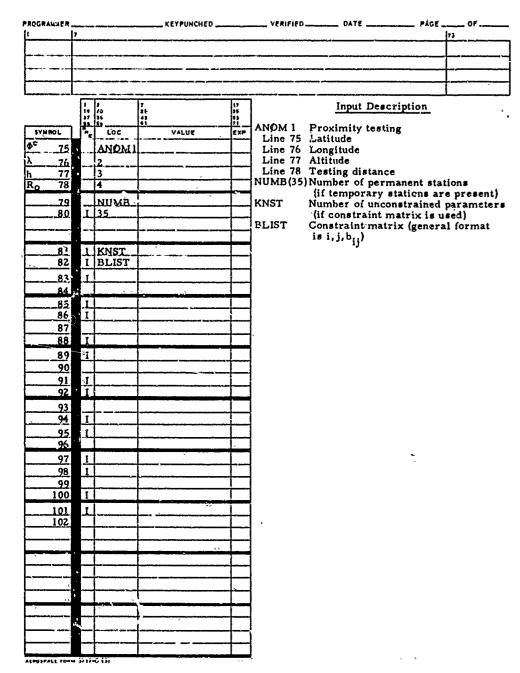


Figure 5-5. TRACE-D Tracking Input Load Sheet (Concluded)

The input initial conditions (IC) for Satellites 3 to 6 are the same as those noted above except that the symbol SAT2 is replaced by SAT3, SAT4, SAT5, and SAT6 as appropriate.

Lines 15 through 27: Initial-Condition and Differential Equation Parameter Specification Boxes

			-		_	_		_	-		_	_	
15	D.	CPRAM	2	x	x	x	X	x	x				,
16	D	DPRAM	x		L		L						
17	D	3	L	L			L						
18	D	5			٠,								
19	D	7					Ĺ						
20	D	9		L	L	L	Ĺ	Ĺ	L				
21	D	PSATE		L			L	L					
22	D	PSAT3											
23	D	PSAT4											
24	D	PSAT5				Ŀ			<u> </u>	L			
25	D	PSAT6											
. 26	D	KPRAM				Ĩ,				Ĺ_			
27	D	3											

An X entered in any CPRAM, DPRAM, PSAT, or KPRAM character position causes the corresponding parameter to be differentially corrected. The ordering of entries in the CPRAM, DPRAM, PSAT, and KPRAM character position boxes is as follows:

a. <u>CPRAM (Initial Condition Parameters for Satellite 1)</u>
(Line 15)

The first position specifies which one of these types of initial conditions is applicable, and succeeding positions indicate the particular parameters that are desired in each case. Ordering of parameter entries for IC Types 1, 2, and 3 is as previously shown in Figure 5-7.

b. DPRAM (Differential Equation Parameters)
(Lines 16 through 20)

The ordering of DPRAM differential equation parameter entries is as previously shown in Figure 5-4. However, in this application the T₁ and T₂ parameters are associated with Satellite 1 only.

Coefficient Parameters for Satellites 2 - 6)
(Lines 21 through 25)

The ordering of PSAT IC and drag parameter entries for Satellites 2 through 6 is shown in Figure 5-6.

PSAT2	a ₂	δ ₂	β2	A ₂	r ₂	v ₂	t _o 2	Drag ₂
PSAT3	a. ₃	δ3	β ₃	A ₃	r ₃	v ₃	t03.	Drag ₃
PSAT4	a ₄	δ4	$\beta_4$	A ₄	r ₄	v ₄	t04	Drag ₄
PSAT5	a ₅	δ ₅	β ₅	A 5	r ₅	¥5	t ₀₅	Drag ₅
PSAT6	a ₆	δ ₆	β ₆	A 6	<b>*</b> 6	v ₆	't _{o6}	Drag ₆

Figure 5-6. Ordering of PSAT Initial Condition/ Drag Parameter Entries

It is important to note that only IC Type 2 may be specified for Satellites 2 through 6.

d. KPRAM (Orbit Adjust Parameters for Satellite 1)
(Lines 26 and 27)

Ordering of KPRAM orbit adjust parameters is as previously shown in Figure 5-4. It should be noted that the orbit adjusts are for Satellite 1 only.

Sixty trajectory parameters is the maximum number which may be selected for simultaneous solution.

Lines 28 through 40: Bounds

28	BNDS	.5	
28 29	2	.5	
. 30	3	.1	
. 31	4	. 5	
32	5	1000.	
33	6	5	
34	7	. 05	
35	8	_	
36	9	,	
37	10		
38	11		
[~] 39	12		
40	13		

A bound must be entered for each parameter selected. These bound entries must be in the same sequence as the parameters. For each iteration of the differential correction process, the change in each parameter is less in absolute value than the corresponding bound if that bound is positive, zero if the corresponding bound is zero, or unrestricted if the corresponding bound is negative.

Lines 41 through 50: Radar Parameter Specification

41	. 1	ARAPAR	05,99	Ì
			,	
42	Į,	01.01	BNLLAT	
43		03,01	.01	
44		04,01		
			,	
45	Ι	01.02	CK24RBIAS	
46		03,02	500.	
4.7		và ûz	750.	
48	41	01.03	HU TBIAS	
49		03,03	.001	
50		04,03	.0035	

Line 41 indicates that the data listed subsequent to RAPAR on the load sheet will be input into a  $5 \times 99$  matrix array which has been preset to zero. The columns of this array correspond to parameters, and the rows correspond to parameter identification (Positions 1 and 2), bounds (Position 3), and bias estimates (Position 4) respectively. Row 5 is currently not used.

Lines 42 through 44 specify the first applicable radar parameter. Line 42 contains the station name (Fositions 1 and 2), pass identification (Positions 3 and 4), and parameter name (Positions 5 through 10). Lines 43 and 44 contain the bound and initial value, respectively, in feet, degrees, and minutes except for R, P, and Q, which are in feet per second. If the parameter is station latitude, longitude, or altitude, the initial value is taken from the station location card.

If the pass identification character position is left blank, all data with the indicated station name will be used to correct the parameter. If the pass identification is not omitted, only data that are identified by both the indicated station name and indicated pass identification will be used to correct the parameter. If the radar parameter specified is station latitude, longitude, or altitude, the pass identification is ignored and all data with the station name are used for the parameter correction.

Lines 45 through 47 and Lines 48 through 50 specify the second and third radar parameters respectively. Station names, pass identifications, parameter names, bounds, and initial values are treated in the same manner as the inputs in Lines 42 through 44 described above. Additional cards may be added in cases where more than three radar parameters are involved. Available radar parameters are listed in Table 5-1.

Note that the total number of parameters which may be selected for simulataneous solution must be less than one hundred.

Table 5-1. Available Radar Parameters

Parameter	Symbol
Station latitude	LAT
Station longitude	LONG
Station altitude	ALT
Pime bias	TBIAS
Range bias	RBIAS
Azimuth bias	ABIAS
Elevation bias	EBIAS
Topocentric right ascension bias	RTBIAS
Topocentric declination bias	DTBIAS
Topocentric hour angle bias	HABIAS
Geocentric right ascension bias	RGBIAS
Geocentric declination bias	DGBIAS
Argument of latitude (u) bias	UBIAS
Cross plane (v) bias	VBIAS
Height bias	HBIAS
x bias	XBIAS
<b>♦</b> bias	YBIAS
ž bias	ZBIAS
P bias	PBIAS
Q bias	QBIAS
Range-rate bias	RDBIAS
P bias	PDBIAS
Q bias	QDBIAS
Range scale factor (KR)	KR
Range-rate scale factor (KD)	KD

Lines 51 through 62: Observation Sigmas

51		SIGMA	100.
52		2	.5
53		3	.5
54		4	1000.
55		5	200.
_ 56		6	300
57	I	ISIG	1
58	I	2	2
59	I	3	3
60	r	4	113
61	I	5	114
62	I	6	115

Lines 51 through 56 contain the observation data weighting factors. For each SIGMA entry, a corresponding entry defining the sigma set and data type appears in ISIG Lines 57 through 62. The ISIG entries are of the form 100I + K, where I is the observation set number and K is the data type. Ten sets, corresponding to  $I = 0, 1, 2, \ldots, 9$ , may be entered. This selected value of I is the same as the entry in Column 5 of the station location card. The data type, K, must be one of those listed in Table 5-2.

Table 5-2. Data Types for ISIG Entries

Data Type (K)	· Data Description	Symbol
1	Range	.R
2	Azimuth	Ä
3	Elevation	· E
. 4	Topocentric right ascension	$^{lpha_{ m T}}$
5	Topocentric declination	$\delta_{\mathbf{T}}^{\mathbf{T}}$
6	Topocentric hour angle	AFI
7	Geocentric right ascension	ag
8	Geocentric declination	δg
10	Argument of latitude	11
11	Cross plane	'♥
12	Height	h
13	Ŷ	<b>x</b>
14	ŷ	ŷ
15	<b>☆</b>	Ž
17	Range difference	, P
18	Range difference	, Ω
19	Range rate	Ŕ
Z0	k difference	. <b>p</b>
21	R difference	Q

Line 63: Maximum Number of Iterations

63	T	MAXIT 4	1	
( 05	_	TATTATA		

If the differential correction process has not converged at the end of MAXIT iterations, the process will be terminated.

Line 64 through 66: Residual Editing

		ويونيك ويومون كالمحدد والأكان
64	CEDIT	3
65	2	. 9
66	3	.1

If CEDIT is zero, no editing is done. If CEDIT is non-zero, residuals will be edited in accordance with the following:

- a. CEDIT < 0 Residuals greater than (input sigma × |CEDIT|) will be discarded.
- b. CEDIT > 0 Residuals greater than (statistical sigma from the previous iteration × CEDIT) will be discarded. No editing is done on Iteration 1. Sigmas are computed for the first five data types encountered for each station.

Line 65 represents a scale factor such that if CEDIT (2) is non-zero, CEDIT is replaced by (CEDIT × CEDIT (2)) at the end of each iteration. If CEDIT (2) is zero, CEDIT is not modified.

Line 66 is a special option wherein if CEDIT (3) is non-zero, Iteration 1 will be repeated with editing performed with the sigmas computed during the first pass through Iteration 1. This will allow editing to be done on all iterations with computed sigmas.

Sigmas (rms) for the first five data types for each station are computed and printed at the end of each iteration regardless of the residuals-editing option selected.

Lines 67 and 68: Elevation-Angle Refraction Index Table

67	REFR	\	
68	2	4.0	-6

A table of refraction indices  $\eta_i$ , which may contain up to ten values, may be input starting at REFR. The entry used to compute refraction corrections for radar elevation observations is determined by the type number contained in Column 6 of the corresponding station location card. A zero in Column 6 causes the entry at REFR to be used, a 1 in Column 6 causes the entry at REFR + 1 to be used, etc.

If the table contains no entries, the value  $312.0 \times 10^{-6}$ , which is built in at location REFR, will be used to compute refraction corrections for all data whose station location cards contain zero in Column 6. All other positions of the table are assembled as zeros.

Line 69: Range Refraction Correction

1 69	IRREPORT I I

Refraction corrections to all range observations will be computed and applied if RREFC is non-zero.

Line 70: Propagation Time Correction

70	SLT	-2820, 1763	

The velocity to be used in calculating the observation time correction due to propagation time is entered at SLT in units of earth radii per minute. In the absence of an entry, no correction will be applied. If an entry is present the correction will be applied to times associated with R, A, E,  $\dot{R}$ , h, P, Q,  $\dot{P}$  and  $\dot{Q}$  data only.

Lines 71 and 72: Data-Tape Options

71	I	IBCDI	6	
72	I	IBINI	1	

If the radar observation and station location information is to be input via a BCD tape other than the A3 normal FORTRAN system input tape, the tape number must be specified at IBCDI. If a binary tape containing compacted radar data produced by a previous run is to be input, IBINI must be non-zero and the tape must be mounted on Logical Unit B5.

Lines 73 and 74: True Equinox Correction

73	DAFLG	004	
74	2		

An additive factor may be applied to the computed right ascension of Greenwich at midnight of epoch day by entering the appropriate value in units of degrees at DALFG for Vehicle 1, at DAFLG(2) for Vehicle 2, etc. This entry usually is used to correct from mean to true equinox reference coordinates.

Lines 75 through 78: Proximity Indicator

Φ [*]	75	ANO	м1		
λ	76	i	2		
h	77		3		
$K_0$	78		4		

During an orbit determination run, an indicator may be obtained whenever the trajectory passes within a given distance (range) of a point on the surface of the earth by input of geodetic latitude (deg), east longitude (deg), and altitude (n mi) of the point at ANOM1 and the succeeding two positions and of the testing distance (the range from the point to the vehicle) at ANOM1(4). Testing and printing is done in the FITA link. Up to three such sets may be input at ANOM1, ANOM2, and ANOM3.

Lines 79 and 80: Number of Permanent Stations

79		NUMB	
80	I	35	30

NUMB(35) must be used whenever the temporary station option is exercised (see Section 5.1.3.3.2). If all stations are to be handled as temporary, a negative entry at NUMB(35) is required. If some stations are to be permanent (locations held in core while all data are processed), the number of permanent stations must be entered at NUMB (35).

Line 81 and Subsequent: Constraint Matrix

	81		I	KNST	4
	82		I	BLIST	1
	83		I		1
p11	84				1
-	85		I		2
	86.		Ι		2
b22	87				1
	88		I		3
<u> </u>	89		I		3
b33	90				1
	91		I		4
	92		I		4
b44	93				1
	94	,	I		5
	95	ŀ	I		1
b51	96				-1
	97 98		I		6 2
			I		
b62	99				. 5
	100		Ī		5
	101		I		5
c ₅₁	102				6
	103		I I		5
	104		I		5
	105				.1

If it is assumed that n parameters are to be solved for  $(p_1, p_2, \ldots, p_n) = p$ , the ordering of the  $p_1$  corresponds to the order of the X's for the CPRAM, DPRAM, and KPRAM and the RAPAR arrays. Further assuming that these parameters are to be subjected to m linear constraints, which, for example for n = 6 and m = 2 might be  $p_1 + p_5 = 6$ ,  $p_2 - 2p_6 = 0$ , KNST would be equal to (n - m) = 4, or the number of effective (unconstrained) parameters.

NUMB(35) must be used whenever the temporary station option is exercised (see Section 5.1.3.3.2). If all stations are to be handled as temporary, a negative entry at NUMB(35) is required. If some stations are to be permanent (locations held in core while all data are processed), the number of permanent stations must be entered at NUMB (35).

Line 81 and Subsequent: Constraint Matrix

				_	
	81		I	KNST	4
	82		I	BLIST	1
	83		I		1
bll	84				1
	85	***	I		2
	86.		I		2
b ₂₂	87				1
	88		I		3
	89		I		3
b33	90				1
	91		I		4
	92	, [	I		4
b ₄₄	93				1
	94	ľ	Ţ		5
	95		I		1
b ₅₁	96				-1
	97		I		6
	97 98		I		6 2
b62	99				. 5
	100		I		5
	101 102		I		5
c ₅₁					5 6
	103		I		5
	104		Ι		5
	105				_1

If it is assumed that n parameters are to be solved for  $(p_1, p_2, \ldots, p_n) = p$ , the ordering of the  $p_1$  corresponds to the order of the X's for the CPRAM, DPRAM, and KPRAM and the RAPAR arrays. Further assuming that these parameters are to be subjected to m linear constraints, which, for example for n = 6 and m = 2 might be  $p_1 + p_5 = 6$ ,  $p_2 - 2p_6 = 0$ , KNST would be equal to (n - m) = 4, or the number of effective (unconstrained) parameters.

observations are to be processed. This information will previously have been accumulated on the station-card load sheet illustrated in Figure 5-7.

# 5.1.3.3.1 Station Card Format

For stations associated exclusively with geocentric or with vehicle-centered observations, only the information in Columns 1 through 6 of Figure 5-7 must be entered. Up to 100 stations may be entered at any one time (see Section 5.1.3.3.2). The last station card must be followed by a card carrying the designation TS in Columns 1 and 2. Specific information categories contained in the station-card load sheet are:

- a. Columns 1 and 2(ST): Station identification symbol. No two stations may be identified by the same symbol or any one station by the symbol TS.
- b. Column 5: Sigma index identifying observation-sigma set to be applied to data from corresponding station. The sets of sigmas are input with the FINP data (see Lines 51 through 62, SIGMA/ISIG).
- c. Column 6: Type of refractivity correction to be used for elevation readings from this station. Refractivities are numbered in their input order within the FINP Data (see Line 67, REFR).
- d. Columns 9 through 17: North latitude of station in degrees
- e. Columns 19 through 27: East longitude of station in degrees
- f. Columns 29 through 36: Altitude of station in feet
- g. Columns 38/39 and 41/42: If a station reports P, Q or P, Q data, Columns 38/39 and 41/42 contain the two letter symbols for the associated station(s) of the tracking configuration. Each such associated station must be represented by a separate station card, but it is not necessary for Columns 38/39 and 41/42 to be filled out on the latter.

# 5.1.3.3.2 Temporary Station Option

The 100 allowable station locations may be classified either as permanent or as temporary stations. Permanent station locations are input in the manner outlined in Section 5.1.3.3.1 and are held in core at all times during a fit. Temporary station locations are input with the data to which they

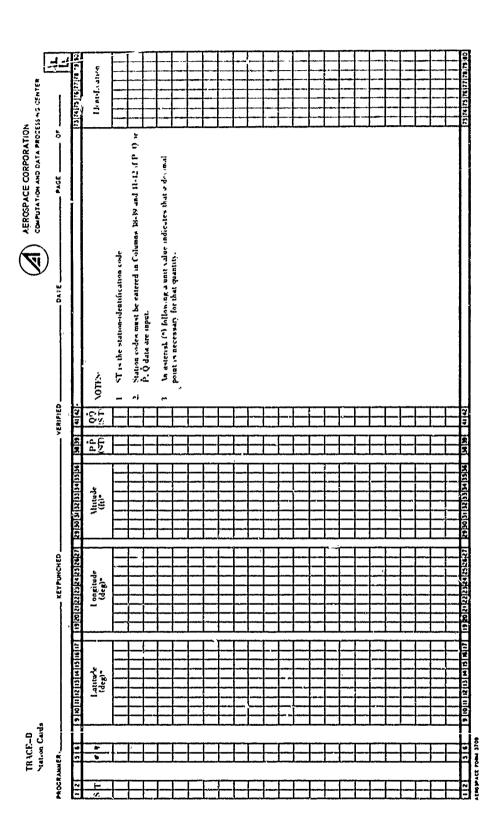


Figure 5-7. Station-Card Specification Load Sheet

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correspond, subject to the flocking restrictions subsequently described. The number of permanent stations, which remains constant throughout the run, is input at NUMB(35) in the FINP data. The number of temporary stations may vary from flock to flock but the total number of permanent plus temporary stations must not exceed 100 for any flock. Radar parameters may be determined for permanent stations only (see Section 5. 2. 2. 6 for the particular deck setup required).

#### 5.1.3.4 Observation Data Cards

Observations are input by means of observation cards punched with information previously accumulated on the observation-data specification load sheet illustrated in Figure 5-8. Symbols identifying information categories noted on this load sheet form are:

- a. <u>Columns 1 and 2 (ST)</u>: Station identification symbol, which must correspond to a station-location card.
- b. Columns 3 and 4 (PS): Pass identification (optional)
- c. Columns 6 through 23: MO, DAY, HR, MIN, and SEC entries indicate the date and time (GMT) of corresponding observations
- d. Column 24: Observation-set number
- e. Column 72: Card number indicating observations, variances, or covariances

Contents of the various observation-load-sheet information fields are itemized in Table 5-3, wherein input units are feet, degrees, and seconds.

The last observation card must be followed by a card carrying the symbol TR in Columns 1 and 2. The TR card must be followed by an END card.

### 5.1.3.5 Flocking Option

For numbers of observations greater than 200, the data must be divided into "flocks." Flocks may be of arbitrary size, but also must not include more than 200 observations each. A control card with the letters TF in Columns 1 and 2 is used to signal the end of a flock, and any number of these may be placed among the observation cards. However, the last flock must be terminated by a TR card. The only restriction imposed is that the obser-

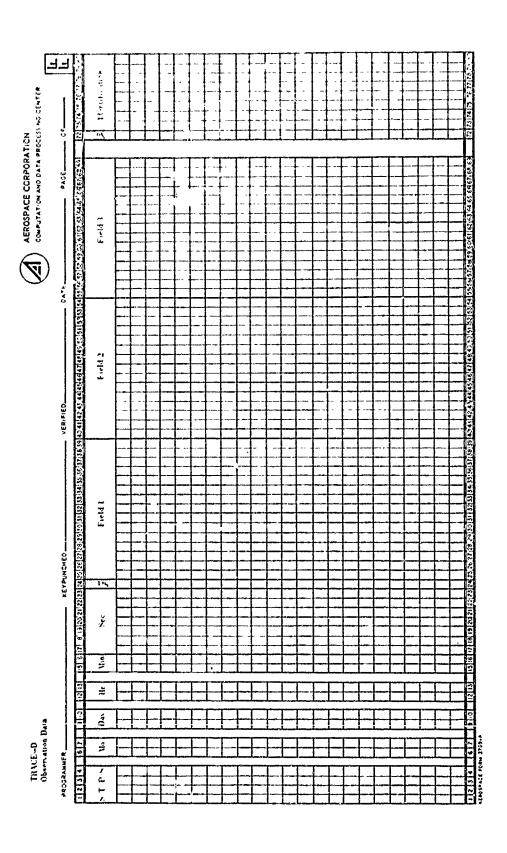


Figure 5-8. Observation Data Specification Load Sheet

Table 5-3. Information Accumulated on Observation Load Sheet

<del></del>		y			·	·	
Field 3	Elevation(E) Variance(E) Covariance(A, E)	Topocentric hour angle (HA) Variance (HA) Covariance ( ⁵ _T , HA)		Altitude(h) Variance(h) Covariance(v, h)	$\overset{ extstyle  imes}{ extstyle  exts$	Range difference(Q) Variance(Q) Covariance(P,Q)	Range rate difference(Q) Variance(Q) Covariance(P,Q)
Field 2	Azimuth (A) Variance (A) Covariance (R, E)	Topocentric declination( $\delta_{ m T}$ ) Variance( $\delta_{ m T}$ )	Geocentric declination( $^{\delta}_{g}$ ) Variance( $^{\delta}_{g}$ )	Cross plane(v) Variance(v) Covariance(u, r)	$\hat{y}$ Variance $(\hat{y})$ Covariance $(\hat{x}, \hat{z})$	Range difference(P) Variance(P) Covariance(R, Q)	Range rate difference(P) Variance(P) Covariance(R, Q)
Field l	Slant range(R) Variance(R) Covariance(R, A)	Topocentric right ascension( $a_T$ ) Variance( $a_T$ ) Covariance $a_T$ , $\delta_T$ )	Geocentric right ascension( $\alpha$ ) Variance ( $\alpha$ ) Covariance $\beta$	Argument of latitude(u) Variance(u) Covariance(u, v)	$\hat{X}$ Variance( $\hat{X}$ ) Covariance( $X$ , $\hat{Y}$ )	Slant range(R) Variance(R) Covariance(R, P)	Range rate(Ř) Variance(Ř) Covariance(Ř, Þ)
Observation Card Type (Column 72)	0 3	0 1 2	0 2	0 1 2 2	0 2 2	0 1 2	21.0
Observation Set Number (Column 24)	7 1 7	0 00	ო ოო	ক কক	വവ	9 99	

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vations must be in partial chronological order such that every data time of a given flock is later than all times in all previous flocks.

The mechanics of this option involve use of TRAIN, which causes the observations to be read, sorted, processed, and written on tape one flock at a time. If more than one flock is present, the differential correction process first reads the tape and then computes residuals and the normal matrix for one flock at a time.

#### 5.1.3.6 Multiple Vehicle Option

If data from more than one vehicle are to be used, the Vehicle-1 data are set up in the manner outlined in Sections 5.1.3.3 and 5.1.3.5, except that the TR card must be replaced by a TT card. The data for Vehicle 2 are then similarly arranged. If Vehicle 2 is the last vehicle, corresponding data are followed by a TR card: if it is not the last vehicle, data are followed by a TT card. Data for Vehicles 3 through 6, as applicable, are added in the same manner. A TR card rather than a TT card must follow the data corresponding to the last vehicle, and an END card must follow the TR card.

#### 5.1.3.7 Correlated Observations

Observations may be weighted by means of the covariance matrix as well as by the usual normalization based on the a priori standard deviation. The allowable covariance inputs are shown in Table 5-3.

The type of information content carried by each observation data card is identified by the 0, 1, or 2 symbol contained in Column 72 of the observation, variance, and covariance cards, respectively. Columns 1 through 24 of all three cards must be identical, and all cards associated with the same observation time must be input in the same flock.

The only covariances accepted are between observations of the same type number which occur at the same time. For example, in the case of an  $\hat{x}$  (Type 5) observation at time t, the only quantities with which it could be correlated would be  $\hat{y}$  at time t,  $\hat{z}$  at time t, or both.

### 5.1.4 Data Generation

Detailed description of the TRACE-D data generation input load sheet shown in Figure 5-9 is presented in Sections 5.1.4.1 and 5.1.4.2.

### 5.1.4.1 Required Input

The only required input in addition to the basic data are the station location data and the data tabulated on Data-Generation Specification. Load Sheets I and II as outlined in Sections 5.1.4.3 through 5.1.3.5.

## 5.1.4.2 Optional Input

# 5.1.4.2.1 Group 1

Line 2: Output Options

1	IFLAG	
2 I	6	1

If IFLAG(6) = 0, all generated data are printed. If IFLAG(6) = 1, rise, maximum elevation, and set times only are printed and the Data-Generation Specification Load Sheet II is not necessary except for listing of a card carrying TR in Columns 1 and 2.

Line 3: Order of Output

3	I 14	1
		4

If IFLAG(14) = 0, data are generated in time sequence until the available core space (bucket) is full. This output is then separated and printed by station in the same sequence as that of the input station cards. Further data are then generated until the bucket again is full, and the sort/print cycle is repeated. If IFLAG(14) = 1, data are printed as they are generated (i.e., in time sequence).

Figure 5-9. TRACE-D Data-Generation Input Load Sheet

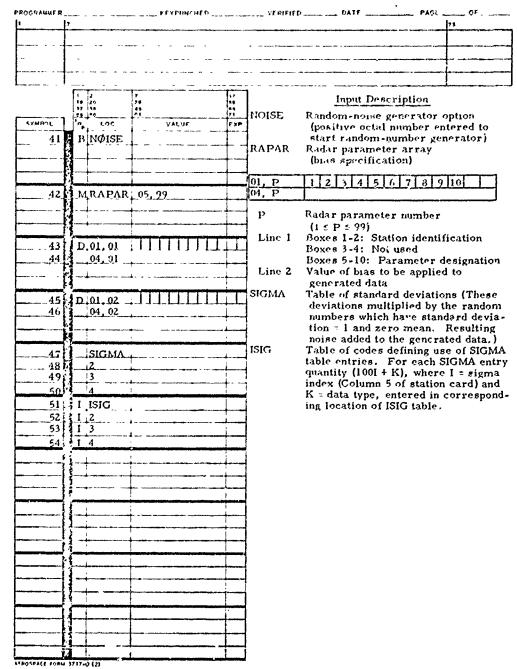


Figure 5-9. TRACE-D Data-Generation Input Load Sheet (Continued)

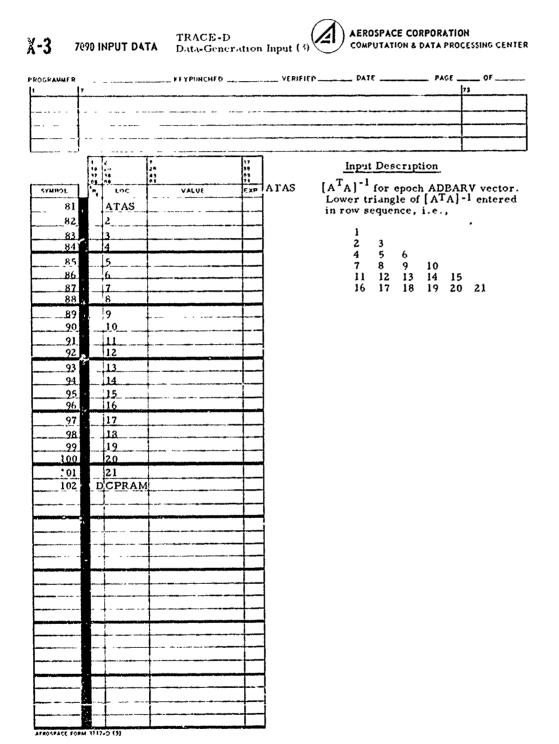


Figure 5-9. TRACE-D Data-Generation Input Load Sheet (Concluded)

## Line 4: Observation Tape Generation

4 I ETAPE 6

If ETAPE is non-zero, a BCD radar observation tape will be generated on the logical tape unit entered at ETAPE. The tape format will be the same as that of the tracking input data. including station locations and TF and TR cards.

# Line 5: Refractivity

<b>5</b>	REÈR	1 1
3	Y-C-C-L	 

The computed elevation, E, is altered to account for refraction, using either

$$E' = E + \eta_{si} \cot E$$

if  $E \ge 0$ . 1 radian, or

$$E' = E + \frac{1}{1000} \frac{\eta_{si} \times 10^6}{12 + 1000E} - \frac{30}{6 + 1000E}$$

if E < 0.1 radian and  $\eta_{si} \neq 0$ .

REFR contains the  $\eta_{si}$  term, wherein i = 0, 1, 2, ... 9. The appropriate value of i is entered on the station card of Column 6. Nominally  $\eta_{so}$  =  $3.12 \times 10^{-6}$ . Rise, set, and maximum elevation values are determined from the geometric E which represents the elevation before refraction correction is applied. Additional cards may be inserted at this location if necessary.

Lines 6 through 8: Vehicle Attitude Specification

$\theta_{\mathbf{v}}$	6	YAW	1.
$\theta_{D}$	7	PITCH	90.
$\theta_{\mathbf{r}}$	8	RØLL	180.

Vehicle attitude may be specified by inputting yaw, pitch, and roll angles in degrees in the manner shown above. These entries normally are introduced in conjunction with aspect angle computations.

Lines 9 through 24: Vehicle Attitude Manuevers

9	YAW	
10	811	1.
11	812	120.
12	813	.01
13	814	.1
14	815	0
15	816	120.
16	817	121.
17	818	~.9
18	819	-9.0
	<u> </u>	
19	820	0
19	820	0
19 20	820 821	0 1420.
19 20 21	820 821 822	0 1420. 1420.5

The time history of vehicle attitude maneuvers may be specified by means of a table entered at YAW(811). The format of this table, which is used in connection with generation of radar aspect angles and may consist of up to three sets of five entries each, is itemized in Table 5-4.

Table 5-4. YAW(811) Table Format

Entry	Description
YAW(811)	Start time in minutes from epoch for first set of angular rates
YAW(812)	Stop time in minutes from epoch for first set of angular rates
YAW(813)	Yaw rate in degrees per minute
YAW(814)	Pitch rate in degrees per minute
YAW(815)	Roll rate in degrees per minute
YAW(816)	Start time in minutes from epoch for second set of angular rates
YAW(817)	Stop time in minutes from epoch for second set of angular rates
YAW(818)	Yaw rate in degrées per minute
etc.	etc.

The yaw-, pitch-, and roll-angle values that make up these input sets of angular rates are assumed to change at the rate given over the time interval defined by the start and stop times. Nominal orientation is zero yaw, pitch, and roll, which corresponds to the condition where the vehicle body axis is normal to the geocentric radius vector, the nose of the vehicle is in the in-track direction, and the top of the vehicle is in the direction of the extended radius vector.

Vehicle attitude at time of epoch and for the case where the entries in Table 5-4 are all zero (i.e., when nothing is input) is assumed to be the attitude specified at YAW, PITCH, and ROLL. If gaps in the time entries of the table are present, the angles are held constant at the last computed values.

Lines 25 and 26: Trajectory Tape Unit

	25		IFLAG		
Γ	26	I	16	10	

The logical unit of a scratch tape to be used for the GAINA-generated trajectory should be input at IFLAG(16). An END card should follow the foregoing input.

# 5.1.4.2.2 Group 2

The data generation input deck contains two END cards. In the event the following Group 2 input is used, this deck must be placed between these two END cards (see Section 5.2.3).

Line 41: Noise Generator

				-								_
41 B	NØISE	3	7	7	7	7	7	7	7 7	7	7	1

If NOISE is non-zero (a positive octal number), normally distributed random noise with standard deviation and mean value specified by input at RAPAR is added to the generated data (see Section 5.1.4.2.2, Lines 42 through 46, RAPAR). The entry at NOISE is used to start the random-number generator.

Lines 42 through 46: Bias Specifications

42.	М	RAPAR	05, 99	-
<u>43</u>	Ď	01,01 04,01	HU ABIAS	
44		04.01	. 03:	
45	Đ.	01,02	AL HBIAS	
46		04.02	200.	

The RAPAR array (see Section 5.1.3.2) is used on data generation runs to indicate the stations for which biased data are to be generated and also as a means of entering the value of the bias.

Lines 47 through 54: Standard Deviations

47		SIGMA	200
48		2	.1
49		3	. 1
50		4	50.
51	I	ISIG	1
52	I	2	2
53	I	3	3
54	I	4	112

Standard deviations for the noise added to generated observations are entered via the SIGMA table. The usage of the SIGMA, ISIG, and station-card index numbers is the same as that previously described in connection with tracking input instructions (see Sections 5.1.3.2 and 5.1.3.3.1) In the example noted above, output R, A, and E data would contain noise with sigmas of 200 feet, 0.1 degree, and 0.1 degree, and with means of zero feet, 0.057 degree, and zero degrees respectively. Also, the input HU station card would carry a zero as the sigma index in Column 5. The AL station card would contain a 1 in Column 5, and the generated output data would contain noise with a 50-foot sigma and a 200-foot mean.

Lines 81 through 101: Orbit Covariance Matrix

81	ATAS	1.	~4
83	3	. 5	-7
86	6	2.	-2
c.			
9.0	10	4.	-2
95	15	2000.	
101	21	1.	

If observation uncertainties are to be calculated, a covariance matrix for the ADBARV elements at epoch must be input in lower triangular form at ATAS. The order of the elements is Row 1/Column 1 at ATAS, Row 2/Column 1 at ATAS(2), Row 2/Column 2 at ATAS(3), etc.

#### Line 102: Parameter Specification

# 102 D CPRAM 2 x x x x x x

If observation uncertainties are to be computed, the ADBARV parameters must be selected in accordance with the usage described in Section 5.1.3.2. However, only the ADBARV parameters may be indicated since their associated covariance matrix  $(A^TA)^{-1}$  is the only one which may be used in computing the uncertainties.

### 5.1.4.3 Station Cards

Data-generation station card format and usage is the same as that previously outlined in connection with the tracking function (see Section 5.1.3.3.1) except that, in the case of a data generation run, the station cards follow the second END card and are in turn followed by a TS card.

#### 5.1.4.4 Data-generation Specification Load Sheet I Input

Specific information categories contained in Data-Generation Specification Load Sheet I as shown in Figure 5-10 are:

- a. Columns 1-2 (ST): Station identification symbol. Must correspond to symbol letters appearing on station cards for that station.
- b. Columns 9 through 16: Time interval in seconds at which data for a given station are to be generated and testing interval for rise/set only option.
- c. Columns 18 through 23: Minimum elevation at which vehicle is visible.
- d. Columns 25 through 30: Maximum elevation at which vehicle is visible. Zero value set to 90 degrees.

2 Start and New times are from midnight of epoch H Visit time in secon epich is defined as In asteriak (*)
following a unit
value rodi atea
jbat a dei enal
paint in necessar
for that quantity AEROSPACE CORPORATION
COMPUTATION AND DATA PROCESSING CENTER 1 N in the statement 1 00 1 7.1107 PAGE _ [60]60] [63]66] [66]63] Note I ame 51[52] | | | | | | | | | | | | | | | | Mart Time VERIFIED ... Maximum Range (a mt) 25/26/27/26/29/3/ Maximum Flevation (deg)* - KEY PUNCHED -10 119 20[21]22[23 Vinimum Elevation (deg)* Interval TRACE-D Data Generation 1 PROGRAMMER

Figure 5-10. Data-Generation Specification Load Sheet I

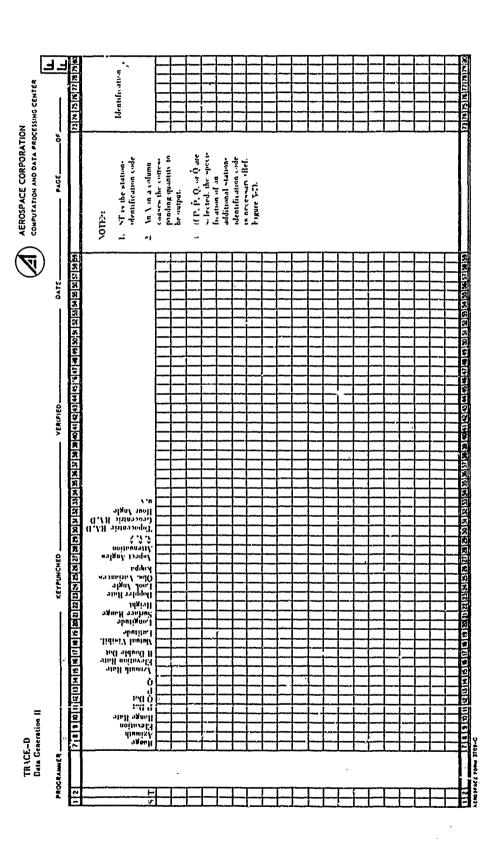
- e. Columns 32 through 40: Maximum range in nautical miles to which vehicle is visible. Zero value causes this test to be ignored.
- f. Columns 51 through 58: Start time from midnight of start date. Zero value implies epoch is start time (Columns 51-52, 54-55, and 57-58, days, hours, and minutes, respectively.)
- g. Columns 60 through 67: Stop time from midnight of start date (Columns 60-61, 63-64, and 66-67, days, hours, and minutes respectively).

The last card carrying Data-Generation Load Sheet I data must be followed by a card identified by the letters TR in Columns 1 and 2.

## 5.1.4.5 Data-Generation Specification Load Sheet II Input

Except for a TR card, Data-Generation Load Sheet II as shown in Figure 5-11 is not used for the rise/set only option. Specific information categories contained in Load Sheet II are as follows:

- a. Columns 1-2 (ST): Station identification symbol. Must correspond to symbol letters appearing on station cards for that station.
- b. Columns 7 through 33: An X entry in the appropriate column will initiate output of quantities itemized in Table 5-5.



**!** 

Figure 5-11. Data-Generation Specification Load Sheet II

Table 5-5. Output Quantities Corresponding to Columns 7 Through 33 of Data-Generation Specification Load Sheet II

Column	Output Quantity	Unit
7*	Range	n mi (ft on ETAPE)
8*	Azimuth	deg
9*	Elevation	deg
10*	Range rate	ft/sec
11-14* .	P, Q, P, Q	ft/sec, ft
15	Azimuth rate	deg/min
16	Elevation rate	deg/min
17	Range acceleration	ft/sec ²
18	Mutual visibility (Output will be a list of numbers of stations visible at output time. Stations numbered in order of input on station cards. Number of stations, 8 maximum.)	
19	Geodetic latitude of vehicle	deg
20	Longitude of vehicle	deg
21	Surface range from station to subvehicle point	n mi
22*	Altitude of vehicle	n mi (ft on ETAPE)
23	Doppler rate	·
<b>24</b>	Look angle (Angle between a vehicle axis and the station/vehicle line of sight. The direction cosines of the vehicle axis in the basic inertial system must be entered in C(37), C(38), and C(39). These	deg

^{*}These quantities are output on ETAPE.

Table 5-5. Output Quantities Corresponding to Columns 7 Through 33 of Data-Generation Specification Load Sheet II (Continued)

Column	Output Quantity	Unit
	quantities may be input as constant or the user may provide a subroutine (FANG) to compute the direction cosines at each output point.)	
25	Observation uncertainties (If inverse ATA matrix for initial conditions is input at ATAS, the ADBARV elements are selected as parameters, and if an X is entered in Column 25, the [ATA]-1 is updated to observation times and the standard deviations in the quantities R, A, E, R, A, E are derived and printed. The uncertainties are only those due to the uncertainty in the ephemeris which is implied by the given [ATA]-1 for the epoch conditions.)	Same units as observa- tions
26	Angle kappa (K) (Angle between station line-of-sight and geocentric radius vectors.)	deg
27	Aspect angles (Angle 1 (Φ) is defined as the angle between the vehicle yaw axis and projection of the station line-of-sight vector in the roll plane. Angle 2 (θ) is defined as the angle between the vehicle roll axis and the line-of-sight vector to the station (See Section 5.1.4.2.1 for description of vehicle attitude-control options.)	deg
28	Signal attenuation = -40 log ₁₀ R, where R is slant range in feet	db
29*	x, y, 2  (Same rectangular earth-fixed (X through Greenwich) geocentric quantities accepted as Type 5 observations for orbit determination.)	n mi (ft on ETAPE)

^{*}These quantities are output on ETAPE

Table 5-5. Output Quantities Corresponding to Columns 7 Through 33 of Data-Generation Specification Load Sheet II (Concluded)

Column	Output Quantity	Unit
30*	Topocentric right ascension and declination	deg
31*	Geocentric right ascension and declinasion	deg
32*	Topocentric hour angle	deg
33*	Vehicle-centered argument of latitude and cross-plan angle	deg

^{*}These quantities are output on ETAPE

### 5.1.5 Residuals Analysis

Detailed description of the TRACE-D residuals analysis input load sheet shown in Figure 5-12 is presented in Sections 5.1.5.1 and 5.1.5.2.

### 5.1.5.1 Required Input

Line 1: Itinerary

אודו מ	1127 1 1
7 2 1/17 173	1 1 4 1

Residuals analysis runs normally require an Itinerary-127 sequence, which causes the TRACE-D program to carry out a l-iteration fit sequence and then to call the RESIDUE link. Since no differential correction is carried out, the only required FINP entries are the basic input and IFLAG(26). The optional tracking-run input items which apply to residuals analysis runs are listed in Section 5.1.5.2. For most runs, station cards and observation cards are required, with formats identical to those previously described in connection with tracking input instructions (see Sections 5.1.3.3.1 and 5.1.3.4).

Lines 2 and 3: Residuals Analysis Options

2		IFLAG	
3	I	26	

IFLAG(26) selects the particular function to be performed by the RESIDUE link. Options are as follows:

- sponding to the given ephemeris (FITA output tape); compute the difference with the measured observations. (B5 tape); resolve the residuals into radial, in-track, and crosstrack components; compute time residuals; and accumulate a statistical summary by station and data type.
- b. IFLAG(26) = 2 TRACE-D will accomplish IFLAG(26) functions noted in Item a. above and also will compute the difference from the mean for each of the resolved residual components.

  This option requires an entry to be input at NUMB(38) (see Section 5.1.5.2).

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AEROSPACE CORPORATION TRACE-D Residuals-Analysis Input COMPUTATION & DATA PROCESSING CENTER **X-3** 7090 INPUT DATA KEYPUNCHED _ Input Description ITIN Itinerary (Itinerary 127 or 7 input)

| VXP | IFLAG(26)Option indicator
| 1: Standard functions VALUE DITIN 2: Standard functions plus computation IFLAG of differences from the mean Edit and punch option  $(\hat{x}, \hat{y}, \hat{z})$  data) (threshold magnitude of residual vector entered in feet) I 26 C C(29) NUMB(38) Scratch-tape unit designation (If IFLAG(26) = 2, logical unit = (9) NUMB entered.) I 43 NUMB(43) Data-tape designation (If computed observations are supplied by a I 44 I 45 second compacted data tape, logical unit = (16) entered) IELAG NUMB(44) Ephemeris input tape designation (If ephemeris in standard even-minute format is input, logical unit = (15) entered.) NUMB(45) Ephemeris input-tape designation
(If a second ephemeris is to be input for differencing, logical unit = (14) entered.) IFLAG(22) A and E residuals used for 0: vector resolution
A and E residuals not used for l: vector resolution

Figure 5-12. TRACE-D Residuals Analysis Input Load Sheet

It should be noted that residuals analysis processing is presently restricted to Data Set 1 (R,A,E), Set 2 ( $\alpha_T \delta_T$ ), and Set 5 ( $\hat{x}$ ,  $\hat{y}$ ,  $\hat{z}$ ).

### 5.1.5.2 Optional Input

Lines 4 and 5: Edit and Punch Option

4	С	
5	29	1

Type-5 observations  $(\hat{x}, \hat{y}, \hat{z})$  may be edited with respect to a specified ephemeris by entering a value at C(29). All sets of  $(\hat{x}, \hat{y}, \hat{z})$  which produce a value of  $R_T$  (the magnitude of the residual vector) less than the number entered at C(29) will be output on the punch tape in observation-card format.

Lines 6 and 7: Intermediate Tape Unit Specification

6		NUMB	
7	I	38	9

If residuals analysis Option 2 is selected, a logical tape unit for intermediate input/output must be specified at NUMB(38).

Line 8: Observation Differences

A	140	1 17	
8 <b>8 1</b> I	143	1 16.	1 1

If the logical number of a tape unit is entered at NUMB(43), RESIDUE will not expect a FITA ephemeris tape and will not compute observations, but will expect a second compacted data tape on the unit specified and will proceed as outlined for IFLAG(26) options (see Section 5.1.5.1).

Line 9: Ephemeric Input

9 <u>I</u>	44	15	

The FITA output tape, which usually supplies the ephemeris input to RESIDUE, may be replaced by a direct tape input from the logical unit specified at NUMB(44). The format must be the even-minute option of the binary trajectory tape format (see Appendix D).

# Line 10: Ephemeris Differences

10 T 45	
1 145	1 14

Two ephemeris tapes in the even-minute format (see Appendix D) may be differenced and the residuals may be processed in the same manner as  $\stackrel{\wedge}{x}$ ,  $\stackrel{\wedge}{y}$ ,  $\stackrel{\wedge}{z}$  data residuals. The logical designations of the units holding the two tapes are entered at NUMB (44) and NUMB(45). Ephemeris points are handled as computed and measured observations, respectively.

Since it is not necessary to utilize the observation processing or fit links for this particular option, a single Itinerary Number 7 may be used.

Lines 11 and 12: Range-Only Option

11	IFLAG	
12 I	22	1

If it is desired to use only range residuals for resolution into the orbit plane (i. e., A and E residuals are assumed to be zero), a non-zero entry should be made at IFLAG(22).

Additional optional input items which may be applicable to residuals analysis runs are the following:

- a. Initial conditions for multiple satellites
- Refraction corrections with respect to elevation and range
- c. Propagation-time correction
- d. Data-tape input options
- e. Proximity testing option
- f. Number of permanent stations

Instructions for use of optional input items are outlined in Section 5.1.3.2.

### 5.2 DATA-DECK ARRANGEMENT

This section describes the sequence of input data and control cards for the most frequent types of TRACE-D program runs. Notations relating to specific data-deck setups are given as appropriate for cases where known program restrictions may be troublesome and/or where tape input options are available. Each data control card is punched with its applicable letter symbol only (*DATA, END, TF, TS, TT, TR), starting in Column 1.

Cards preceding the *DATA card will be omitted in all but the first datadeck setups described in this section, wherein it also will be assumed that the constants deck is included in the FINP data.

### 5.2.1 Trajectory Only

### 5.2.1.1 Single Case

Except for control card changes (tape setup, priority, etc.), the portion through the constants of the trajectory card deck shown in Figure 5-13 normally remains unchanged from run to run. This remains true regardless of the itinerary sequence selected and is the basis for the term "basic running deck."

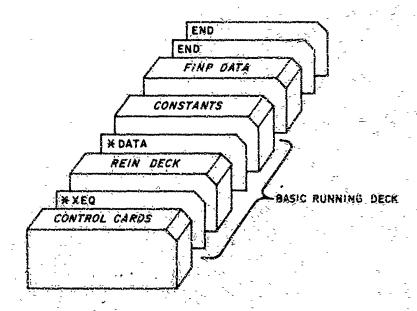


Figure 5-13. Deck Arrangement for Single Trajectory Case

Note:

The constants deck includes the standard INTEG and G (constants) entries as well as some inputs relating to other locations where standard values have been selected (see Appendix A for listing of standard constants deck currently in use).

### 5.2.1.2 Stacked Cases (Itinerary 333)

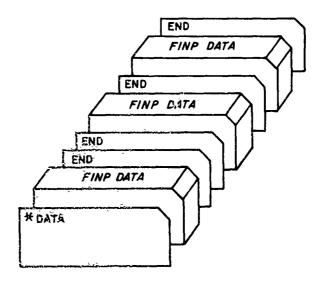


Figure 5-14. Deck Arrangement for Stacked Trajectory Cases

Note:

In general, FINP input remains unaltered, and any quantity which is not overwritten will be used on the subsequent case. Exceptions are ICTXP, CTAPE, and the PKICK, XKICK, THRST, and PRTIM tables. Entries at these locations must be loaded for each case.

### 5.2.2 Tracking

O

### 5.2.2.1 Basic Arrangement

Figure 5-15 shows the tracking input deck arrangement in terms of its major components. The detailed deck contents for various special tracking applications are described in Sections 5.2.2.2 through 5.2.2.7.

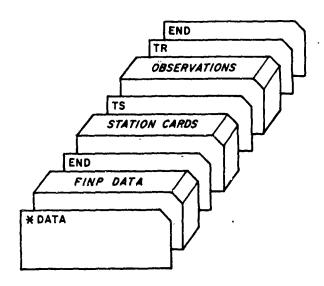


Figure 5-15. Deck Arrangement for Tracking Input

Note: The observation deck may include variance and covariance cards and/or temporary-station cards.

### 5.2.2.2 Flocked Observations

In the event that more than two hundred observations cards are present, the cards must be separated into flocks, as indicated in Figure 5-16. In Figures 5-17 through 5-21 it may be assumed that observation decks should be similarly flocked unless otherwise specified.

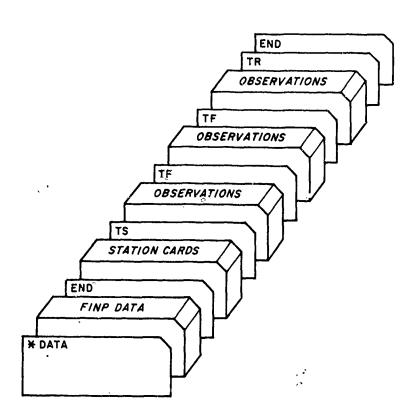


Figure 5-16. Deck Arrangement for Flocked Observations

Notes: 1. All observation times in any flock must be earlier than all observation times in all succeeding flocks.

2. The last flock is followed by TR and END cards only (no TF card)

### 5.2.2.3 BCD Input Observation Tape

If a BCD input observation tape is used, the station and observation card-decks are absent, as shown in Figure 5-17.

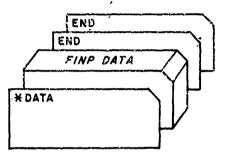


Figure 5-17. Deck Arrangement for Tracking Input with BCD Observation Tape

### Notes: 1. The FINP data includes an entry at IBCDI.

- 2. The ETAPE prepared by GAIN is suitable for input as a BCD observation tape,
- 3. The BCD input tape contains the card images of the station- and observation-card deck that would be used if those cards were input directly (See Section 5.2.2.2). The first image on the BCD tape is of the first station card and the last image is of a TR card.

### 5.2.2.4 Input Compacted Data Tape

If the tracking observations are input by means of a previously prepared compacted data tape, the tracking input deck will be structured as shown in Figure 5-18.

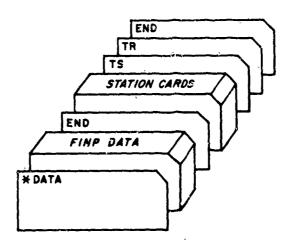


Figure 5-18. Deck Arrangement for Tracking Input with Compacted Data Tape

Notes: 1. The FINP data includes a non-zero entry at IBINI.

- 2. The input RAPAR matrix must be identical to the one entered on the run which generated the binary data tape.
- 3. The station-card deck must include all of the station cards in the same sequence as those appearing on the run which generated the binary data tape. The 2- and 4-column identifications also must be the same.

### 5.2.2.5 Multiple Vehicles

Observations for different vehicles are separated by TT cards, as shown in Figure 5-19.

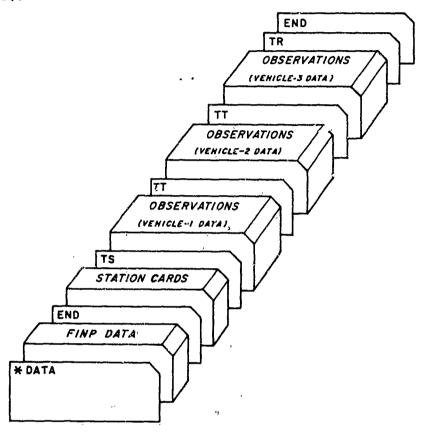


Figure 5-19. Deck Arrangement for Multiple-Vehicle Observations

- Notes: 1. The observation time sequence restriction for flocking applies only within the data for each vehicle.
  - 2. No TT card is required after the data for the last vehicle.
  - 3. If either of the tape input options is used, all observations for all vehicles must be on the tape.
  - 4. If flocking is used, the TF card should be omitted after the last flock for a vehicle (i.e., immediately before the TT card).
  - 5. RMS of residuals for temporary-station data may be obtained by setting NUMB(35) = 0 before the final END card.

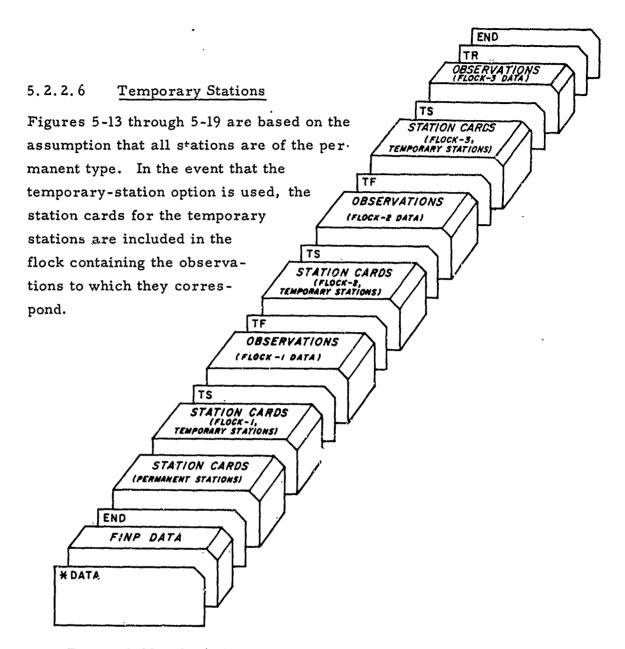


Figure 5-20. Deck Arrangement for Temporary-Station Option

Notes: 1. The number of flocks is not restricted.

- 2. The number of temporary stations in any flock plus the number of permanent stations may not exceed 100.
- 3. The FINP input includes the number of permanent stations entered at NUMB(35).
- 4. A TS card must be present in every flock if the temporarystation option is selected.

# 5.2.2.7 <u>Temporary Stations with Input</u> Compacted Data Tape

If a previously prepared binary compacted data tape is used, the tracking input deck will be structured as shown in Figure 5-21.

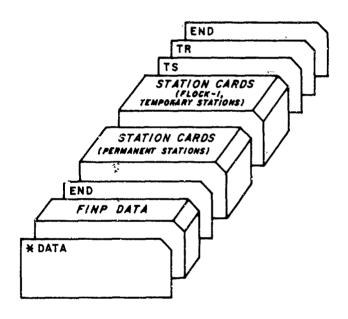


Figure 5-21. Deck Arrangement for Temporary-Station Option and Binary Compacted Input Tape

Note: Temporary-station cards for all flocks other than the first are contained on the binary compacted data tape.

### 5.2.3 Data Generation

### 5.2.3.1 Single Case

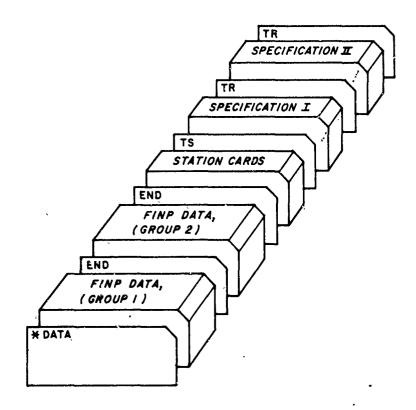


Figure 5-22. Deck Arrangement for Data Generation, Single Case

Note: For a rise/set only run, Specification II cards require only the station identification symbol.

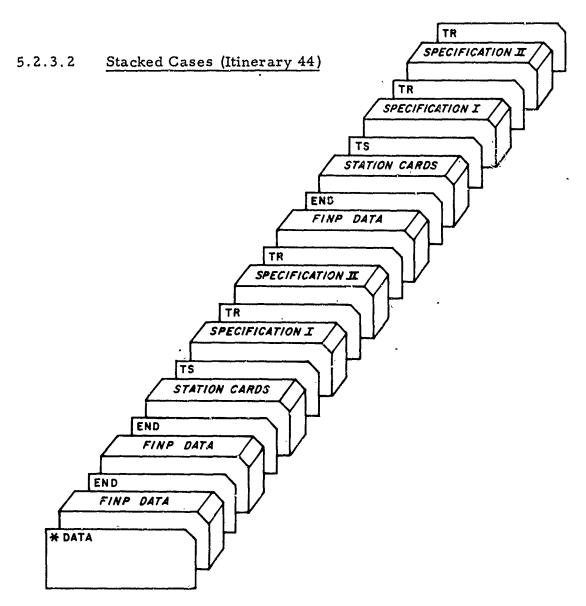


Figure 5-23. Deck Arrangement for Data Generation, Stacked Cases

- Notes: 1. The only input carried over from case to case is part of the FINP data (see Section 5.2.1.2). Complete station and data generation specification decks must be loaded for each case. The RAPAR agray must be reminput if used.
  - 2. Since the TRACE-D program rewinds the tape specified by ETAPE at the start of each case, use of this option with Itinerary 44 is not recommended.

### 5.2.4 Residuals Analysis

Deck configurations for residuals analysis runs in general are identical to corresponding tracking-run configurations due to the fact that the TRACE-D program processes the Itinerary 127 sequence as if it were a 1-iteration tracking run followed by a transfer to the RESIDUE link. The single exception to this rule is the setup for the Itinerary 7 ephemeris differencing run, shown in Figure 5-24.

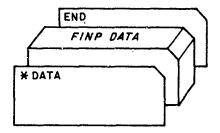


Figure 5-24. Deck Arrangement for Residuals-Analysis Ephemeris Tape Differencing

Note: On all residuals analysis runs, accumulated statistics (RMS, etc) are obtained for permanent stations only.

### 5.2.5 Mixed Itinerary Runs

#### 5.2.5,1 Itinerary 123

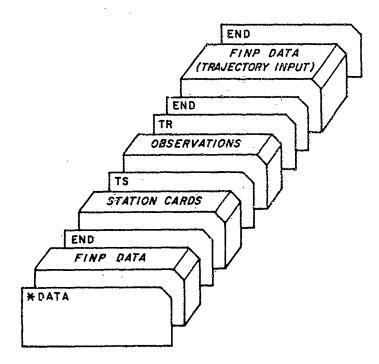


Figure 5-25. Deck Arrangement for Itinerary 123 Sequence

# Notes: 1. The maximum amount of FINP data should be input for the trajectory portion of the Itinerary 123 run. Except for constants and the required basic input. it should be assumed that none of the FINP input to the tracking run is carried over.

- 2. The ICTYP6 option may be used to obtain the ephemeris corresponding to the fit solution by loading the ICTYP6 entry with the trajectory input.
- 3. If PKICK parameters were determined in the fit, the solution values for the ΔV will be used for the trajectory portion of the run, but the times in the PKICK table must be reloaded with the trajectory input.

### 5.2.5.2 Itinerary 1243

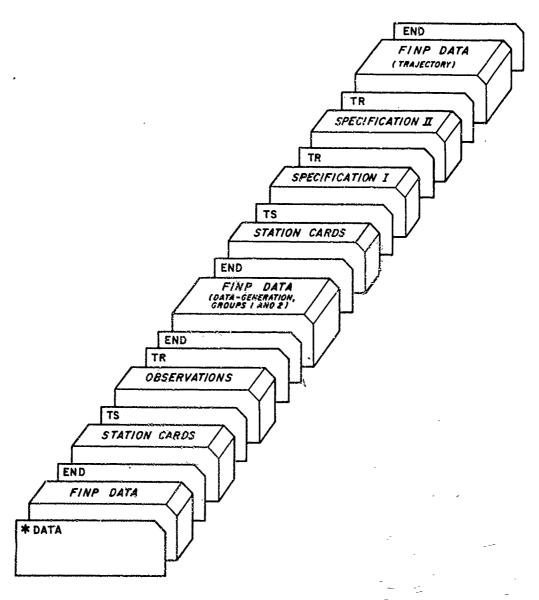


Figure 5-26. Deck Arrangement for Itinerary 1243 Sequence

Note: A data generation run (Itinerary 4) should not follow a trajectory run (Itinerary 3).

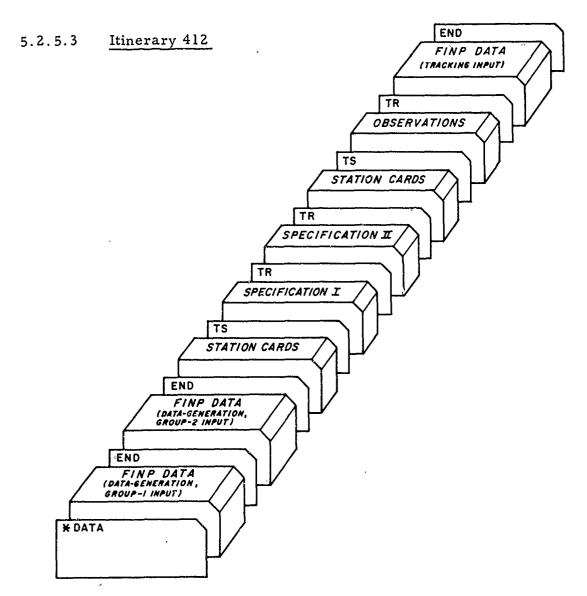


Figure 5-27. Deck Arrangement for Itinerary 412 Sequence

- Notes: 1. The Itinerary-412 sequence normally is used with the ETAPE option in order to generate and fit observation data.
  - 2. It should be noted that the FINP data for the tracking run is loaded after the observations. This is necessary because the CHAIN link is not called after the Itinerary 4 function. The TRAIN link, which reads station cards and observations, is called first, followed by the INITA link, which calls the FINP routine.

### 5.2.5.4 Itinerary 312

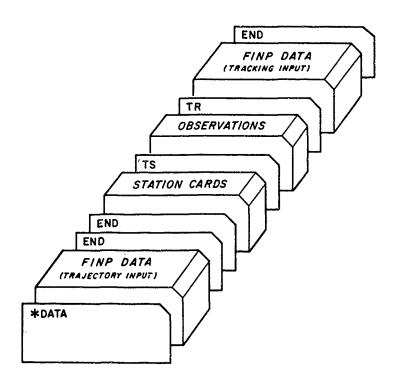


Figure 5-28. Deck Arrangement for Itinerary 312 Sequence

Note: 1. The Itinerary-312 sequence using the ICTYP5 feature may be used to shift epoch for the fit.

### 5.3 TAPE UNIT REQUIREMENTS

The information tabulated in Tables 5-6 through 5-9 delineates the tape unit requirements that are applicable to the four principal types of TRACE-D program runs. A summary of tape unit requirements by logical unit is given in Table 5-10.

These requirements are based on the assumption that a program tape mounted on Tape Unit 8 is used. However, if the program is loaded by cards, Tape Unit 8 is replaced by Tape Unit 11. The appropriate tape unit number may be assigned by input at points where sympolic locations are given.

In Tables 5-6 through 5-10 the logical unit given is standard for TRACE-D program operation at Aerospace Corporation. Also, it should be noted that standard system tapes are omitted in Tables 5-6 through 5-9 but are included in Table 5-10 for completeness.

Table 5-6. Tape Unit Requirements for Trajectory Runs

Logical Unit	Symbol	Function
٠,7	CTAPE	Planetary-coordinate input
8*		Program input
14	DTAPE	Binary difference tape for trajectory differencing
15	NTAPE	Binary trajectory tape (nominal) for trajectory differencing
15		Binary trajectory tape in standard format

^{*}Use of corresponding tape is mandatory.

Table 5-7. Tape-Unit Requirements for Tracking Runs

`Logical Unit	Symbol	Function
6	ETAPE	BCD data output
7	CTAPE	Planetary coordinate input
8*		Program input
9*		Scratch tape (A ^T A)
10*	٧	Scratch tape (FITA trajectory)
13*		Binary compacted data (I/O)

Table 5-8. Tape-Unit Requirements for Data Generation Runs

Logical Unit	Symbol	Function
6	ETAPE	BCD data output
7	CTAPE	Planetary coordinate input
8*		Program input
10	IFLAG(16)	Scratch tape (GAINA trajectory)
		\#

Table 5-9. Tape-Unit Requirements for Residuals-Analysis Runs

Logical Unit	Symbol	Function
8*		Program input
10*		Scratch tape (FITA trajectory)
13	NUMB(43)	Compacted data input (differencing)
14	NUMB(45)	Trajectory input (differencing)
15	NUMB(44)	Trajectory input
		•

*Use of corresponding tape is mandatory.

Table 5-10. Summary of Tape-Unit Requirements by Logical Unit

Logical Unit	Symbol	Function
1		FORTRAN monitor system*
2		System input*
3		System print output*
4		Not used
5		Not used
8	IBCDI	BCD observation input
6	ETAPE	Data generation output
7	CTAPE	Planetary coordinate input
8		Program input*
9		Scratch tape (tracking*)
9	NUMB(38)	Scratch tape (residuals analysis)
10		Scratch tape (tracking*, residuals analysis, data generation)
11		System chain tape
12		System punch output*
13		Compacted data input/output (tracking*)
14	DTAPE	Differences (used with TTAPE)
14	NUMB(45)	Trajectory input (residuals analysis differencing)
15	NTAPE	Trajectory (nomal) for trajectory link differencing
15		Trajectory in standard format, output from trajectory
15	NUMB(44)	Trajectory in standard format, input to residuals analysis differencing
16	NUMB(43)	Compacted data input, residuals analysis differencing

^{*}Use of correponding tape is mandatory

### 5.4 IBM 7094 SENSE SWITCH CONTROLS

The sense switch controls on the IBM 7094 computer console may be used to control TRACE-D program operation. Table 5-11 itemizes resulting action for Sense Switches 1 through 6 in the On position. The itinerary types with which the use of each sense switch is permissible are noted in all cases.

Table 5-11. Action Resulting from IBM 7094 Sense Switch Use

Sense Switch Number	Function
1	Termination Options (DCS System only)
	When subroutine EXIT is called, the message "SET 7094 CONSOLE KEYS, PRESS START TO CONTINUE" is printed on-line and the computer halts. When START is pressed, the program tests the console key positions and accomplishes one of the following functions:
	a. Terminates normally if the Q key is down.
	b. Empties the output buffers, rewinds and unloads the A2 list output tape, and calls Link 1 if Key No. 1 is down.
	c. Rewinds and unloads the A3 input tape and calls Link 1 if Key No. 2 is down.
	d. Rewinds and unloads punch tape and calls Link l if Key No. 3 is down.
	Used for all itinerary functions.
2	Iteration Print
	Results of each iteration, corrections, an RMS summary, etc., are printed on-line and the convergence test is bypassed.
	Used for orbit determination only.
3	Forced Termination
	The observation time that is encountered during the FITA integration process after Sense Switch 3 is turned on is taken as the last one for the current iteration and the least-squares process is initiated. If Sense Switch No. 2 also is down (On) the corrections are applied and integration for the next iteration is initiated in the normal manner if

Table 5-11. Action Resulting from 7094 Sense Switch Use (Concluded)

Sense Switch Number	Function
3 (continued)	MAXIT has not been exceeded. If Sense Switch No. 2 is not down, the run is terminated after the least-squares process is completed.
	In the case of a trajectory, or ephemeris generation run, integration is terminated as soon as Sense Switch No. 3 is turned on. If a data generation is in process, the GAINA integration is terminated and the GAINB link is called to compute and output the generated data.
	Used for orbit determination, ephemeris generation, and data generation.
4	Impact Indication
	A message is printed on-line whenever the input altitude at C(35) is reached either from above or below.
	Used for orbit determination and ephemeris generation.
5	Residuals Print
	All residuals are printed on-line.
	Used for orbit determination only.
6	Apsis Print
	Position information is printed on-line and off-line whenever the flight-path angle ( $\beta$ ) passes through 90 degrees.
	Used for orbit determination and ephemeris generation.

### 5.5 OUTPUT

This section describes the printed output produced by the TRACE-D program for typical trajectory, orbit determination, data generation, and residuals analysis runs. The samples of actual output listings which are included are annotated to detail specific portions of the output data, and also are cross-referenced against applicable equations and definitions given elsewhere in this document. In the case of items occurring within more than one sample listing, citations are given for their first appearance only.

## 5.5.1 Output Common to All TRACE-D Runs

The initial pages of output generated from any TRACE-D run will present material similar to that tabulated in the sample output listing shown in Figure 5-29. Supplementary descriptive information relating to indicated areas of this listing is annotated in Table 5-12.

ENTRY !	ENTRY POINTS TO SUB	SROUT [.H	SUBRGUTINES REQUESTED FROM LIBRARY, (1)	FROM	LIBRARY, (I)			
	EXECUTION 19.585	.585						
CHAIN.	. LINK NO.	4						
GINTEG		-C STA	RACE-C STANDARD INTEGRATION CONSTANTS	TION	CONSTANTS		FINP INPUT CARD	
11	<b>,</b>	71	~	13	0	STDINTEG 01	FINP INPUT CARD	
•	q	'n	1	=	1.00002516	STOINTEG 02	FINP INPUT CARD	E 3
23	1.	-9 26	1	30	1	STOINTEG 03	FIND INPUT CARD	•
31	-015625	32	*	33	1 ~1	STOINTEG 04	EINP INPUT CARD	'n
134	+	135	1	37	.001	STRINTEG 05	FINP INPUT CARD	•
38	6.	40	2820-1763	143		STOTNIEG 06	FINP IMPUT CARD	^
ပ္ပ	TRACE	-D STAR	RACE-D STANDARD PHYSICAL CONSTANTS	CONS	STANTS 10/ 1/65		FINP INPUT CARD	•
-	.43752691	7 2- 169	-55303935 -2	9 2		STDCONST 01	FINP INPUT CARD	6
	.43772691	691 -2 9	1-	9	10	STOCONST 02	FINP INPUT CARD	-
13	3260,8399	*	57.2957795	15	20925734	STDCONST 03	FINP INPUT CARD	1
77	332951.3	17	-0122999	18	.814979	STOCONST 04	FINE INPUT CARD	12
19	107821	82	317.667	77	95,129	STDCOMST 05	> 3 FINP INPUT CARD	
72	23454-865	23	3443.9336	<b>52</b>	20925738	STOCONST 06	FINP INPUT CARD	ı
\$2	348762.3	56	32-174	æ	348762.3	STDCONST 07	FINP INPUT CARD	15
Ť	11.5	32	1.0471976	ñ	3.14159265	STOCONST 08	FINP INPUT CARD	9
*	298.3	35	300000	36	82505.922	STDCONST 09	FINP INPUT CARD	i
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Figure 5-29. Sample TRACE-D Program Common Output Listing

FINP IYPUT CARD 18	FINP INPUT CARD 19	FINP INPUT CARD 20	FINP INPUT CARD 21	FINP INPUT CARD 22	FINP THPUT CARO 23	FINP INPUT CARD 24	FINP INPUT CARD 25	FINP INPUT CARD 26	FINP INPUT CARD 27	FINP INPUT CARD 28	FINP INPUT CARG 29	FIND INPUT CARD 30	FINP INPUT CARD 31	FINP ÎNPUT CÂRO 32	FINP INPUT CARD, 33.	FINP INPUT CARD 34	FINP INPUT CARO 35	FINE THPUT CARD 36	FINP INPUT CARD 37	FINP THPUT CARD 38
		(	<u>ئ</u>		*								4	( <del>-</del>	)		•			,
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4	.10823 -2	*X		-15-684		ILE SERVICE	6,TP ORDER EARTH MUDEL	20925741.	1.723 -6	.16434	9- 61150.	.05329 -4	9958000*	.011666	.00005153 -6	5.31	-136.68	36.01	-3.45	157-21
£3	~	18 ->!THA!X4	3443.9336 DRAG	6.83 4		THE PREVIOUS CAKES WIRE READ FROM FILE SERVICE	6,TP 0RDER	.55304505 -2 15	8	.4482 -6 5	.1536 -6 8	-1569 111	*00%093 -6 14	.03746 -6 17	.0003328 -6 20	-13-18 3	. 9 00.91	-1.10 9	-2.60 12	-15.32 15
12 0	26801	-5 4	42 34	3 6.		REVIOUS CAKES W	STANCARD DECK	,043752695-1 2 .5	741. UBJT	4 0	L 9-	01 9-	-6 13	-6 16	-6 19	2 -1	<b>\</b>	<b>&amp;</b>	77	1- 41
1108 4	Ó 41	323	NUMB	12 1	RREFC1.	GC THE PR	GC STANCA	1 ,0437	24 20925741.	3 1-856	6 .7278	9 .504781	12 .005842	115 .06611	18 .002256	081.7	4 -13.33	7 27.47	10 -81.86	13 58.25

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Figure 5-29. Sample TRACE-D Program Common Output Listing (Continued)

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Figure 5-29. Sample TRACE-D Program Common Output Listing (Continued)

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Figure 5-29. Sample TRACE-D Program Common Output Listing (Continued)

1 0		1000	<b>(5)</b>	
FIND INPUT CARD	0.21574342E 08 0.20808183E-07 0.83221839E 02 0.20237660E 03 0.29568523E 03 0.48652040E 03	02(6) -05 J5= -0.599999999=-08(18) -06 J10= 0. 1.52= -0.34099999 01 1.53= -0.34499999 01 1.54= 0.582540000 02	7 7 1	
	E 03 Am 0.0-6 En 0.0-	2 =-0.15684000E 02 (6) 3	0.8482000E-09 0.66110000E-07 0.31850000E-07 0.2256000E-08 0.3279999E-09	
INITIAL, CONDITIONS	0.20663586E 03 0.3199999E 02 0.88999999E 02 0.7999999E 03 0.21574342E 08 0.2554359E 05	FIN MODEL -0.26930000E 0. J52E 02 J53E 01 J54E	02 J63= 02 J63= 02 J64= 02 J64= 02 J64= 02 J64=	
	ALPHA= 0517A= 857A= AZ= N = V = CDA/W=0.090	0.10827599E-02 J3# 0.6329999E-06 J0# 1212 0.13180000E   1312 0.53100000E	.,	ED FOR PLANETARY (OTTON) (2)
END ITINERARY 3 EXAMPLE. (II)	= -0.16354387E 08 = -0.32024749E 07 = 0.11432640E 08 01	(i) 0.55304505E-02 J2* 0. 0.38999999E-06 J7* -0. 21* 0. 22* 0.17230000E-05 31* 0.1854000E-05	0.44819999E-06 0.16429999E-06 0.17380000E-06 0.57190000E-07 0.5719999E-08	THE FOLLOWING BODIES ARE USED FOR PLANETARY PERTURBATIONS  NUME (2)  FIRMULATION  COMELL (EQS.OF MOTION) (2)  DIFFERENTIAL EQUATION SUBROUTINE
END	X	6/4 0.552 J64 0.385 J21 422		THE FOLLOWI NOWE (2) EFRENCE ATTOM

Figure 5-29. Sample TRACE-D Program Common Output Listing (Continued)

(E)			(;	<b>(2)</b>		
UNGE KUTTA 4		0CTAL 171552343100	231477232264	223524455115	172623026050 175671505015 207574410142	
RATIO OF COMELL SYEP TO RUNGE KULTA PAXIMUM= 0.6460E 02		0ECIMAL 0.55304505E-02	0.20925741E 08 0.34439336E 04	0.34876230E 06 0.34876230E 06 0.29830000E 03	0.12299900E-01 0.10782100E-00 0.95129000E 02	
1 1	·		EARTH RADIUS - FT	1-0, VELOCITY FI/SEC//E.R./N.M.	) ) RN)	
A= 1.000 0.1563E-01		CONSTANTS	į	!	(MARS)	
= 0.1000E-09 MINIMUM= RRECTOR	(3)	0CTAL	202735465305	231477232264	223595113515 200641211666 211475706112	
ACKSCN E 64R= 0.100 TIAL= 0.100CE ON HIRECTOR	USE N1 = 9 N2= 6 23	DECIMAL	0.37312833E 01 0.32808398E 04	0.32173999E 02	0.33295130E 06 0.81497900E 00 0.31788700E 03	
STEP SIZE - INITION OF THE PER	EQUATIONS OF MOTION				DEG/SEC//RAC/MIN MELATIVE HASSISUN) IVENUS)	

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Figure 5-29. Sample TRACE-D Program Common Output Listing (Concluded)

Table 5-12. Common Output Listing Description

		<del></del>
Item	Description	Page Reference
1	FORTRAN II monitor message giving names of subroutines called from library by REIN link.	4-1
2	Card images of the first seven FINP input cards. These input data contain the standard entries for the integration constants array.	3-63 Appendix A Appendix F
3	Card images for FINP Input Cards 8 through 22. Standard values of physical constants and option indicators are shown.	4-7 Appendix A Appendix F
4	Card images for FINP input cards numbers 23 through 42. Numbers shown are entries for a gravity field model including non-zero coefficients through Degree 9 for the zonal and through Degree and Order 6 for the tesseral and sectoral terms.	3-46/3-49 Appendix A Appendix F
, <b>5</b>	Card images for FINP Input Cards 43 through 50. These input data specify a single-case trajectory run.	5-1/5-17 Appendix F
6.	Program identification. AD014D is the Aerospace Corporation Computation and Data Processing Center program number for accounting purposes. The word REFERENCE means that the program which produced this output is associated with the basic or reference version of TRACE-D, or the version wherein no modifications are included. Output produced by a modified program version would reflect the appropriate modification numbers in lieu of the word REFERENCE. It should be noted that all material contained in the present document is directed toward description of the reference program version.	
7	Hl header card entry.	Figure 5-1
8	If any header information had been input on an H2 card, the entry would have been printed at this location.	Figure 5-i

Table 5-12. Common Output Listing Description (Continued)

Item	Description	Page Reference
9	Epoch time	5-4
10	Program link identification. Each time a different link of the program is called a remark of this nature is printed.	4-1/4-5
11	Card image of the final (second) END card in the input deck. This card is required because the FINP routine is called in the INITA link as well as in the CHAIN link. Under certain conditions additional FINP input data may be read at this point.	4-1/4-5 5-60 Appendix F
12	Trajectory initial conditions in three coordinate systems. Initial-condition values as shown are the result of transformations which have been applied to the input values. The transformation for the input coordinate set (a, δ, β, A, r, v in this case) consists of conversion from decimal to octal numbers, conversion of units from feet, degrees, and seconds to earth radii, radians, and minutes, and performance of corresponding inverse conversions for output. The two other types of elements sets also require accomplishment of coordinate-system transformations in addition to the number- and units-systems conversions noted above. Accuracy of the values as printed therefore is subject to numerical and roundoff errors.	3-1/3-5 3-9/3-12 5-4,5-5
	Quantities in the left-hand column are position and velocity components in the basic vernal equinox coordinate system, with units of feet and of feet per second. The center column gives the usual ADBARV spherical system coordinates (i.e., Type-2 initial conditions in units of feet, feet per second, and degrees). The right-hand column from top to bottom contains orbit semi-major axis, eccentricity, inclination, right ascension of ascending node, argument of perigee, and time of last perigee passage in minutes from midnight of epoch day. Other units are feet and degrees.	

Table 5-12. Common Output Listing Description (Continued)

Item	Description	Page Reference
13	Identification of atmosphere model to be used in computing drag force. LOCKHEED and ARDC 1959 refer to the Lockheed-Jacchia and the ARDC 1959 model atmospheres, respectively.	3-50, 3-51 5-6
14	Reciprocal of ballistic coefficient, CDA/W	3-50 5-6
15	Ballistic coefficient, $W/C_D^A$	3-50 5-6
16	$d_1$ and $d_2$ are values of certain constants in the Lockheed-Jacchia atmosphere density expressions.	5-6 Appendix C
17	The product GM, or the universal gravitational constant times the mass of the earth (frequently designated by $\mu$ ), expressed in units of earth radii cubed per minute squared.	3-46, 3-47 Appendix A
18	Unitless coefficients of the zonal harmonic terms in the earth potential field expansion (i.e., $J_2$ through $J_{10}$ ).	3-47 Appendix A Appendix F
19	Coefficients and longitudinal arguments of tesseral and sectoral terms in earth potential field expansion, with J indicating a coefficient and L an argument in degrees. The digits following J or L are the associated Legendre polynominal degree and order, respectively.	3-47 Appendix A Appendix F
20	Names of solar-system bodies included in computation of perturbative accelerations.	3-49 5-7 Appendix A
21	Trajectory method indicator. The Cowell formulation of the equations of motion is the only trajectory method available in the present TRACE-D program.	2-2 3-46
22	Numerical integration parameters. The Gauss-Jackson method (subroutine COW) is the only integration method available in the present TRACE-D program.	3-63 Appendix A Appendix F

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Figure 5-31. Sample TRACE-D Program Tracking Output Listing

Table 5-12. Common Output Listing Description (Concluded)

Item	De	scription	Page Reference
24 (cont)	m. N.M./E.R.	Number of nautical miles per earth radius	
	n. I-O, VELOCITY	Conversion factor for input/ output in feet per second/ earth radii per minute	
	o. FI/SEC// E.R./MIN.	Units conversion factor in feet per second/earth radii per minute	
	p. 1/EPS (1/c)	Earth flattening (reciprocal of earth ellipticity)	
	q. (MOON)	Mass of moon relative to mass of earth	
	r. (MARS)	Mass of Mars relative to mass of earth	
	s. (SATURN)	Mass of Saturn relative to mass of earth	

## 5.5.2 Trajectory Output

The listed output created by a typical trajectory run is shown in Figure 5-30. Supplementary descriptive information relating to the indicated areas of this listing is annotated in Table 5-13.

;		!	i T		!		-				!
		REV. NPD. NPDK. NXEG	00		・	REV, APD, NPCK, NREG		•0	•	• • • • • • • • • • • • • • • • • • • •	REV.hPD.NPDK.NREG
		xocr,y Lar, Long, H, SBV ALPHA, CELTA, BEFA, A	31.99999928	0		LAT, LONG, H, SBV ALPHA, DELTA, BETA, A	7.21385860	65.51185417	89.96440029	163-44273567	LAT, LCNG, H ŞBV ALPHA, DELTA, 3ETA, A. REV. NPD, NPOK, NREG.
		LAI, LONG, H, SBV	32.17318	32.16780	•	LAT, LONG, H, SBV	65.65669	20.55430	117-48816	16159*59	LAT, LCNG,H SBV
		xocr, sec.	0.13575507E 05	0.25543559E 05	-0- SEC.	xpor.v	0.21173423E 35	0.10008825E 05	-C.10122698E 05	0.25513906E 05	20.31693 SEC. _XDDT _C V
Entring Link and 4 Intig	IK NO. 8	4/26/65 8 HAS. 30 MIN. H.SI.OT X,R	510.00000	0.21574342E 08)	8 HRS. 50 PIN.	α.×	0.88748144E 07	0.11233307E 07	0.19640148E 08	0.21581465€ 08	4/26/65 9 HRS. 6 PIN.
בשוניצועם כזו	ENTIRANG LINK NO. 8	4/26/65	510.0000	0.25000	1126/65	HE, MIL ST, DT	20.00000	230.00000	31799.99951	00000-1	4/26/65 9 HRS. ME, MISSTAUT X.R

Figure 5-30. Sample TRACE-D Program Trajectory Listing

C

546,33862	0.82080155E 07	0.27833810E 04	31.59920	0.0000777	0.50000
32780,31641		-0.25357457E 05	109.34348	90.01619530	0.
£, 00000	0.21590124E 08	Q.25535751E 05	0.0000	173.22540474	•0
41.26/65	9 HRS. 10 MIN.	-0. SEC.			
ME, MY, ST, DT	e X	XDOT.V	LAT . LONG . H . SBV	ALPHA.CELTA.BETA.A	REV. NPD. NPOK. NREG
40.00000	0.1904750 = 08	-0-71894251E 04	-14-87704	24-14084196	0.54136
550,00000	0.8536701JE 07	0.19215893E 03	32.47760	-14.78183973	0
32999,99951	-0.55078332E 07		109-67533	90.03582287	
1.00000	0.21587552E 08	0.25536284E 05	-14-87409	172.99185562	•0
47.26/65	9 HRS. 30 MIN.	-0- SEC.			
ME, MM, ST, DT	4	V. 100	LAT. LONG. H. SBV	ALPHA DELTA BETA . A	PEW-NPO-NPOK-NRFG
60.00000	-0.31340595E 07	-0,23349G;*E 05	-80-84501	155-16534996	0.76736
570.00000	0-14504394E 07	-0.994442231.04	158-48841	-80-78437138	0
34199,99951	-0.21285260E 08	0.27671982E 04	116-22682	90-01528549	
1,60060		0.25528986E 05	-80.34303	47.53156471	0
41.26/65	9 HRS. 50 HIN.	-0- SEC.			
ME, MM, ST, DT	۲,	V , 100	LAT.LCMG.H.SBV	ALPHA.DELTA.BETA.A	REV. NPO. NPOK. NREG
80.00000	-0-19980005E 08	0.184337928 03	-2-30664	202-03945732	0.569.0
590,00000		-0.31801306E 04	200-34884	-2-29121947	0-
35399,99951	-0.86243754E 06	0.25357323E US	106.45209	89.98230743	0-
1.00000	0-21572443E 08	U-25556624E 05	-2.30618	6.77947885	•
4726/65	9 HRS. 50 MIN.	33.99216 SEC.			
HE MA STON	X,X	XDOT, V	LAT . LONG . H. SBY	ALPHA, DELTA, BETA, A	REV.NPD.NPOK.NREG
30,56654	-0.19957592F 08	0.11376827E 04	-0-03005	202-31175423	1-00000
590.56654	-0.81899897E 07	-0.27915415E 04	200-47911	-0-00005180	
35433.99170			105.47580	89,98370457	3 6
1,00000	0.21572700E 00	0.25556367E 35	-0-0000	6.17400285	0.0
A,E,I,0,U,T	HEAN ANN.	17.04108	APGGEE× 3557,14874	374)	
0.21592714E	GB TRUE ANH=	17,07367	HT = 114,20410	610	
0.96955182E-	(	9	E 3	778 (4)	
0.20231175E		-4.15387) PER	HT = 107.31314 PERIOD(K) = 28.56033	_	
0.34292526E	63	PER		187	
0.58637441E	<b>( 60</b>	PER	PERIOD(N)= 88.48662	562)	
A-5" C 46.00	75 . 50	200			

Figure 5-30. Sample TRACE-D Program Trajectory Listing (Continued)

-0.38656866E  0.21036513E  0.21036513E  0.19142365E  0.69184285E  0.69184285E  0.69184285E  0.21589882E  0.195777899E  0.26637282E	07 C.89774919E 04 08 0.486484E 04 08 0.486484E 04 08 0.68615822E 04 07 0.5876804E 04 07 0.5876804E 04 07 0.5876804E 04 07 0.5876804E 04 07 0.5876808E 04 08 0.25531579E 05 08 0.25531579E 05 08 0.25531579E 05 08 0.255358191E 05 08 0.255358191E 05 08 0.255358191E 05 08 0.25535420E 05	227.08046 117.87643 17.24529 19.59969 19.59969 110.59369 19.59590 10.59368 10.00007 0.00007 0.00007 0.00007	ALPHA, DELTA, BETA, A 19, 9852669 32, 13441420 19, 87085485 19, 47840810 89, 99269440 172, 81200790 172, 81200790 22, 27862501 0,00007069 90,01715755 173, 22672272	REV, NPO, NPCK, NREG 1.44549 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.00
0.21036513E 0.21036513E 10 HKS. 30 M X.R. 0.19142365E 0.471931809E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.21589843E 0.2158943E 0.2158943E 0.2158943E	08 0.48648424E 04 08 0.48618424E 04 08 0.68615822E 04 07 0.5876842F 04 07 0.527682F 04 08 0.25531579E 05 08 0.25531579E 04 08 0.25531579E 05 08 0.2553642E 04 08 0.2553642E 05	117.25929 17.25929 19.59969 8.15285 10.59969 10.59969 10.599909 10.599909 10.599909 10.599909 10.00007 10.22637	ALPHALDELIALBEIALA 19.45134414.20 32.134414.20 19.47045485 19.47045485 19.47045485 172.81200790 172.81200790 172.81200790 173.81200790 10.00007069 90.01715755 173.22672272	0.000 0.100 1.44549 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.
0.21575265E 0.19142365E 0.69184285E 0.69184285E 0.21589882E 0.21589882E 0.21589882E 0.21589882E 0.1977789E 0.26637282E 0.26637282E 0.26637282E 0.26637282E 0.26637282E	0.2551617E 05  0.68615822E 04  0.58768047E 04  0.58768047E 04  0.25531579E 05  49.54850 SEC.  XEOT.V  -0.11488482E 04  0.2553642E 05  0.2553642E 05  0.2553642E 05	17.24929 17.24929 19.59969 10.59969 10.59990 10.59990 10.59990 10.59990 10.22637 0.00007	ALPHALDELIALBEIALA 19.87085485 19.87085485 19.47840810 89.9906040 172.81200790 172.81200790 173.22672775 173.22672775	REV, NPO, NPCK, NREG 1, 44549 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0
10 HKS. 30 PI 10 HKS. 30 PI 0.19142365E 0.69184285E 0.21589882E 10 HKS. 34 MI 0.199777895 0.199777895 0.26637282E 0.21589413E 0.21589413E 0.21589413E 0.21589413E 0.21589413E	-0. SEC. XD01.9 -0. 88152E 04 0. 881682E 04 0. 5876867E 05 0. 2531579E 05 0. 2531579E 05 XD01.9 -0. 2531579E 05 0. 2533151E 05 0. 25336420E 05 0. 25336420E 05 0. 25536420E 05	17.24929 19.59969 19.59969 10.59969 19.59990 19.59590 10.59986 109.22637 0.00007	ALPHALDELIA BETALA 19.87085485 19.4708100 89.92060440 172.61200790 172.61200790 ALPHA, DELTA, BETALA 22.27862501 0.00007069 90.01715755 173.22672272	REV. NPO. NPCK. NREG 1.44549 0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.
10 HKS. 30 M X-R 0.19142365E 0.69184285E 0.71991809E 0.21589882E 0.21589882E 0.19977789E 0.91847834E 0.26637282E 0.21589413E 10 HRS. 50 MX X-R X-R X-R X-R X-R X-R X-R X-	25C. XDOI.9Y C. ADDI.9Y C. ADDI.9	LAY, LONG, H, SBY 19,59969 8,15285 110,59349 19,59590 19,59590 10,59590 10,00007 10,22637 10,22637	ALPHALDELIALBETALA 19-87085485 19-47840810 89-99060440 172-81200790 ALPHALDELTALBETALA 22.27862501 0.00007069 90-01715755	REV. NPO. NPCK. NR. EG. 1.44549 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.
X,R 0.19142365E 0.69184285E 0.21589882E 10.185, 34 MI N,R 0.19577789E 0.21684734E 0.21589413E 0.21589413E 0.21589413E 0.21589413E 0.21589413E 0.21589413E	XDO1.9 0.68615822E 04 0.68615822E 04 0.252878647E 05 0.2531579E 05 49.54860 SEC. XDO1.0 -0.11486482E 04 0.21540728E 04 0.25358191E 05 0.25358191E 05 0.25358191E 05 XDO1.0	LAY, LONG, H, SBV 19,59969 8,15285 110,59309 19,59590 19,59590 10,59590 10,59590 10,59590 10,59590 10,59590	ALPHALDELIALBETALA 19.87085485 19.47840810 89.99060440 172.81200790 172.81200790 ALPHALDELTALBETALA 22.27862501 0.0007069 90.01715755 173.22672272	REVANDOANEGA 1.44549 0.00 0.00 0.00 REVANDOANEGA 1.50000 0.00 0.00
0.19142365E 0.69184285E 0.471991809E 0.21589882E 30 HRS. 34 MI 0.1977789E 0.26637282E 0.21589413E 10 HRS. 50 MJ X.R X.R 0.3667282E 0.21589413E 0.21589443E 0.21589443E	0.68615822E 04 0.58768047E 04 0.525815762E 05 0.25531579E 05 49.548E0 SEC. XEOT.V -0.1148848E 04 0.213640128E 04 -0.25358191E 05 0.25536420E 05 XEOT.V XEOT.V	LAY, LONG, H, SBV 0,00007 10,59309 19,59309 0,00007 109,25637 0,00007	ALPHA, DELTA, BETA, A  19.47840810  89.99060440  172.81200790  172.8120790  80.00007069  90.01715755  173.22672272	REV. NPO. NPES. NREG. 0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0
0.69184285E 0.71991809E 0.21589882E 10.199777899E 0.26637282E 0.21589413E 0.21589413E 0.21589413E 0.21589413E 0.21589413E	0.5876867E 04 -0.2531579E 05 0.2531579E 05 49.54860 SEC. XDOTA -0.11486482E 04 0.25336191E 05 0.25336420E 05 -0.25336430E 05 -0.25336430E 05 -0.25336430E 05 -0.25336430E 05 -0.25336430E 05	19.59969 8.15.285 10.59309 19.59590 10.59590 10.59590 10.22637 10.22637	19.87085485 19.47040810 89.92060440 172.61200790 172.61200790 ALPHA, DELTA, BETA, A 22.27862501 A.00007069 90.01715755 173.22672272	1.44549 0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.0.
0.21549882E 0.21549882E 0.21549882E 0.19577789E 0.91847839E 0.21549413E 10 HRS. 50 KI X.R R&&&QQQE 0.29490443E	49.54860 SEC.  49.54860 SEC.  X001,V  -0.11488482 04  -0.218407286 04  -0.25536420 05  -0.25536420 05  X001,V	LAY, LONG, H, SBV 0,00007 109,253309 0,00007 0,22637 0,00007	19.47840810 89.99060440 172.81200790 ALPHA, DELTA, BETA, A 22.27862501 90.01715755 173.22672272	0. 0. 0. REV,NPD,NPDK,NREG 0. 0.
0.21589882E 10 HRS. 34 MI 0.1977789E 0.26637282E 0.21589413E 10 HRS. 50 MJ X,R 0.2949643E 0.29496443E 0.29496443E	49-548(8(6.% 05-67-68)	110-59309 19-59590 19-59590 0-00007 109-25696 109-25697	89.9960440 172.81200790 172.81200790 ALPHA,DELTA,BETA,A 22.27862501 90.01715755 173.22672272	0. 0. 0. 1.5000 0. 0.
10 HKS. 34 MI X,R 0.195777896 0.266372826 0.266372826 0.266372826 10 HKS. 50 MV X,R 0.264036 0.29490438	49.54860 SEC. XDOT V -0.11486482E 04. 0.21540728E 04. 0.25358191E 05. 0.25536420E 05. -0.25356191E 05. -0.25356191E 05. -0.25356191E 05.	19.59590 LAY, LONG, H, SBV 0.00007 109.22637 0.00007	172.61200790 ALPHA, DELTA, BETA, A 22.27862501 0,,0002069 90.01715755 173.22672272	0. REV,NPD,NPDK,NREG 1.50000 0. 0.
10 HKS. 34 HI N. R.	49.54860 SEC. X601.V -0.11486482E 04. C.218.0728E 04. -0.25358191E 05. 0.25536420E 05. XD01.V	LAY, LONG, H, SBV 0.00007 9.35086 109.22637 0.00007	ALPHA, DELTA, BETA, A 22.27862501 0.00007069 90.01715755 173.22672272	REV,NPD,NPDK,NREG 1.50000 0.00000000000000000000000000000
X,R 0.195777895 0.26637282E 0.21589413E 0.21589413E 10 HRS. 50 M/ X,R 0.22490443E -0.1886338E	X601,V -0.1148442E 04 C.2184014E 05 -0.25358191E 05 0.25536420E 05 x001,V	LAY, LONG, H, SBV 0.00007 9.35986 109.22637 0.00007	ALPHA, DELTA, BETA, A 22.27862501 0.00007069 90.01715755 173.22672272	REV, NPD, NPDK, NREG 1.50000 0.00000000000000000000000000000
0.19977789E 0.48637282E 0.26637282E 0.21589413E 10 HRS. 50 MJ X.R 0.486072409E 0.52490438E	-0.11488482E 04 0.21840728E 04 -0.25358191E 05 0.25536420E 05 -0. SEC.	0.00007 9.35086 109.22637 0.00007	22.27862501 0.00007069 90.01715755 173.22672272	1-50000
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Figure 5-30. Sample TRACE.D Program Trajectory Listing (Concluded)

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Table 5-13. Trajectory Output Listing Description

Item	Description	Page Reference
l	Date and time of day (Greenwich Mean Time) with which the quantities in the print block following are to be associated.	5-11
2	Minutes from epoch, minutes from midnight of current day, system time (i.e., seconds from midnight of current day), and current integration step size in minutes.	5-11
3	x, y, z, r: Components and magnitude of the radius vector from geocenter to satellite in the basic coordinate system in units of feet.	3-2
4	x, y, z, v: Components and magnitude of the inertial velocity vector with respect to the basic coordinate system in units of feet per second.	3-2, 3-3
5	Geodetic latitude, in degrees, of the point where the radius vector intersects the ellipsoidal surface of the earth, geographic longitude measured east from Greenwich in degrees, altitude of the satellite above the oblate earth in nautical miles, and geodetic latitude of the subvehicle point in degrees. All latitude quantities are considered positive north of the equator and negative south of the equator.	3-64
6	a, δ, β, A: Right ascension of satellite position, declination of satellite position, flight path angle, and inertial azimuth of velocity vector in units of degrees.	3-3 3-9
7	a, e, i, $\Omega$ , $\omega$ , $\tau$ : The classical elements as computed from X, $\dot{X}$ at the ascending node in units of feet, degrees, and minutes from midnight of epoch.	3-4 3-11 5-8
8	M, v, Ω, ω: Mean anomaly and true anomaly in degrees, and nodal regression rate and rate of advance of the line of apsides in degrees per day as computed from X, X at the ascending node using closed-form expressions.	3-4, 3-5 3-64, 3-65 5-8

Table 5-13. Trajectory Output Listing Description (Concluded)

Item	Description	Page Reference
9	Radial distance at apogee, height of apogee above the oblate earth, and radial distance and altitude of perigee in nautical miles; Keplerian period, anomalistic period, and nodal period in minutes as computed from X, X at the ascending node using closed-form expressions.	3-65, 3-66 5-8
10	Revolution number, nodal period in minutes, nodal period decay rate in minutes per revolution, and nodal regression rate in degrees per revolution. Due to the fact that the nodal period is calculated by simple subtraction of ascending-node crossing times, this quantity cannot be determined until two ascending node crossings have been detected. Also, since the nodal-period decay rate is computed by differencing the nodal-period values at successive ascending nodes, this rate cannot be calculated until three ascending nodes have been crossed. The nodal regression rate is computed by differencing values of right ascension at successive ascending nodes.	3-66 5-15

## 5.5.3 Tracking Output

Listed output produced by a typical tracking (orbit determination) run is shown in Figure 5-31. Supplementary descriptive information relating to the indicated areas of this listing is annotated in Table 5-14.

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Figure 5-31. Sample TRACE-D Program Tracking Output Listing

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Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

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Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

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Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

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ATHOSPHERE	ATHOSPHERE - LOCKHEED	CDA/W = 0.2000 DI = 0.6829	0.20000000E-01 0.68299999E 01	W/CDA = 0.49999999 02 D2 =-0.15684000E 02	: 02 : 02
	J2=		EARTH MODEL J3= -0.26930006-05	# <b>*</b>	0E-05 J5+ -0.59999999E-08
J6# 0.38999 J21# 0. J22# 0.	0-38999998-06 J7= -( 21= 0. 22= 0.17230006-05	-0.63299996-06 J8= 0. L21= 0. L22= -0.1318COOE D2	0. J52= 02 J53=		0.209999995=06 JIA 0. 000E-07 L52= -0.26000000E 01 999E-08 L53= -0.34499999E 01
	0.18560000E-05 0.44819999E-06	L32= -0.13330000E		0.4C929999E-08 0.84620000E-09 0.66110000E-07	L54* 0.58250000€ 02 L55* -0.15320000€ 02 161* 0.157.999€ 03
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Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

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USES 1	MATRIX						
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Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

-	2	ANH	173.84310	310		m			
	Ť		173-84310		M I		6		
1		C0G1*	1.59386		PERIGEER	M	_		
		upo1*	-2-04119		# 12 K		(91)人。		
U, 15882923E G3				1	PER TOUCK Z	Ì	)		
0.18615689E 03 -0.30146602E 02					PERIOD(A)= PERIOD(N)=	103.71713	- 0		•
ENTERING LINK MO.	5 FIT	IT A							
Ŏ	Ĭ	601421724760	24760	177650254365		/2000000000000	471651221774	1734224, 113	175422532313
UST	<u>.</u>	10.0	10.0 SECONDS	S FROM MIDNIGHT	NIGHT OF	OF EPOCH **	•0		
	£	201421611154	11154		Ю	774300000	-571650366020	573422716353	575422736454
UST RESULT		0.94960182E-04	82E-04	FT/SEC#SEC	2				
	Į	601422111433	11433	177646122413	)ı	552737400000	171647064332	173422563440	175422525653
UST RESULT		0.90158949E-04	49E-04	FT/SEC+SEC					
	Į,	201421773630	73630	517644540745		152751600000	571646211710	573423055244	575422734010
THRUST RESULTANT =		0-85600495E-04	•	FT/SEC+SEC	,	(%)			
IHRUST E		100GC.0 SECONDS		FROM MIDNIGHT	0	OF EPOCHOOO			
1/64 207		601422272620	72020	177643770103		553755454000	171644726523	173422723003	175422523224
3/ 1/64 259.41747	ī	201422150267	50267	577642355674		154536310000	571644047473	573423216157	575422734243
1/64 311		601422445672	45672	177641611167	-	554515100000	171642502765	173423057507	112422524911
1/64	ī	201422325656	25656	577640204152		154637260000	571641621156	573423364043	575422732632
3/ 1/64 415.07563	r.	601422621146	21146	177637423163		554447540000	171640316430	173423233045	175422525157
1/64	T.	261422502342	02342	577636031463		155457100000	571637412175	573423540032	575422131053
1/64 518	ĭ	661422772364	72364	177635244217		555634720000	171636171600	173423412732	175422527026
3/ 1/64 570.73259	ī	201422655213	55213	577633663144		155660314300	571635251791	573423722110	575422730030
1/64	X.	601423143133	43133	177633073161		555571234300	171634031322	173423576154	175422527513
	ĭ	201423026515	26515	577631513562		154434424000	571633127720	573424104515	575422727424
3/ 1/64 726,39095	ĭ	661423313701	13701	177630723356		555631434000	171631665327	173423761420	115422527343
	ĭ	201423175471	15471	517627337737		155757300000	571631005362	573424265753	575422730620
3/ 1/64 830.16116	Ĭ.	601423465601	65601	177626553451		555535660000	171627505456	173424136375	175422525727
3/ 1/64 882-04481	I	201423344157	44157	577625157746	-	156523714000	571626600054	573424431146	575422733050
3/ 1/64 933.93166	£	601423640727	40727	177624400504	1	556610614000	171625301653	173424271447	175422523710
3/ 1/64 985.81609	E.	201423524335	24335	577623000610		156555322400	571624342556	513424562105	575422734355
THE FOLLOWING POINT	SAR	E FOR SA	TELL ITE	POINTS ARE FOR SATELLITE NUMBER 2.(2)	(17)				
	İ	i	!		)	i			
MM 00000 007 34/8676	3	344766374341	3000	001011201100		000000000000000000000000000000000000000	1000000000		

Figure 5-31 Sample TRACE-D Program Tracking Listing (Continued)

Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

1 15060-00 1 15115-00 1 15115-00 1 15115-00 1 15130-00 1 15130-00 1 15130-00	1 15145-00 1 15160-00 1 15160-00 1 15745-00	1 15760.00 1 15760.00 1 15760.00	1 15815.00 1 15815.00 1 15815.00 1 15830.00	1 15830-00 1 15830-00 1 15845-00 1 15845-00	1 15860.00 1 15860.00 1 15860.00	1 15915.00 1 15915.00 1 15915.00
0.3757E-01(HA)	0. -0.7938E-01(HA) 0. 0.1610F-01(HA)	0. 0. -0.3839E-02(HA) 0.	0.3886E-01(HA) 0.	0.1977E-01(HA) 0. 0. -0.2127E-01(HA) 0.	0. 0.1353E-01(HA) 0.	0. 0. 0.
0. -0.5321£-01(70) 0. 0. -0.1647E-02(70)	1 1	1 7	0.5053E-01(TD) 0.	0.8073E-01(TD) 0. 0.7116E-01(TD)	0. 0.4641E-01(TO) 0.	0. 0.4375E-01(10) 0.
0.4637E-01(V) 0.4637E-01(RD) 0.4627E-01(R) 0.1369E-01(V) 0.3758E-01(RD) 0.3758E-01(RD) 0.3758E-01(RD)	-0.1243E-01(V) 0.5286E 01(RD) 0.1049E-00(TR) -C.1187E-01(V) 0.1881E-01(TR)	-0.4653E-02(V) -0.5319E 00(RD) -0.2135E-01(TR) -0.4479E-02(V)	-0.2855E-00(RD) 0.8042E-01(TR) -0.4324E-02(V)	-0.1272E-01(IR) -0.4159E-02(V) -0.4499E-01(RD) -0.5855E-01(IR) -0.4012E-02(V)	0.1855E-03(RD) 0.3751E-01(TR) -0.3868E-02(V)	0.4016E-001RD) 0.2804E-011TR1 -0.3728E-02(V)
0.1490E-01(U) 0.9983E-01(E) 0.4493E 04(2) 0.1497E-01(U) 0.2773E-01(E) 0.5772E 04(2) 0.1503E-01(U)	0.1509E-01(U) -0.9759E-02(E) 0.5583E 04(Z) 0.1515E-01(U) -0.9913E-01(E)	0.1655E-01(U) 0.3050E-00(E) 0.2495E 04(Z) 0.1662E-01(U)	0.8375E-01(E) 0.9956E 0312) 0.1668E-01(U) 0.1649E-00(E)	0.4381E 04(2) 0.1674E-01(U) -0.1285E-00(E) 0.4211E 04(2) 0.1680E-01(U)	0.6657E-01(E) 0.2717E 04(Z) 0.1686E_01(U)	-0.1212E-00(E) 0.4346E_04(Z) 0.1692E-01(U)
0.2530E-01(GD) 0.2530E-01(A) 0.1594E 04(Y) 0.2734E-02(GD) 0.8941E 03(Y) 0.4209E-01(GD) 0.4209E-01(GD)	-0.3702E-02(GD) 0.1381E-06(A) -0.3502E 03(Y) 0.428E-01(GD) 20.1491E-06(A) 0.4925E 03(Y)	0.4652E-01(GD) ECITED 0.1017E-0C(A) 0.1840E 02(Y) 0.7015E-01(GD)	0.6352E-03(A) 0.2697E 04(Y) -0.9521E-01(GD; EDITED	0.29/4c 04(1) -0.8696E-02(GD) EDITED -0.1102E-00(A) 0.2948E 04(Y) 0.3199E-01(GD)	-0.1633E-00(A) 0.2332E 04(Y) 0.2856E-01(GD)	-0.1007E-00(A) 0.2446E 03(Y) 0.3849E-01(GD) EDITED
0.3310E-01(GR) -0.3418E 04(R) -0.434E 04(R) 0.3597E 04(R) -0.3673E 04(X) -0.3673E 04(X)	04(X) 04(X) 04(X) -01(GR) SICUAL 04(R)	-0.7967E-01(GR) RESICUAL -0.6715E 04(R) -0.5170E 04(X) 0.8947E-01(GR)	.619E 04(R) 683E 04(R) 619E-01(GR) RESIDUAL 6519E 04(R)	-0.6355-01(GR) 0.3793E-01(GR) (R) RESIDUAL -0.6394E 04(R) -0.2876E 04(R) -0.2109E-01(GR)	2082	-6537E 04(R) -6661E 04(X) -1104E-01(GR) RESIDUAL
6675,0000 6675,0000 6675,0000 66875,0000 66890,0000 66890,0000	6705,0000 6720,0000 6720,0000 6720,0000 FCLJDNIAG ( FCLJDNIAG ( 7065,0000	7065-0000 FCLLOWING ( 7080-0000 7080-0000	7095.0000 7095.0000 7095.0000 FOLLOWING (	7110.0000 7110.0000 7125.0000 7125.0000 7125.0000	7140.0000 7140.0000 7140.0000 FOLLOWING (	7155.000 7155.000 7155.000 FOLLONING (
88888888	88888	2 222	222 2		***	**

Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

(

	TYPE		(E)			(5)	(E)		(E)		(E)	
	RMS	SHS/S16	0.113480E-00	0-113480E 01		0-13C768E-00			0.202472E-00		0.430031E-00 0.430031E 01	
	×		84			72	85		23		96	
	TYPE		(A)		(X)	3	8	(X)	3	(X)	(8)	(X)
(£)	) S#S	RNS/SIG	0-922048E 00	0.922048E, 01	42 0.659534E 04 0.659534E 01	0.109016E-00	0.601024E 00 0.601024E 01	0.171160E 05 0.171160E 02	0.750748E 00 0.750748E 01	0.163137E 05 0.163137E 02	0.480115E-00 0.480115E 01	0.225802E 05 0.225802E C2
	×		92		24	27	885	*	[2]	23	89	33
	TYPE		(R)		(80)	(8)	(%)	(RD)	(R)	(RD)	(R)	(RD)
	RMS	RMS/S16	0.117125E 04	0.117125E 02	0.212510E 02 0.212510E 02	0.139140E 03		0.113003E 02 0.113003E 02	0.404818E 03	000	0.492022E 03	0.0
\ {	Z,		57		42	27	9	45	1	0	58	0
	STAT		VV		AA	38	ນ	23	EE	FE	7.5	F.F.

Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

	NERE USED IN THE SOLUTION (19) IS BEST SO FAR (29)	\$1	DELTA	0. 0.8999999 02 0.34499999E 03 0.24010739E 08 0.2	0.0999999E-02 0.83169469E 02 0.
(B)	ERE USED IN THE BEST SO FAR 29	ION IS		03 0.	
	2156 DATA POINT CURRENY SOLUTION	CURRENT SOLUTION	ALPHA	30 0.15882923E 0	(0.09999999E-03

Figure 5-31. Sample TRACE-D Program Tracking Listing (Continued)

Figure 5-31. Sample TRACE-D Program Tracking Listing (Concluded)

Table 5-14. Tracking Output Listing Description

		Page
Item	Description	Reference
1	Permanent-station information. The six columns from left to right contain station identification, weighting sigma index number, geodetic latitude of station, longitude of station measured east from Greenwich, and height of station in feet above mean sea level.	3-5 5-32/5-34 5-62
	If temporary stations are present, corresponding information is printed immediately preceeding the observations for the appropriate block (see Item 2).	5-34, 5-35 5-67, 5-68
2	Observation time. The month, day, hour, minute, and second of an observation are associated with the set of values appearing in the same line. The year is assumed to be the same as that of epoch day.	5-35/5-37
3	Station identification. If pass identification (observation-card columns 3 and 4) is used, the characters entered will appear to the immediate right of the indicated letters.	5-35/5-37
4	Observation set number. The integers in the indicated column designate which specific observation types are represented by the measurements given on that line (see Item 5).	5-37
5	Observations. The specific observation type is indicated by the set number (see Item 4). For example, the last line on the first page of Figure 5-31 contains range, azimuth, and elevation measurements.	3-13/3-20 5-35/5-37
6	End of flock. This break in the listing of observations indicates that a TF card has been encountered by the TRAIN link input routine. If temporary stations are present in any flock, the corresponding station-location and-identification information is printed immediately preceeding the observations in that flock.	5-35/5-38 5-63

Table 5-14. Tracking Output Listing Description (Continued)

Item	Description	Page Reference
7.	Satellite identification. A message such as the one indicated is printed when the input routine encounters a TT card in the observation deck. Satellites are numbered sequentially as the corresponding observations are encountered in the input deck.	5-18, 5-19 5-22 5-66
8	Indication of the quantities (parameters) to be differentially corrected, which in this case are $\alpha$ , $\delta$ , $\beta$ , A, r, and v for Satellite No. 1, thrust amplitude and time constant for Satellite No. 1, $\alpha$ for Satellite No. 2, and $\alpha$ for Satellite No. 3.	2-7 3-70 5-13, 5-14 5-22, 5-23
9	Flock count. If a binary data tape is used to input the observations, this count should be ignored.	
10	Card image of the END card following the observation cards in the input deck.	5-67
11	Differential correction bounds. This sequence corresponds to the previously described sequence of the parameter indications (see Item 8).	2-11 3-70, 3-73 5-24
12	Weighting sigmas. The observation type number and the value of the weighting value are shown. For example, observation Type 19 corresponds to range rate and the assigned weight is one foot per second. Sigmas are entered for observation Types 1, 2, 3, and 19 only. A weighting sigma of zero is automatically applied to the other types of observations entered, which has the effect of excluding them from the least squares process (i.e., they are given zero weight).	2-7 3-70, 3-71 5-26, 5-27
13	Initial conditions for additional satellites. If more than one satellite orbit is defined, the ADBARV quantities at epoch for the additional orbits will appear at this location.	5-18/5-22

Table 5-14. Tracking Output Listing Description (Continued)

Item	Description	Page Reference
14	Gravity field indices for partials computation. These integers define the highest-degree and -order terms of the gravity-field expression that are to be used in the variational equations (see Table 5-12, Item 23).	3-52/3-54 3-60/3-62 Appendix F
15	T-matrix indicator. The disposition of the variational equation T-matrix term option is indicated at this point.	3-53 5-6 Appendix C
16	Definition of current orbit. For each iteration the current values for the parameters are used to compute the quantities shown (see Table 5-13, Items 8 through 10).	3-4 3-11, 3-12 3-63/3-66 5-97, 5-98
17	Node print. Each time the integrated trajectory crosses the equator (as determined by interpolation between integration steps) the date, time in minutes from midnight of epoch, and the rectangular elements (x, y, z, x, y, z,) in units of earth radii and earth radii per minute are printed in the octal mode. All output by the FITA link is in sequence by time for each satellite. The numerical integration interval for each satellite begins at epoch and ends at the time of the latest observation for that satellite. A message is printed each time any of the events of equator crossing, start of thrusting, end of thrusting, or orbit adjust are detected during the integration interval	3-63 5-5
18	Thrust start message. This output indicates the beginning of a thrusting interval for the satellite whose motion is being integrated.	3-51 5-8, 5-9
19	Thrust resultant. During the thrusting interval the thrust magnitude at the time of node crossing is printed on the line following the nodal elements.	3-51 5-8, 5-9
20	End of thrust message. No thrusting will be included in the equations of motion after the time appearing at this point.	3-51 5-8, 5-9

Table 5-14. Tracking Output Listing Description (Continued)

Item	Description	Page Reference
21	Satellite-number message. Integration of equations of motion for several satellites is performed serially, wherein the complete jectory for Satellite No. 1 is integrated, the complete trajectory for Satellite No. 2, etc. message indicates that integration of the ecof motion for Satellite No. 2 is starting and the node prints following apply to that satellites.	en the This tuations that
22	Station identification and system time of re These are to be associated with all residua which appear on the same line. It should be noted that system time is defined as second from midnight of the current day.	ls e
23	Residuals. These are unnormalized difference between the input observations (as modified bias or refraction corrections) and corresping values for the same observation types computed from the integrated trajectory poat the observation times. Up to six residuate the same time are printed on one line. The vation type is indicated in parentheses immediately to the testing the residual value in each case, that residuals appear for the unweighted as as for the weighted observations.	3-70 3-76, 3-77 5-8 sition als for e obser- ediately Note
	Identification of the foregoing observation- indicators with observation descriptions or defined elsewhere in this report is in accor with the following:	symbols
	Indicator Description or Symbol	<u>Unit</u>
	R Range A Azimuth E Elevation TR Topocentric right ascension	ft deg deg deg

Table 5-14. Tracking Output Listing Description (Continued)

Item	D	escription	,	Page Reference
23 (cont)	Indicator Desc	ription or Symbol	Units	
	HA Topocer GR Geocent GD Geocent U Horizon V Horizon angle H Altitude X X Y Y Z Z R Range P Range d Q Range d	ifference ifference	deg ft ft ft ft ft ft ft ft	
		ate cate difference cate difference	ft/sec ft/sec ft/sec	
24	in terms of seconds alternate form, whe the hour and minute	The time identified in Ite from midnight is given arein the day of the month of the day are given as is are given to two decing	in h and	
25	deletes an observation shown is printed. I included in the least	Thenever the residuals edion, a message such as the indicated residual is the considered but will be reconsidered.	he one not e	5-28
26	of the residuals for each station is compand the result is praction identified included in the RMS	esiduals. The root-mean each type of observation puted by the residuals ed inted at this location. In tification, number of res (i. e., the total number eminus the number delet	from itor cluded iduals for	5-28

Table 5-14. Tracking Output Listing Description (Continued)

Item	Description	Page Reference
26 (cont)	the editor on this iteration), the RMS, and the RMS divided by the input weighting sigma. The observation-type indicators are the same as those used in the residuals print output (see Item 25). Units are feet, degrees, and seconds. Interpretation of the boxed printout area of the Item-28 sample output should be that twenty-three azimuth observations from station EE passed the residuals editor and were included in the least-squares process. The root-mean-square of these residuals is 0.753981 degree, which is 7.53981 times the sigma input for weighting azimuth observations from station EE (input sigma = 0.1 degree).	
	A restriction associated with the residuals editor is apparent if the summary information is compared to the detailed residuals print described in Item 25. Only five observation types for some stations are represented on the summary output, whereas more than five types were used in the fit. Because of storage capacity constraints, the residuals editor will accumulate residuals and perform editing checks for only the first five observation types encountered for each station.	
27	Iteration number. TRACE-D performs the tracking, or orbit determination function, by computing series of differential corrections to the parameters selected by the user. The iteration number is advanced each time the process of computing a set is repeated. The number may be interpreted as an indication of the number of times the trajectory-integration/least-squares process has been performed.	2-9 3-77 5-28
28	Observation count. The number of individual observations included in the current least-squares computation is indicated.	1

Table 5-14. Tracking Output Listing Description (Continued)

Item	Description	Page Reference
29	Convergence indicator. If the weighted RMS for all residuals for the current iteration is less than that for any previous iteration, then the fitting process is converging and the message shown is printed. If the RMS obtained on the current iteration is greater than the smallest RMS obtained on previous iterations, the message  CURRENT ITERATION IS NOT GOOD	2-9 3-77
	(RMS = C. xxxxxxxx xx)	
	is printed in this position.	
30	Current solution. If the iteration is successful (i.e., the overall RMS has been lowered), indicated values are the parameter values used in the trajectory, partial derivative, and residuals computations which have just been completed. In the case of Iteration No. 1, they are the input values of the parameters.	3-77
	If the iteration is bad, the words	
	GO BACK TO	
	are printed, and the values of the parameters which so far have produced the lowest RMS are recovered from memory and printed at this point. Parameter names are generally self-explanatory, with the possible exceptions of the multiple-vehicle elements. The satellite number is printed before the element name for Satellites 2 through 6. In the case of the boxed printing on the Item 30 sample output, the parameter is right ascension of Satellite No. 2, where units are feet, degrees, and seconds.	
31	Current solution in octal digits and machine units. These numbers corresponding to those described in Item 30 are given both in the octal mode and in the units used for internal computations. Use of these quantities permits bypassing units and number-system conversions during input and output.	5-5

Table 5-14. Tracking Output Listing Description (Continued)

Item	Description	Page Reference
32	RMS. This is the quantity which is to be minimized in the tracking or orbit determination process and is the root-mean-square of the nor-malized residuals included in the least-squares calculations on the current iteration.	2-9 3-76, 3-77
33	Corrections. The result of solving the system of normal equations associated with the current iteration. Each correction is associated with the parameter which occupies the corresponding position in the current solution block (see Item 30). Units are feet, degrees, and seconds.	3-73/3-76
34	Bounds. Current values of the numbers used to limit the size of corrections. In general, these bounds are automatically increased on a good iteration and automatically decreased on a bad one.	2-11 3-73 5-24
35	Bounding indicator. This message will be either	3-72/3-76
	HITTING BOUNDS	
	or	
	NOT HITTING BOUNDS	
	The first message indicates that the magnitudes of the corrections have been controlled by solving the system in such a way that the constraint implied by the bounds is satisfied, and the latter that the nor- mal equations have been solved without applying the bounds.	
36	Next solution. Each value is the sum of the parameter value given in the corresponding position under "current solution" and the associated correction. These are the parameter values which will be used for the next iteration.	,
37	Next solution in octal mode and units of earth radii, radians, and minutes. (see Item 31).	5-5
l		

Table 5-14. Tracking Output Listing Description (Concluded)

Item	Description	Page Reference
38	Predicted RMS. If the fitting process is converging in a completely linear fashion, this will be the RMS on the next iteration. The comparison of this number with the current RMS (see Item 32) may be used to measure the degree to which the process has already converged.	2-9 3-76
39	Sigma of parameters divided by sigma of the normalized observations. The numbers given are the square roots of the diagonal elements of the inverse normal matrix. If certain assumptions are made about the characteristics of the observation set, the numbers may then be taken as the variances on the parameter solutions.	2-17 3-76
40	Correlation matrix, correlation coefficients for the parameter set. These values are computed directly from the covariance matrix (i.e., the inverse normal matrix). Rows and columns are in the same sequence as in the Item-39 block.	3-78

## 5.5.4 Data Generation Output

Listed output produced by a typical data generation run is shown in Figure 5-32. Supplementary descriptive information relating to the indicated areas of this listing is annotated in Table 5-15.

RERERERE + +++  REPRERERE + AAAAAA  RERERERE + AAAAAAA  REPRES + AA  HONTH DAY TZONE H  ANTA  LEPTA - CONE H  ANTA - CONE H					***	***				
REPRESENCE   A					:		*			
RR RRRRRRR	TITI	TTTSTTT	RRRRRR	RRR	*	¥	+	ວວວວວວວວວວ	EEEEEEEE	
RRRRRRRR	TITT	rrrrrr	RRRRRR	RRR	+	AAAA	+	כככככככככ	EEEEEEE	
RRRRRRRR + AAAAAAAAA + CC RR RR + AAAAAAAAA + CCCCCCCCC RR RR + AA AAAAAAAA		11	<u>«</u>	<b>K</b>	+	AA AA	+	ដ	ינט	
RR RR + AAAAAAAA + CC RR RR + AA AAAAAAA CCCCCCCCC RR RR + AA AA AAAAAAA CCCCCCCCCCCCCCCCCC		11	RRRRRR	RRRR	+	44 44	÷	ປູ	EFEEEE	
RR RR + AAAAAAAAAAAAAAAAAAAAAAAAAAAAAAA		11	RRRRRR	18.88	÷	AAAAAAAAA	*	ບູ	EEEEEE	
RR RR + AA AA + CCCCCCCC RR + AA A + CCCCCCCCCC  + + + + + + + A00140  2-23-65  NITA  WITA  AA + CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC		11	RR	88	+	TAAAAAAAAA	+	CC	EE	
## ## ## ### #### ####################		<b>.</b>	9	0	*	44	4	200000000	255555555	
### ### ### #### ##### ###############		::				**	٠ 4			
2-23-65 +++ +++ +++ +++ +++ +++ +++ +++ +++ +			7	44		-	ا.	22222222		
2-23-65 HONTH DAY TZONE HOUR HIN 00. G. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.					•	•	٤			
2-23-65 2-23-65 #ONTH DAY TZONE HOUR WIN 2. 23. 0. 0. 6. 0					<b>†</b>					
2-23-65  #ONTH DAY TZONE HOUR WIN 2. 23. 0. 0. 6. 0					Ť		*	100140		
2-23-65 HONTH DAY TZONE HOUR NIN 2- 23- 0- 0- 0- 0 NITA						****	æ	REFERENCE		
NITA  2-23-65  40NTH DAY TZONE MOUR HIN  0-6-0  0-10-10-10-10-10-10-10-10-10-10-10-10-10			1	!						
MUTH DAY TZONE HOUR HIN 2. 23. 0. 0. 6. 0	BIT I DATA	SENERATION	2-23-	65						
YEAR HONTH DAY TZONE HOUR WIN 1965. 2. 23. 0. 0. 6. 0 RING LIM MO. 3 INITA										
YEAR HONTH DAY TZONE HOUR HIN  1965. 2. 23. 0. 0. 6. 0  RING LINK HO. 3 INITA										
RING LIMK MO, 3 INITA	HOCH	YEAR	HONTH	DAY	TZON		N I K	SEC		
NIERING LINK MO. 3 INITA		1965.	2.	23-	Ö		ં	•		
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	NTERING LIM	K NO. 3 IN	IITA							
								***************************************		
	Section 200									
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Figure 5-32. Sample TRACE-D Program Data-Generation Output Listing

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IS 103.01/1000. The INPUT CARD FINE INPUT CARD		1 TABLE 3 -1000000E-00 4 -5000000E-01 5 -5000000E-01 6 -5000000E-01	8 .5000000E-01 13 .1000000E 04 14 .1000000E 04 15 .1000000E 04 19 .1000000E-00	INITIAL CONDITIONS				* 0.21533352E 08 U* * 0.25567859E 05 T* -	CCA/W = 0.09999999E-01 W/CDA = 0.9999999E 02	EARTH HODEL 99E-02 J3# -0.26930000E-05 J4# -0.15600000E-05 J5# -0.5999999E-08	152= 0.5329000E-07 L52= -0.20	02 J53= 0.58419999E-08 L53= -	01 J54= 0.40929996-08 L54= 0.58250000E	J55* 0.84620000E-09 L55* -0.15320000E	02 J61= 0.66110000E-07 L61=	03 J62* 0.37459999E-07	02 J63* 0.11660000E-07 L63= -	-0.10999999E O1
Q <u>01,0188 RBIAS Q3,01,1000.</u> ON 2-23-65		SIGMA TABLE 2 .1000000E-00 3 .1000000E-00	000E-01 13 .1000000E 04 14	INITIAL	ALPHA=	DELTA	651A # A2 **	# # <b>*</b> >	CCA/W = 0.09999999999999999999999999999999999	0-10827599E-02	121= 0-		131=	L32= -0.13330000E	L33* 0.1600000E		142= 0.2746999E	L43= -0.10999999E
LRAPAROS, 99 QOI. END. GRBIT I DATA GENERATION	BOUNDS 0.	1 .1C00000E 03 2 .1000	7 .50000000E-01 8 .50000		-0.10055931E 07	■ 0.21509859E 08	Z * 0. ******* -0.10793655F 05		ATHOSFHERE - LOCKHEED	1	121 0 0 2 121	32% 0.1723000E-05				341 = 0.72780000 E-06	ı	J4:3= 0.57190000E-07

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

JS1= 0+15090000E-06	LS1= -0.81	L510.8185999E 02	J66= 0.51530000E-10	L66= -0.14340000E 02	00E 02
THE FOLLOWING BODIES ARE USED FOR PLANETARY PERTURBATIONS	USED FOR PLANE	TARY PERTURBAT	IONS		
NONE			,		
FORMULATION COMELL (EQS.OF MOTION)	JE KOTION J				
DIFFERENTIAL EQUATION SUBROUTINE GAUSS-JACKSON	ROUTINE E BAR=	0-1000E-09		RATIO OF COVELL STEP TO RUNGE KILLTA	UNGE KUTTA 4
STEP SIZE - INITIAL* 0.1000E 01 MI DO NOT RECOMPUTE PERTURBATIONS FOR CORRECTOR	0.1000E 01 NATIONS FOR COR	MINIMUM=	0.156 E-01 MAXIMUM=	JM= 0.6400E 02	1
EQUATIONS OF MOTION USE	USE NI = 9 NZ= 6				
	!	CON	CONSTANTS		
9	DECIMAL	OCTAL		DECIMAL	OCTAL
	0.43752695E-02	171436571536	E C	0.55304505E-02	171552343100
ALPRA G	U. 2664 7102E 01	20222022346			
		214632063602	RAKIH KAULUS J. FI	0.20925741E 08	2314/1232264
ANCE		231477232264	I-0. VELOCITY		223524455115
	0.32173999E 02	206401310550	FT/SEC//E.R./N.N.	0.34876230E 06	223524455115
	0.10471976E 01	201414052221	1/EPS.	0.29830000E 03	211452231463
E MASS (SUN)	0.33295130E 06	223505113515	(MOOM)	0-12299900E-01	172623026050
(VENUS) 0.8	0.81497900E 00 0.31788700E 03	200641211666 211475706312	(MARS) (Saturn)	0.10782100E-00 0.95129000E 02	175671505015 207574410142
ENTERING LINK NO. 4 INITS	178				
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Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

AA -00. 75.00000000  EC -00. 0. 0.  EE -00. 0. 0.  EF -000. 0.  A SEC. DEG. DEG. DEG. CORECTED  BB RBIAS  DATA TYPES  S RANGE AZMTH ELEV. R.DO  A SUR.R HIGHT DOPLR LOOK  A SUR.R HIGHT DOPLR LOOK  A SUR.R HIGHT DOPLR LOOK  BB X X X X X X X X X X X X X X X X X X		LONGITUDE	HE	нејсит			
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TA  INTERVAL  IS-0	315.000000000		500.000				
TA  INTERVAL HIN.EL HAX.E  SEC. DEG. DEG. DEG. 15.0  15.0 -000. 15.0  15.0 -000. 15.0  15.0 -000. 15.0  15.0 -000. 15.0  15.0 -000. 15.0  15.0 -000. 15.0  15.0 -000. 15.0  15.0 -000. 15.0  15.0 -0000. 15.0  15.0 -0000. 15.0  15.0 -000000. 15.0  15.0 -000000000		135-000000000		200-0000			
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¢	×			<b>&gt;</b>	>	>	7
RE X X	×						

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

VG GAINA. LINK 9  VG GAINA. LINK 9  VG GAINA. LINK 9  VG GAINA. LINK 9  AT 0.889068886 02 HHE. 574611226466 201407112565 000000000000 573773036372 567573220611  AT 0.122089476 03 HHE. 5746112264673 60140667324 15510626000 173773036372 567573220614  AT 0.122089476 03 HHE. 574637210 1745 56140667524 15570626000 173773230066 5677732201346  AT 0.220159956 03 HHE. 57464725335 60140067675 155466000 173773230066 56777121201340  AT 0.220159956 03 HHE. 5746472535 6014067676 15 1546262000 173774062520 167771620  AT 0.220159956 03 HHE. 5746472500 20140718444, 1554652000 1737740625 167771620  AT 0.220159956 03 HHE. 5746472700 2014071844, 1554652000 17377406250 167771620  AT 0.220159976 03 HHE. 5746472700 2014071844, 1554652000 17377406045 1677711620  AT 0.220159976 03 HHE. 1744230120 2014071844, 1554652000 17377406045 1677711620  AT 0.220159976 03 HHE. 17742714513 20140728473 1554746000 17377406045 16747116645  AT 0.4201976 03 HHE. 1774714513 2014072846 5544130000 17377410420 16774716545  AT 0.4201976 03 HHE. 177471416776 2014074057 1544130000 17377416220 16674272015  AT 0.44021976 03 HHE. 177471416 03 HHE. 17747177717777777777777777777777777777	C GAINA. LINK 9					<b>&gt;</b>	<b>&gt;</b> -	<b>&gt;</b>	<b>&gt;-</b>	ر •«	(
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AT 0.10125195E 04 MME. 5625.4404,210,601406775031, 1547330,6000, 1737743,81214,35,60444276000. AT 0.10565304E 04 MME. 170467514705 201407244136 55650101400 573773602530 163450471320. AT 0.1106396E 04 MME. 571444463510 601406777171, 156404530000 17377427416 56434260420. AT 0.118895535E 04 MME. 57143452537 6014067233556, 55555150000 57377425467 56542372711. AT 0.12325617E 04 MME. 172540776562 20140722073 55550410000 573773555070 165523562113. AT 0.12325617E 04 MME. 172540776562 20140674675, 156547654000 17377425452 56525641375. AT 0.13205701E 04 MME. 17254073533 20140674675, 156547654000 57377355470 1665723562113. AT 0.1345724E 04 MME. 1775130535 201406737715 556643204000 57377355470 5654564137260. AT 0.13457749E 04 MME. 17775130004, 201406731751 155707740000 5737735447 1664556034251.	AT 0.10125195E 04 MME. 56554464110 601406775031 154733060000 173774314164 56044471600000000000000000000000000000000		0.9	03 1	S		555656400000	573773603		5474460	17542014436
AT 0.10565304E 04 MME. 170467514705 201407244136 556501014000 573773602530 163450471320 AT 0.11056394E 04 MME. 571644463510 601406771171 156404530000 17377427416 564434260420 AT 0.1145484E 04 MME. 571644463510 601406771171 156404530000 5737737427416 564434260420 AT 0.1188553E 04 MME. 572633522537 601406762012 156520160000 57377355450 5654227771134 AT 0.12325617E 04 MME. 572640352237 601406762012 156520410000 573773555070 165523562113 AT 0.1276561E 04 MME. 57264435302 60140674575 156547654000 17377424532 56526541372 AT 0.13205701E 04 MME. 57364435302 60140674675 155777554000 573773534452 165730217260 AT 0.1365774E 04 MME. 573426555023 601406731571 155707740000 57377353447 1664556034251	AT 0.10565304E 04 MME. 170467514705 201407244136 556501014000 573773602530 163450471320 AT 0.11005394E 04 MME. 871444645310 601406711171 156404530000 173774274116 56447260420 AT 0.11005394E 04 MME. 871444645310 6014067717171 156404530000 173774274116 564427260420 AT 0.12325617E 04 MME. 87243352537 601406762012 156520160000 173774254576 565422372711 AT 0.12325617E 04 MME. 8724395302 501407222073 55650410000 573773555070 165523562113 AT 0.13205701E 04 MME. 87244345302 60140674757 156547654000 173774242532 565525641372 AT 0.13205701E 04 MME. 87342655023 601406720773 1556643204000 573773534452 165730217260 AT 0.13267746 04 MME. 87342655023 601406731571 155707740000 173774247301 566415510070 AT 0.13645724E 04 MME. 87342655023 601406731571 155707740000 173774247301 566415510070 AT 0.136457446 04 MME. 87342655023 601406731571 155707740000 173774247301 566415510070	- 1	9-10125195E	쇰	٠;	- 1	.154733060000	173776312	- 1	<b>4276000</b>	57542043170
AT 0.11005396E 04 MME. \$7144463510 601406771171 156404530000 173774274116 564454260420  AT 0.11445484E 04 MME. \$71464711650E 201407233556 555655150000 573774274116 564454260420  AT 0.11885535E 04 MME. \$7243352537 601406762012 156520160000 173774254576 56552372711  AT 0.12325617E 04 MME. \$7243352537 6014067222073 55650410000 573773555070 165523562113  AT 0.12765661E 04 MME. \$724465502 20140722073 55650410000 573773534452 165530217260  AT 0.13205701E 04 MME. \$73426555023 601406746755 1565476440000 573773534452 165730217260  AT 0.13667749E 04 MME. \$73426555023 6014067174706 556474440000 57377353447 1664556034251	AT 0.11005396E 04 MME. \$7164463510 601406771171 156404530000 17377427416 56454566420 AI 114454584646 4 MME. I7657116056 201407233556, 55555150000 17377427416 56454566420 AI 0.11885538 04 MME. \$72633522537 601406762012 156520160000 5737752547654067 1645352777124 AT 0.12325617E 04 MME. 172540776502 20140722073 55650410000 573773555070 165523562113 AI 0.12325617E 04 MME. 172540776502 201407207751 55650410000 57377355457 16550241375 AI 0.13265701E 04 MME. 172751730535 201407207751 556643204000 57377354452 165730217260 AI 0.13665724E 04 MME. 573426555023 601406731571 15570774000C 173774247301 566415510070 AI 0.14085749E 04 MME. 173471510004 201407174706 55647440000 57377353447 166458034251		0.10	6	•		556501014000	573773602		0471320	17542015321
AT 0.114454846 04 MME. I71657116056 201407233556 555655150000 5737735745047 1646352777.34 AT 0.118855535 04 MME. 87243352537 601406762012 1565201600000 173774254576 565422372711 AT 0.123256176 04 MME. 8724345770 20140722073 556506410000 573773555070 165523562113 AT 0.12765461E 04 MME. 872446745702 20140722073 556506410000 57377355070 165523562113 AT 0.13205701E 04 MME. 87242655023 60140674575 156547654000 573773534452 165730217260 AT 0.13657214E 04 MME. 873426555023 6014067317711 155707740000 57377353447 1664556034251	AT 0.11445484E 04 NME. IZ1657116056 201407233556 55555150000 573773574067 1646352777.354   AT 0.11885553E 04 NME. 57243352537 601406762012 156520160000 173774254576 56542277211   AT 0.12325617E 04 NME. 57243352537 601406722073 556504100000 573773555070 165522372711   AT 0.1326561E 04 NME. 57264634536202 60140674075 556506410000 573773555070 165523562113   AT 0.13205701E 04 NME. 172751730535 201407207751 55643204000 573773534452 165730217260   AT 0.13645724E 04 NME. 573625023 601406731571 15570774000C 173774247301 56445510070   AT 0.14085749E 04 NME. 57342655023 601406731571 15570774000C 173774247301 56445510070   AT 0.14085749E 04 NME. 172471510004 201407174706 556474460000 573773534147 166456034251.		0.11	6				173774274		4260420	57542043412
AT 0.11885553E 04 MME. 572433522537 601406762012 156520160000 173774254576 565422372711 AT 0.12325617E 04 MME. 172540776502 201407222073 556506410000 573773555070 165523562113 AT 0.1232651E 04 MME. 172544345302 601406746755 156547654000 173774242532 56525644372 AT 0.13265701E 04 MME. 17275173033 201407207751 556643204000 573773534452 165730217260 AT 0.1365774E 04 MME. 573426555023 601406731571 155707740000 57377353447 166456034251	AT 0.11885553E 04 MME. 572433522537 601406762012 156520160000 173774254576 565422372711 AT 0.1232561TE 04 MME. 172540775622 201407222073 556506410000 573773555070 16552362113 AT 0.12765661E 04 MME. 572644345302 60140676755 156547654000 173774242532 565654541375 AT 0.13205701E 04 MME. 172751730535 201407207751 156547654000 57377353452 15676541375 AT 0.13265701E 04 MME. 172751730535 201407207751 15564764000 173774247301 566415510070 AT 0.13645749E 04 MME. 573426555023 601406731571 155707740000 173774247301 566415510070 AT 0.14085749E 04 MME. 173471510004 201407174705 556474440000 573773534147 166456034251		0.11	04 H		- 1		573773574	- 1	5277.39	17542016071
AT 0.12325617E 04 MME. 172540776502 201407222073 556504410000 573773555070 165523562113  AI 0.12765661E 04 MME. 572644365302 601406746755 156547654000 173774242532 56562644375  AI 0.13465724E 04 MME. 17275130535 20140720775 55643204000 5737735344252 165730217260  AT 0.13467724E 04 MME. 773426555023 601406731571 15570774000C 173774247301 566415510070  AT 0.14085749E 04 MME. 173471510004 201407174700 556474440000 573773534147 166456034251	AT 0.1232561TE 04 HHE. 172540776502 201407222073 556504510000 573773555070 165523562113  AT 0.1275561E 04 AME. 572544345302 601406746755 15657654000 173774242532 565595441375  AT 0.13265701E 04 HME. 1751730535 201407207751 55664320400 17377424352 1655956413726  AT 0.13645724E 04 HME. 573426555023 601406731571 155707740000 173774247301 566415510070  AT 0.14085749E 04 HME. 173471510004 201407174706 556474440000 573773534147 166456034251.		0.11	40				173774254		2372711	575420437331
AT 0.12765661E 04 MME. 572644345302 601406746755 156547654000 173774242532 56562644375. AT 0.13265701E 04 MME. 172751730535 201407207751 55643204000 573773534452 165730217260 AT 0.13465724E 04 MME. 172751730535 20140781571 155707740000 173774247301 566415510070 AT 0.13465724E 04 MME. 173471510004 201407174700 556474440000 573773534147 166456034251	AT 0.12765661E 04 MME, 512644345302 601406746755 156547654000 173774242532 56565641375 AT 0.13205701E 04 MME, 172751730535 201406746755 156547654000 173774242532 565656413750 AT 0.13645724E 04 MME, 172751730535 201407207751 556643204000 573773534452 165730217260 AT 0.13645724E 04 MME, 573426555023 601406731571 155707740000 173774247301 566415510070 AT 0.14085749E 04 MME, 172471510004 201407174706 556474440000 573773534147 166456034251.		0.12325617E	40				573773555		3562113	17542016511
AT 0.13205701E 04 NME. 172751730535 201407207751 55643204000 573773534452 165730217260 AT 0.13645724E 04 NME. 573426555023 601406731571 15570774000C 173774247301 564415510070 AT 0.14085749E 04 NME. 173471510004 201407174706 556474440000 573773534147 166456034251	AT 0.13205701E 04 HRE. 172751730535 201407207751 55643204000 573773534452 165730217260 AT 0.13645724E 04 HRE. 573426555023 601406731571 15570774000C 173774247301 566415510070 AT 0.14085749E 04 HRE. 173471510004 201407174706 556474440000 573773534147 166456034251 THE LYME AND 10 GAIN B		0.127656615	9	S	- 1	~	173774242		6441375	57,542044346
AT 0.13645724E 04 MME. 573426555023 601406731571 15570774000C 173774247301 564415510070 3 AT 0.14085749E 04 MME. 173471510004 201407174706 556474440000 573773534147 166456034251	AT 0.13645724E 04 MME. 573426555023 601406731571 15570774000C 173774247301 56415510070 3 AT 0.14085749E 04 MME. 173471510904 201407174706 556474440000 573773234147 166456034251. THE LYME ND. 10 GAIN B		0.13205701E	ŏ	7		_	573773534		0211260	17542016630
AT 0.14085749E 04 MME. 173471510004 201407174706 556474440000 573773534147 166456034251	AT 0.14085749E 04 MME. 172471510004 201407174706 556474440000 573773534147 166456034251.			0	-		155707740000	173774247		5510070	575420445340
	THE LYMK NO. 10 CAIN B			0				573773534		6034251	175420164300
		FATERING	LYNK NO. 10	CAIN	•						

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continuea,

ļ				FEBRUARY	23.	1965				
ST	ST HR MINS	T-ST	RANGE	AZIMUTH		ELEVATION RANGE RATE	HEIGHT	×	*	7
			NAUT MILES	DEGREES	DEGREES	FT/SEC	MAUT MILES	NAUT MILES	FT/SEC MAUT MILES NAUT MILES NAUT MILES NAUT MILES	IAUT MILES
		·	TOP RT.ASC	TOP DECLIN	GEO RT.ASC	GEO	TOP HR.ANG	Đ	>	
	-		DEGREES	DEGREES	DEGREES	DEGREES	DEGREES	DEGREES	DEGREES	
*	(1) A15E (	-0-	DEGREES ELBY.)		3. HDURS 14.5	14.57 MINUTES	AZIMUTH 1	AZIMUTH 162.149 DEGREES (	ees (I)	
4	£ 14.15	194.75	846.228	159-302	0.951	-7043-192	105.438	1089-054	-1287.258	3113-294
	ľ	,		-13.821	151.773	61.598	338.601	16.039	64.300	
*	3. 15.00	195.00	347.004	155.082	1.067	-5391.049	105,459	1114.292	-1232.523	3126.459
\$	3- 15-25	195.25	819-686	151.011	1.038	-3656-266	105.476	1138-418	-1177.469	3138.609
			171.393	-12.394	155.599	62-396	330.298	78,083	64.483	
Y	3. 15.50	195.50		146.749	1.177	-1861.778	105-487	1163.051	-1122.465	3149-817
				-11.744	15		325.834	79:105	64.563	
4	3. 15.75	195.75	_	142.548		-36.C32	105.493	11,67,225	-1066.650	3160-057
			180.264			63.184	321,602	80.126	A. 635	
V	MAX EL (		1.73 DEGREES ELEV.		HOURS 15.76	2	AZEMUTH 1	42.251 DEGREES	ees(10)	
¥	3- 16-00	196.00	812.689	137.950	1.300	1790.380	105.495	1210-846	-1046.934	3169.426
			184.615	-10.253	161.928	63-523	317-122	81.148	64.700	
4	3. 16.25	196.25	819.345	133.679	1.027	3586.948	105.492	1234.634	-954-779	3177.545
				-9.675	164.182	93.896	312.917	82.170	64.75	
¥	3. 16.50	196.50		129.585	0.899	5325.288	105.483	1257.861	-898.134	3184.642
;				-9.068	166.377	64-095	305.647	83.192	64-808	
4		3. 16.75. 196.75	197-448	125.491	168-699	6982-133	105.470	1280-764	+89-1+8-	3190-900
					1				(3)	
¥	IA SET ( -0. DEGREES ELAPSED VISIBLE TIME =	TALE TIME	DEGREES ELEV.) E = 2.37 /	) 3. MINUTES DU	3. MOURS 16.9 DURING REVOLU	3. HOURS 16.93 MINUTES MINUTES DURING REVOLUTION NUMBER	AZENUTH I	AZIRUTH 122.587 DEGREES []		
Ą	) 3814	ę	DEGREES ELEV.		4. HOURS 42.	42.80 MINUTES	AZEMUTH 2	AZEMUTH 204.539 DEGREES	EEG	
AA	4. 43.00	283.00		201,835	1.262	-15084-742	105.342	552.374	-1572.874	3123.122
			141.000	-13.393	126.090	046-10	164-77	770-01	04.370	
									*	
				,						

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

	1	CEGREES	,			142.342		146.039	149.712	742. 631		157.550		161-553		103.388	162 691	100-601		173.831		177.831	181 473		185.578		189.235		
		HILES			EES	1931-364		1976.949	2021.856	2048, 779		2109.373		2151.769	676	2193-900	202 3255	£633+303	EES	2276.566		2315.695	2255.062	2000	2393,204		2430.938		
	:	NAUT FILES	*	DEGREES	AZIMUTH 149.915 DEGREES	-2762.254	52.207	-2744.715	-2726.279	53.463	54.052	-2687-162	54.617	-2666.542	55.157	060-6497-	279.66	56.172	11.684 DEGREES	-2599.860	56.648	-2576.315	2551 969	57.540	-2526.806	57.959	-2501.454	58.360	
		E RATE X X TEST TEST NAUT FILES NAUT	5	DEGREES	AZEMUTH 1	-1090-609	36.990	-1052.710	-1014.736	39.032	40.053	-937.736	410.14	-898-363	42.095	-828-960	43-116	44.137	AZIMUTH 1	-778.805	45.158	-738.553	671-04	47.200	-657.132	48.221	-615.740	49.242	
1965		ELEVATION RANGE RATE DEGREES FT/SEC	TOP HR.ANG	DEGREES	33.11 MINUTES	-14120.582	318.748	-12858.077	-11429.840	311.546	307.744	-8061.617	303.944	-6135.888	206-662	-40/8-350	295.871	291.893	X	271.301	287.887	2463.264	489-814	280.090	6626.619	276.338	8517.982	272.793	
23,		DEGREES	GEO DECLIN TOP HR.ANG	DEGREES	4. HOURS 33.1	0.878	32.996	1.240	1.757	34-806	35.634	2.728	36.574	2.982	37.362	3.135	38.289	39.105	HOURS 35,24	3.363	39.995	3.512	40.481	41.701	3.038	42.532	2.768	43-380	
FEBRUARY		DEGREES	GEO RT.ASC	DEGREES		147.958	109.567	144.488	140.501	110-878	111.515	131.768	112.203	127.080	112-621	980-221	113.634	114.256	4.	111.505	114.974	106.419	101 - 171	116-521	96.345	117.274	91.364	118.068	
		NAUT MILES	TOP DECLIN GED RT.ASC	DEGREES	DEGREES ELEV.)	824.778	-36.553	791.448	761.435	-31.784	-29.057	713.038	-26.041	695.475	246.22-	082.832	146-61-	-16.126	3.63 DEGREES ELEV.	673.379	-12.566	676-738	1/0.6-	-5.699	699.353	~2.391	718.085	0.611	
		T-ST			,0°	273.25		273.50	273.75	274.00		274-25		274.50	,	214-15	376	77.00	3.63 DE	275.25		275.50	37.75		276.00		276.25		
		Z I Z			RISE (	4. 33.25		4. 33.50	4, 33.75	4. 34.00		4. 34.25		4. 34.50		34.15	200	00.66	MAX EL (	4. 35.25		4. 35.50	34.75		4. 36.00		. 36.25		
		ST HR			9.0	88			88	4	1	98 4	- 1	98 +		20			20	•		88 4	4	1	88 4		.4. 88		,

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

192.675	•	196.048	1	199-385	272 505			!		65.148	1	62.669		24-767	44.480		64-145		63.511		62.133	;	020-19		60-365		244.373		55.432		51-186		74-465	
2468.008		2504-130	,	2539.463	457 4596		200		49	2056.507		2099-878		2142-765	2124.885		2226.701		2257.245		2307.555		2346-718		2385-442		5453.405	1	2459-927		2696.491		2532.969	
-2474.607	58.744	-2447-505	59.112	-2419.195	1300 045	59.801	3396730 687 66		AZIMUTH 228.700 DEGREES	-2134.562	53.932	-2131-219	54.501	-2126,563	2121 919	55.570	-2310.581	56.071	-2110-768	56.551	-2104-604	57.011	-2097.271	57.451	-2090-079	27.5/4	-2082,100	56.278	-2073-326	58.666	-2064-055	59.037	~20540484	のないのない
-574.469	\$0.264	-532.545	51.285	-490-637	200	53.327	ATAMITE		AZEPUTH 2	-1940-195	39.835	-1896-704	40-856	-1852.581	-1808 205	42.898	-1763.305	43.919	-1717.303	44:961	-1671-124	45.962	-1824.229	*6.983	-1577-206	40004	195.9.401	44.025	-1440.860	50.046	-1432-090	51.068	-1383°130	52,089
10248.757	269.272	11809.252	265.908	13198.923	310-307	259.844	27 38 MINITES	TION NUMBER	1.85 MINUTES	-23616.276	58.305	-23518.696	58-405	-23387-964	23212.219	ASS. ON	-22974-130	59.579	-22646.232	60-133	-22186-667	61-102	-21523.695	62-160	-20339.792	635.529	-19030-546	65.673	-16652-285	68.531	-12891-343	72.956	-7261.500	79.613
2.2.9	44.081	1.561	45.035	1.338	2000	46.637	A MOVING 27 3	삪	6. HOURS 1.8	1.222				3.125		38.086		1		39.799			- 1		13.613	45.297	166*91	43-113				44.840	28-972	48.64X
86.916	118.915	82.759	119.763	79.114	107.07	121.565		MINUTES DU		229.047	111.162	230.198	111.813	231-288	744.001	112.104	234.325	113.826	236.636	114.654	239.109	115,385	262.313	116-044	246-467	116.944	25% 205	177.453	260-208	1150479	272.659	119,279	283, E94	130.274
741.304	3.420	768.564	6.093	799.476	200	10.527	OCCUPEC CLEV	4.27	DEGREES ELBV.)	808.543	-26.871	750.361	-25.509	692.458	200-62	-21.012	577-864	-19.827	522.563	-17.339	466.164	-14-441	412-174	** GOU!-	350,172	~2.483	311.206	0.040	266.941	8.077	230.108	18.594	204.817	32.103
276.50		276-75		277-00	. 30 400	630113	1	ELAPSED VISIBLE TIME =	-0. DEG	362.00		362.25	;	362.50	34.5.76	61.706	363.00		353.25		363.50		363.75	•	364.00		354.25		364.50		304075		248,00	
05.96 -4,		4, 36.75		4. 37.00		69-16-1	, ,	ED VISI	RISE (	2.00		2,25		2.50	3,78		3.00	1	3.25		3.50		3.75		4.00	1	4.45		\$.50		40	- 1	3.60	
l l								LAPS		٥		٥			ı	•	\$		\$		۵		3		ċ		4		96 15.		÷		*	, 4
99		8		2		<b>8</b> D		ש מ	2	9		2		80 80		0	60	į	8		98	1	8	;	න ආ	-	(C)		8		33	•	8	

Figure 5-32, Sample IRACE-D Program Data-Generation Listing (Continued)

		-		5 5 6 1						1
	EES	27,798 DEGREES	AZ 2 H93 T H 0.	8.71 HINDIES IOLATSON NUMBER	6. HOURS 8.71 NEWDES Minutes During Revolution Number	le-	DEGRÉES ELEY. IE = 5.86	61.465ED VLSTBLE TINE	527 CB	RH SET Elarsed
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270,998	2893.963	-1896.294	-759-953	23358-677	3-263	540 125	693.45.2	369-60	8,00	ê
		62.415	63.324	213.651	53.958	333.932	44,501			
271.145	2566.501	-1912.102	-613.786	23185.049	4.673	23,263	633,938	367.75	7.75	
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274.322	2814,193	-1942,182	-920-423	22622,261	7,322	29.520	525.747	367.25	7.25	25 A.
			60-260	207,708	31,932	328,321	2000000	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
276.945	2786.040	-1456.876	-973.334	22163,221	3.363	17.102	449 459	273	26 A	2 46
230-774	Z/57.201		-1026.111	21500.205		14 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	417,552	356.33	6.75	ő
		61.227	58.237	197.851	50.388	124-045	57.889	•	ŧ •	
286.412	2727.591	-1984.393	-1078.104	20514.465	13.45%	9.437	259.544	366.30	65.40	38 6.
		60.934	57-155	187.951	49.580	123,030	1000 C			,
296.513	2697.055	-1997.472	-1124,816	19000.539	17.266	34.70	094 FEE	546.34	35.3	1
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		60,039	54.131	113.367	67.261	1220124	60.257	,		;
12.684	2600.560	-2032,653	-1282,659	1133-565	29.143	323.242	204,608	965 59	25.8	1
	un Hu	225120 4218018 309-858 DEGREES	AZIKUTA KIKUTA	S MINUTES	HOURS SALE	124,4270	072.54	₹0.45 DE	¥	ž
	071-0075	276.6402-	-1353. Lyb	-41.0163	30-737	307,538	145.613	345.25	8,42,8	ś

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

E AAIE FF/SEC NAUT MILES NAUT MILES NAWI MILES DEGREES	<b>A</b>	GREES	487.708 180.284		10 (12.238 213.130 14	17 686.099 275.556	5: 55: 55: 55: 5: 5: 5: 5: 5: 5: 5: 5: 5	630000	9 573.941 313.771		6 517.523 319.728	)()  6 460_850 323_724		14 404-135 326-944		11 347.310 329.460		22222	7 233-126 333-843		3 175.881 335.439		0 118-659 337.277	•
NAUT HILE	V DEGREES	AZIHUTH 356.512 DEGREES	851.014	28.078	26-394	902.497	24-652	22.853	953-179	20.998	941.686	1002-196	17.130	1024.254	15-123	1050.231	13.073	10.984	1094.677	8.861	1119.783	6-711	1142.020	4-040
NAUT MILES	DEGREES	AZIHUTH	27)	165.596	•	3351.481	167-643	168-666	3358.535	169.690	3361-101	170°713 3362°193	171.737	3361.922	172.760	3361.070	173.784	174.808	3356.018	175.831	3352-220	176.855	3346.926	F/ (* 8 / 8
ELEVATION RANGE RAIE DECREES FY/SEC	TOP HR. ANG DEGREES	BE. ST HIMUTES	-22929,000	47.83.83. 43. 44. 44. 44. 44. 44. 44. 44. 44. 4	50.400	-22410.595	350.846	323.553	-21529.219	312.637	-20860-770	306.599	302.779	-18711.763	299-645	-16985-163	297.294	295.034	-11306-146	293.010	-7034.212	291.293	-1941-985	510-627
ECEVATION DECREES	GEO DECLIN TOP HR. ANG DEGREES DEGREES	6. HOURS 33.	0.934	13-056	24 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -	2.435	11.271	16.412	4.812	9.374	6-274	7.726	7.511	9.483	£,,628	37.246	5.634	4.615	15-213	3.804	16.785	2.818	17.801	766-1
DEGREES	GED RI.ASC DEGREES		356.522	1000 C	265,475	0,397	266.35%	266.702	4.894	267.201	8.162	11.865	268.143	16.622	268.598	22.677	268-982	269,402	39.354	269.890	50.571	270-260	63.363	*61.00.7
NAUT MILES	TOP DECLIN	DEGREES ELBY.	796-D87	36.937	34.572 88.172	586-386	87-713	85.754	578.222	83.105	525-825	19.832	75.737	427.575	71.005	383.376	464.884	57.537	312.112	48.390	289.274	37.539	278.071	KK7*C7
1-53.		o .0.	392.75	600	37.00.25	393.25	- KOC		353×75		394.00	394.25		394.50		394.75	305		395.25		395.50	1	395.75	1
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Figure 5-32, Sample TRACE-D Program Data-Generation Listing (Continued)

12.680   271.164   0.989   278.083   396.25   294.537   89.108   16.368   8.91.827   324.537   396.50   320.249   397.557   0.911.537   0.911.537   0.911.537   396.50   320.249   399.976   14.660   12.19.934   395.291   395.291   115.586   10.764   17534.603   397.05   395.291   115.586   10.764   17534.603   397.05   395.291   115.586   10.764   17534.603   397.25   440.627   121.002   3.640   19112.583   397.25   440.627   121.002   3.690   19112.583   397.25   440.627   121.002   3.690   19112.583   397.25   480.288   125.585   7.276   2025.2646   397.25   480.288   125.585   7.276   2025.646   397.25   480.288   125.585   7.276   2025.646   397.25   480.288   125.585   4.343   21705.681   398.25   647.47   134.27   2.329   277.215   398.25   647.47   134.27   3.229   2171.97   398.25   647.47   134.27   3.229   2171.97   398.25   647.47   134.27   3.229   2171.97   398.25   647.47   134.27   3.229   2171.97   398.25   647.47   134.27   3.229   277.215   398.25   647.47   134.27   3.229   277.215   377.216   398.25   647.47   134.27   2.134   2.227.675   398.25   647.47   134.27   2.134   2.227.675   348.22   277.216   348.22   277.216   2.134   2.227.675   348.22   277.216   348.22   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216   277.216	340-674	342.218	343.804	346.938	348.510	351.065	353-179	356-24]		
294.537 213.164 0.989 278.2083 294.537 89.108 16.368 0.919.827 0.0849 271.164 0.989 0.919.827 0.0849 0.849.827 0.091 2.94.531 0.849 271.268 0.941 2.84.321 0.849 271.268 0.941 2.84.324 0.989 0.949 0.989 0.949 0.841 2.845 0.949 0.941 2.845 0.949 0.949 0.981 0.849 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.989 0.	4-177	-53.190	-110.435	-224.959	-281.682	-395.665	-452.557	-563.750	8	
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279.869 279.869 294.537 30.849 30.6249 -9.526 18.179 395.521 440.627 440.627 440.627 440.627 440.627 440.627 440.627 460.347 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 102.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 103.594 1	17-672 0.989	14.660	12.825	12. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0	7.276	-5.521 4.343 -6.427	3.229	-8.352 1.222 -9.278	ING REVOLUT	
6. 36.00 396.00 179.869 6. 36.25 396.25 294.537 6. 36.50 396.25 294.537 6. 36.75 396.75 354.552 6. 37.00 397.00 395.201 6. 37.50 397.50 489.201 6. 37.75 397.75 40.627 6. 38.00 398.00 593.202 6. 38.50 398.25 647.417 6. 38.75 398.75 758.517 758.517 8. 38.75 398.75 758.517 758.517 8. 38.75 398.75 758.517 8. 38.75 398.75 758.517 8. 38.75 398.75 758.517 8. 38.75 398.75 758.517 8. 38.75 398.75 758.517 8. 38.50 398.50 702.594 8. 38.50 398.50 702.594 8. 38.50 398.50 702.594 8. 38.50 398.50 702.594 8. 38.50 398.75 758.517 8. 56.629	76.672 271.164 89.108	271.557	272.048 108.555 272.416	272.910 121.002 273.262	125-585 273-768 129-055	274-172 131-896 274-548	134.227 275.096 136.451	275.567 138.377 276.021		
6. 36.00 396.00 6. 36.25 396.25 6. 36.75 396.75 6. 37.00 397.00 6. 37.50 397.25 6. 37.75 397.25 6. 38.00 398.00 6. 38.50 398.50 6. 38.50 398.50 6. 38.75 398.75 6. 38.75 398.75	279.869 12.680 294.537	320.249	354.552 -18.179	-25.092 440.627 -30.678	489.288 -35.266 540.347	-38.866 593.202 -41.924	647.417	-46.483 758.570 -48.222	6.29	
6. 36.00 6. 36.25 6. 36.25 6. 37.00 6. 37.25 6. 37.25 6. 38.25 6. 38.75 6. 38.75	396.00	396.50	396.75	397.25	397.50	398.00	398.25	398.75	-0. DEC	
	36.00	36.50	4		37.75		38.25	38.75	SET (	
		1	9 4		ı	ļ	1		ELAPS	

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

	OP RT.ASC	S DECREES					305.428		308.697		312.081	216,009		320.357		325,165		330.231		335.822		341.778		348.048		354-456		718-0		7.225	<u> </u>	
	1 7	IABT HILES				\$3	-2762.505		-2791.083		-2818,732	-2845_801		-2871.696		-2896.513		-2920-850		-2943.678	;	-2964-023		-2987-715		-300g*016	EX.	-3026-913		-3045.584		
	٨	FT/SEC MAUT MILES NAUT MILES NAUT MILES	>	DEGREES		AZIRUTH 356.435 DEGREES	2125-230	61.548	2101-013	61.794	2070-576	2051-624	62.253	2026-179	62.466	1999.884	999-29	1973-163	62.861	1945.860	63.044	1918-155	63.217	1896.014	63.381	27C-1921	68.307 DEABEES	1832-226	63-682	1802.487	63.819	
	×	MAUT MILES	3	DEGREES		AZERUTH 3	612.506	120.514	563.819	179.491	514-705	465.419	117.445	415.693	116.422	366-300	115-399	316.147	114.377	266.142	113.354	215.906	112-331	165.563	111-309	110,284	AZIMUTH	64-509	109.263	13.687	108,241	
\$90	ELEVATION RANGE RATE	FT/SEC	TOP HR.AMG	DEGREES		22.69 MINUTES	-18811-820	3.128	-1802	0.003	-17084-302	-15963.971	352.785	-14631.942	348-537	-13059-093	343.829	-11220-254	338.778	-9105.192	333,102	-6724.233	327.218	-4118-40Z	141-126	414.796			308-364	4502.964	302-161	
FEBRUARY 23, 1965	ELEVATION	DEGREES	GEO DECLIN	DEGREES	- 1	5. HOURS 22.6		-51.307	1-482	-52.089	2.059				-54.254			. 1	-55.574	5.813	-56.288	6.252	-56.971	6-707	050-10-	-58.248	HOURS 25.39	ŀ	-58.792	6.803	-59.375	
FEBRUA	AZIMUTH	DEGREES	GEG RT.ASC	DEGREES			356.980	307.557	359.962	308-619	691°E	6.924	311.023	10.709	312.195	15.217	313.486	20.066	314.802	25.720	316.282	31.689	317.693	38-043	201-616	320,719	3.	51.043	322.306	57.939	323.946	
	RANGE	NAUT MILES	TOP DECLIN GED NT.ASC GED DECLIN TOP HR.AMG	DEGREES		DEGREES ELEV.)	828.780	24.732	783.326	23.423	739.953	699-126	22,120	661-336	21.091	627.057	19.881	597.059	18.370	571.925	16.859	552-309	15.086	236.842	200 668	11.032	6.83 DEGREES ELEY.	532.230	8.885	539.212	6-869	
	1-ST				- 1	•	322.75		323.00		323-23	323.50	}	323.75		324.00		324.25	;	324.50	!	324.75		353.00	306.26	-	6.83 DE	325.50		325.75		
	R HENS					RISE (	5. 22.75		5. 23.00		2- 23-23	5. 23.50		5. 23.75		5. 24.00		5. 24.25		5. 24.50		5- 24-75		3- 63-00	S. 28.25		MAX EL (	5. 25.50		5. 25.75		
	ST HR				ļ	K.	FF		W.	1		ŭ.		T.	- 1	L.				ų.	- 1	ı.			u		ı	r.	- 1	ı.		

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

lu lu	FF 5. 26.00	326.00	552.842	64-123	6.548	6802-539	-37.304	1772.525	-3062.853	13.219
	FF 5, 26,25	326.25	4.841 572.610	325.648 69.983	-59.963	296.097 9175.303	107.218	63.948	-3079-319	18.948
1		i	3.055	327.307	-60.499	290.496	106.195	64.068		
u.	5. 26.50	326.50	597.906	75.685	5.113	11281.579 285.214	-138.648 105.173	1711.013	-3094-731	34-308
1	FF 5. 26.75	326.75	628.096	80.597	4.658	13111.176	-189.549	1679.722	-3109-470	29.116
			0.040	331.078	-61-404	280.503	104-150	64.285		;
-	FF 5. 27.00	327.00	662.441	85.045	3.784	14676-093	-240-108	1647.861	-3122.930	33.606
			-1.119	332.891	-61.931	276.035	103-128	64.382		
	FF 5. 27.25	327.25	700-343	334.883	3-166	16000-550 272-121	102.105	1615-039	-3130-484	31.629
1	FF 5. 27.50	327.50	741.240	92.706	2.256	17114.684	-345.018	1582,789	-3147.333	41.287
			-2.865	336.956	-62.860	268.505	101-093	64.552		
Ì	FF 5. 27.75	327.75	784.697	95.617	1.548	18049.040	-392.745	1549.982	-3157.404	44.622
	20 62 8 30	326 00	-3.518	339.062	-63-129	265.212	100.061	64-626	-3166.899	47.458
			-3.957	341.186	-63.492	262,333	99.038	64.692		
</th <th>SET (</th> <th>FF SET ( -0. DE</th> <th>DEGREES ELEV.) E = 5.43</th> <th></th> <th>HOURS 28.1 RING REVOLU</th> <th>5 HOURS 28.12 MINUTES HINUTES UURING REVOLUTION NUMBER</th> <th>AZEMUTH 0:</th> <th>99.867 DEGREES</th> <th>EES</th> <th></th>	SET (	FF SET ( -0. DE	DEGREES ELEV.) E = 5.43		HOURS 28.1 RING REVOLU	5 HOURS 28.12 MINUTES HINUTES UURING REVOLUTION NUMBER	AZEMUTH 0:	99.867 DEGREES	EES	
H.	RISE (	Ŷ	DEGREES ELEV.)	ę	HGURS 51.9	51.90 MINUTES	AZEMUTH 3	AZIMUTH 309.732 DEGREES	EES	
T.	6. 52.00	412.00	820.479	310.063		-23710.095	1108-924	1712.216	-2891.573	278-429
ļ		- 1	15.437	313.025	- 1	52.506	115.605	62.630		
-	FF 6. 52-25	412.25	162.057	311.026	119-1	-23613-551 51-384	114.582	110.0011	-2915-696	279-690
-	FF 6. 52.50	412.50	703.928	312,130	2.758	-23483-446	995.665	1700-065	-2939-225	281-154
1		1	14.055	315.848	-56-151	49.756	113.559	630.69		
Ľ.	6. 52.75	412.75	646.145	313.266	5.862	-23309-529 48,129	939.241	1693.919	-2961-459	282.975
į ¯	FF 6. 53.00	413.00	588.904	314.851	5.361	-23073.913	881.848	1687.178	-2983-175	285.026
-	FF 6. 53.25		12-425	318.639	6-995	46.155 -22750.818	111.514	63.350	-3003-725	287.347
ı		1	11.506	320.161	-58.085	43.853	164.011	63,507		
r.	6. 53.50	413.50	476-663 10-490	319.211	8.785	-22299.288 40.972	109.468	1671,934	-3023.170	290-268
Ľ	FF 6. 53.75	413.75	422.368	322.342	U	-21652.098	708.303	1664.084	-3041-742	293.913
			9.281	323.356	-59.218	37.485	108-446	63-794		
								1		

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

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-3059.415 298.552		-3076.087 304.488		137-716 100-16061	-3106-625 322.751		-3120.156 336.574		-3132.846 353.300			-3144.525 10.472		-3155.699 25.847		-3165-227 37.863		-3173-837 46-824		-3181.463 53.650		-3188-102 58-760		-3193.808 62.765		-3198.447 65.909		-3202.165 62.592		-3204-674 70-693		-3206.533 72.679			-3207-076 74-193	
1655-276		1		191-49	J.	64.267	1617.212	64.355	Ť	64-455	RE		64.538			_		_				1536.590	l		İ	Ĺ		1				Ĭ.	64.965			
650-192	107-423	291.460	186-400	105.378	474.094	104.355	415.059	103.332	356.041	102-310	AZEMUTH	296-308	101.287	236-793	100-265	176.819	242-66	117.326	98.220	57.469	97.197	-2-22	96.175	-61.879	95.153	-121-781	94-130	-181-462	93.108	-241.362	92.086	-300.855	91.063		-360.715	90.041
-20697.109	32.948	-19243.800	27.040	-Te3/01-	-13395.160	8.827	-8023.742	355,138	-1000-993	338.606	E	6270.080	321.296	12145.378	306.172	16161.866	294.194	18728.531	285.221	20361.923	278.457	21426.018	273.410	22140.733	269.443	22635.575	266.374	22986.833	263.750	23241.778	261.715	23429.082	259.927		C3200.433	258.365
13.413		1		. 779-67	1		27.851	-61.863	29.658	-62.215	HOURS 55.29	28.783	-62.720	25-183	-63.089	21-174	-63.342	17.417	-63.718	14.226	-63.938	11.537	-64.205	9.456	-64.493	164°2	-64.771	6.047	-64.747	4.556	-64.871	3.116	-64.839	124	45745	-65.000
326.321	325.030	331.797	326.785	357.455	350.400	330.429	5.331	332,362	24.631	334.370	9	44.570	336.301	166.09	338,344	72.907	340.463	81.294	342.595	87.261	344.910	91.756	347.231	94.952	349.564	97.475	351.874	99.497	354.254	101-303	356.593	102.611	339.015	104.404		1.372
370-022	7.815	320.595	5.941	275-660	237.880	0.811	211.023	-2.815	199.675	-6.680	REES ELEV.)	6. 55.50 415.50 206.256	-9.740	229.418	-11.457	264.729	-12.073	307.995	-12.046	356.410	-11.625	408-096	-11-104	461.906	-10.305	517.237	-9.913	573.579	-9.224	630-640	-8-764	688.,274	10°078	746.243		-7.523
414-00		414.25		414-50	414.75		415.00		415.25		29.78 DEC	415.50		415.75		416.00		416.25		416.50		416.75		417.00		417.25		417-50		417.75		418.00		418.25		
FF 6, 54,60 4		FF 6. 54.25 4		FF 6. 54.50 4	7 51.48 . 4 33		FF 6. 55.00 4		6. 55.25 415.25		MAX EL I	6. 35.50		6. 55.75 415.75		FF 6. 56.00 4		FF 6. !6.25 4		FF 6. 56.50 4		FF 6- 56-75 41		FF 6. 57.00 4)		FF 6- 17-25 417-25		FF 6. 57.50 4		FF 6. 57.75 4)		FF 6. 58.00 4		CE A. RR DE A.	73.07	7.00
3.6		u.		4	11	:	u.		H.		11	K.		L.		u.		T.		T.		u.		ı,		FF		u.		¥.		T.		N.		

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Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

	AZIMUTH 105.361 DEGREES	•						
FERRUARY 23, 1965	FF SFE ( -0. DEGREES ELEV.) 6. HOURS 58.72 HINUTES AZIMUTH 105.361 DEGREES ELAPSED VISIBLE TIME = 6.81 HINUTES DURING REVOLUTION NUMBER 0.	CHAIN. LINK NO. L						.9, '

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Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

7	12-1	RANGE	AZIMUTH	ELEVATION	RANGE RATE	SUR RANGE	*	>-	7
		NAUT MILES	DEGREES	ŧ		MAUT MILES NAUT MILES NAUT	NAUT HILES	NAUT MILES HAUT	AUT MILES
		TOP AT.ASC TOP DECLIN			GEO DECLIN TOR HR. ANG	TOR HR. ANG	מ	33	
		DEGREES		DEGREES	DEGREES	DEGREES	DEGREES	DEGREES	
RISE (	9-	DEGREES ELEV.)		10. HOURS 57.3	57.34 MINUTES	AZEMUTH 3	AZEMUTH 329.066 DEBREES	EES	
0	CC 10, 57,50 657,50	772,883	328.405	1.096	-23962.695	758.364	2156.431	-2726.426	659.755
			58,494	ł	10.719	\$8.714	166.131	23.800	
13	CC 10. 57.75 657.75	713.816	32/-884	2-056	-2389	699.279	2181.314	-2719-911	603-453
			57.696			86.654	169,155	21.974	
CC 10. 58.00 6	658-00		326.977		-23789-750	640-370	2205.075	-2712-404	24(-133
	36 037	187.923	400000000000000000000000000000000000000		8.89 P	581-69	2228.451	2704.222	490-295
	C 10. 30.63 636.63		55.385	267.171		82.495	171.202	18.160	
8	CC 10, 52,50 658,50		324.088	5. 3	-23452.568	'n	2251.037	-2695.310	433-774
			53.770	267-637	7.060		172.226	14.177	
23	CC 10. 58.75 658.75	460.562	322-030	7.623	-33172-149	*	2272.601	-2685.429	376.915
			51.611	268-083	6.103		173.249	14.149	
00	CC 10. 89.00 659.00		319.950	759-6	-22762.260	408-026	2293.865	-2674.613	624-DZE
		197.388	49.002	268.539	5.282	75.585	174.273	12.079	
52	CC 10. 59.25 659.25		316.820	11-780	-22142.496	351.577	2314.574	-2663.441	262.788
	200	200 317	45.481	906-897	240	704 638	2224 018	-2661 273	208.617
5	rr TO: 24.50 624.50	202.867	40.812		3.404	70,179	176-326	7-837	1
75	CC 10. 59.75 659.75	264, 447	306-470		-19544.806	243.864	2353,170	-2637.805	148.723
		206.046	34.200	269.786	2.376	67.016	177.344	5.676	
CC 11: -0.	960.00	219.367	297.109	23.795	-1673	195.475	2371.248	-2624.310	91-643
			24.571	270.258	1.503	63.682	178.367	3.496	
CC 11. 0.25 St	840-25		282.426	29.713	<del>11184</del>	155.426	2389.217	-2610.148	34-107
			10-700	270-614	0-260	59.802	179.391	1.306	
CC 11. 0.50 64	660-50	163.274	260-230	34.054	-4135.683	131.563	2406.049	-2594.044	-23.514
			-8.280	271.113	~0.410	55.488	179.585	0.889	
•	24 43	C. WAY RI C 34 73 DECEREC ELEV. 1	11	TALIN SAIDH	ATTENTE	A73 MITTH 25	A73BILTH 267, SOA OFGEFFE	n n n	

-80-360	-137.957		-195.092	-252.176		-309-320		-305-911	-422.918		-479.696		-536.097		~592.72E		-648.502		-704.825		-760.465					-752-567		-697.314		-641-289		-585.257	
-2578.218	2560-920	5.263	-2543.198 7.429	-2524.869	9.570	-2505-657	11-682	13.759	-2464-177	15.796	-2442.780	17.787	-2420-545	19.730	-2397.059	21.621	-2373.143	23.458	-2349.005	25.238	-2323.477	26-951	£6		ES	-2203.617	26.700	-2192.756	24.972	-2181.424	23.187	-2169.375	21-346
2421.982	2437.378	177.538	2452.210	2466.117	175.491	2479.300	174.467	2491.473	2503-132	172.420	2514-130	171.396	2524.735	170.372	2533.722	169.349	2542.619	168.325	2550.579	167.302	2557.713	166.278	AZIMUTH 167-308 DEGREES		AZIMUTH 156.300 DEBREES	2669.068	13.554	2692.589	12.543	2715.795	176811	2738,165	10.500
132-914	158.829	43.975	199,978	248.914	25.968	301-873	12.932	337.066	413.604	338.217	470.998	320.347	528.968	305.565	587.344	293.848	646.015	284.924	704.907	278.070		272.580	AZIMUTH 16	•0	AZIMUTH 19	806.220	270-224	766.308	271.729	729-066	212.834	694-926	273.775
5010-111	12449.368	-2.160	17090-323	19742.044	-4-114	21278.034	+26-4-	22209.126	22801.744	-6.850	23194.646	-7.854	23463.897	-8-777	23652.753	-9-664	23787.115	-10.528	23883.575	-11.536	23952.030	-12.381	3.89 MINUTES	TION NUMBER	57.22 MINUTES	-16654.001	-12-231	15651.093	-11.319	-14482-317	-10.396	13127-241	-9-433
33.925	28.962	271.947	23.345	i		14.643	273.251	11.753	9.224	274.252	7.362	274.572	5.652	275.155	4.397	275,503	3.018	275.785	1.852	276.359	1.039	276.806	HOURS 3.8	Z Z	21. HOURS 57.23		83.332	1.156			- 1		84.66
233.)87	212.460	-47.663	198.388	189.307	-69.509	183.506	-75-122	179.523	176.255	-80.058	173.973	-80.605	172.123	-80.484	170.871	-79-924	169.717	-79.175	168.479	-78.469	167.737	-77-747	11.	MINUTES DUR		156.457	-66.387	153.063	-63.118	149.547	-29.463	145.394	-55.457
164.398	186.519	229.419	223.491	269.262	247.493	320.060	260-634	373.840	429.416	295.398	486.217	313.287	543.882	328-263	602.008	339.992	660.580	348.809	719.459	355.816	778.486	1.431	REES ELEV.)		OEGMEES ELEV.)	621.585	167-697	181.104	166.233	744.469	161-661	710-337	104-318
660.75	661.00		661.25	661.50		661.75		007700	662.25		662.50		662.75		00.699		663.25		063-50		663.75		þ	IBLE TIME =	-0. DEG	1317.25		1317.30		1317.75		1318-00	
EC 11. 0.75	cc 11. 1.00		cc 11. 1.25	cc 11. 1.50		CC 11. 1.75		CC 11. 2.00	CC 11. 2.25		CC 11. 2.50		CC 11. 2.75		CC 11. 3.00		CC 11. 3.25		05.11. 3.50		CC 11. 3.75		CC SET (	ELAPSED VISIB	CC RISE (	CC 21. 57.25 1317.25		CC 21- 37-30 1317-30		CC 21. 57.75 1317.75		CC 21- 58-00 1318-00	

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

-528.744	-472.276	-415.684	-358-355	-301.852	-244.937	-187.631		-150-619	-73.325	-16-240		41-022	98.290		155.553	212.852	269.896				-16.950	
-2156.756 19.451	-2143.432	-2129.580 15.512	-2114-930	-2099.685	-2083.658	6	7.144	-2050.502	-2032-629	2.803	0.615	-1995.281	-1975.872	3.760	-1955.793 5.933	-1935.081	8.087 -1913.947	10.215	ses	EES	-2969.473	0.658
2759.341	2780.202	169.6972 7.436	2818.509	2836.489	2853.718	AZIMUTH 112.040 DEGREES	3.351	2885.369	2899.851	1.308	0.287	2926.251	2937.942	1.756	2948-871 2-777	2959.333	3-799	4.820	67.384 DEGREES	AZIMUTH 252.252 DEGREES	1930-989	0.307
664.369	637.912	616.086	599.400	588.291	583.084	AZINUTH 1	274-726	390.824	603.545	274-031	273.599	6440952	672.661	272.615	271.985	739.475	777.605	270.639	AZINUTH 0.	AZEMUTH 2	719.189	88.388
-11569.098	-9797.554	-7.050 -7815:269 -6.786	-5640.215	-3310.740	-863.370	Ï.	-2.999	3986.006	6274.739	8403-1-195	-0.262	10333.619	12050-920	1.558	13557.752	14865.483	3.466	4.331	ION NUMBER	27.57 MINUTES	-9493.661	-0.287
3.068	3.627	3.060	4.288	4.594	4.786	HOURS 59.59	87.78	4.492	4.438	38.562	89.043	3.431	2.826	89.858	2.145	1.764	90.841	91.156	22, HOURS 1,96 MINUTES HINUTES DURING REVOLUTION NUMBER	HOURS 27.57	2.095	88.804
141.053	136-141	131.059	125.896	120.232	114.208		-18.223	102.407	96.743	-6.789	-1.445	86-467	81.681	8.277	77.561	73.422	16.398	168-61	22. H MINUTES DUR	23.	268.609	-1.284
679.804	653.397	631-597	514.981 .63.159	603.890	598.741	DEGREES ELEV.	163.771	606.408	619.127	164.582	164.953	660-414	688-103	166.162	719.723	754.886	167.625	168-403	DEGREES ELEV.)	DEGREES ELBV.)	734.575	12.478
1318.25	1318.50	1318.75	1319.00	1319.25	1319.50	4.80	•	1320.00	1320.25	1320.50		1320.75	1321.00		1321.25	1321.50	1321.75		E TIM	-0-	1408.50	
CC 21. 58.25 1318.25	CC 21. 58.50 1318.50	CC 21. 58.75 1318.75	CC 21. 59.00 1319.00	CC 21. 59,25 13	CC 21. 59.50 1319.50	CC MAX EL (		CC 220.	CC 22. 0.25 13	CF 22. 0.50 13		CC 22. 0.75 13	CC 22. 1.00 13		CC 22. 1.25 13	CC 22. 1.50 13	CC 22. 1.75 13		CC SET ( -	CC RISE (	CC 23. 23.50 1	

Figure 5-32. Sample TRACE-D Program Data-Coneration Listing (Continued)

C 23.	28.75	CC 23, 28.75 1408.75	713.347	273.044	2.450	-7726.235	268.169	1950.506	-2956.220	39.746
			12.836	3.185	89.283	0.686	17.984	0.715	1.532	
23,	29.00	CC 23, 29.00 1409.00	696.570	278,079	2.770	-5810.257	641.149	1968.436	-2942.970	97-123
			13.230	8.075	89.540	1.648	67.590	1.736	3.717	
23,	29.25	CC 23, 29.25 1409.25	684.727	283.000	2.758	-3771:789	669.284	1986.093	-2928-653	154.518
١		,	13.552	13,002	90.145	2.443	67.173	2.757	5.890	
23,	29.50	CC 23, 29.50 1409.50	678.015	268.189	3.054	-1648,730	662.574	2003.356	-2913.272	211.598
			13.940	18.138	90.528	3.424	67.087	3.779	440.8	
Ħ	9	3.17 DEG	REES ELEY.)		HOURS 29.69	I	AZINUTH 29	292-145 DEGREES	EES	
23.	29.75	CC 23. 29.75 1409.75 676.613	676.623	293.377	2.958	51	691-199	2020-317		258.542
			14.165	23.396	90.999	4.328	196-90	4.800	10.173	
23.	30.00	CC 23. 30.00 1410.00	680.563	298.458	3.023	2660.094	665.100	2035.736	-2879.799	325.732
			14.270	28.622	162.467	5-194	86.846	5.821	12.271	
23	30.25	CC 23. 30.25 1410.25	269-689	303.708	2-822	4745.537	674.270	2051.432	-2862.337	382.434
į			14.137	33.577	91.841	6.163	86.914	6.843	14.332	
23.	30.50	CC 23,, 30.50 1410.50	703.872	308:751	2.512	6725.358	698.469	2066.520	-2843.083	438.995
			14.154	38.529	92.332	7.084	121-181	7.864	16.352	
23	30.75	CC 23. 30.75 1410.75	722.787	313.387	2,242	8567.851	707.393	2080,300	-2623.223	495.739
		3	13.889	43.235	92:165	8.029	87.524	8.885	18.326	
23.,	31.00	CC 23., 31.00 1411.00	746.070	318.065	1.775	10252.785	730.670	2093.971	-2802.759	552.406
İ			13.494	47.728	93.144	8.998	87.835	4.907	20.251	
23.	31.25	CC 23. 31.25 1411,25	773.297	321.773	1.310	11771.277	757.899	2106.367	-2781.307	608.475
	f	•	12.935	51.820	93.612	9.875	18.485	10.928	22.123	
CC 23.	31:2	1411.50	804.054	325.909	0.864	13124.404	788.668	2119.183	-2759.231	664.741
		,	12.247	55.729	94.037	10.844	89.298	11.949	23.940	
-/	ier (	-0. DEG	DEGREES ELEV.)	23.	23. HOURS 31.6	31.67 MINUTES	AZIMUTH 32	AZIMUTH 328.215 DEGREES	EES	
N S	0 V:S	ELAPSED VISIBLE TIME =		MINUTES DU	KING REVOLU	MINUTES DURING REVOLUTION NUMBER	<b>~</b> C			-
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Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

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	×	DEGREES NAUT MILES		DEGREES					31-150		30.129		29.108		28.087		-2214.396			26.045		23.024		44E-4162-	£09*47	
	1 AND 2	DEGREES	TOP HR. ANG	DEGREES			EES	19.146	136.345	19.753	136.205	20.534	136.229	21.532	136.395		22.805	136.897	24.437	138.318	26.546	141.239		5D6-67	150.513	
	ASPECT ANG	DEGREES	GEO DECLIN	DEGREES			AZIPUTH 193.856 DEGREES	224.203	-27.804	225-714	-27,009	227-193	-26-171	228,621	-25.297		229.976	-24.308	231.235	-23.474	272,272	-22-607		233.302	CF0-17-	
		1	ED RT. ASC	DEGREES			AZEPUTH 1	105.401	76.781	76.350	77.286	76.211	17.694	75,939	78.290	) ) )	75.566	78-779	74.988	79.335	74-165	79.933	1	(3-015	174-08	
59	RANGE RATE	FT/SEC	TOP DECLIN 6	DEGREES DEGREES DEGREES			8.69 MINUTES	-23799.836	-69.952	-23731.551	-71.287	-23636,979	-72.730	-23507-535	-74.499		-23329.216	-76.408	-23081.344	-76.670	-22730.896	-81.445		169.77777	100.401	
AY 23. 1945			TOP RT.ASC	DEGREES			10. HOURS 8.6		303.939	1-626	304.208	2.752	1	3-676			5.043	303-557	6.821 ·	ŀ	A.222 .	1		- 1	470.48	
FEBRUARY	AZ I MUTH	DEGREES	. 2					193.825	-1660-726	192.843	-1611.680	191.733	-1561-481	190-648	-1511.586		189.274	-1440-806	187.531	-1409.659	185.448	-1357-991		C/9-781	- to - social	
	RANGE	NAUT MILES	*	NAUT MILES NAUT MILES	>	DEGREES	DEGREES EL <b>B</b> V.)	824.893	2346.064	766.224	2347.713	47.097 707.768	2348.340	46.201	2346.770	45.264	591.696	23472495	534-427	2346.746	43.269	2344-510	42.205	197.774	41.093	
	T-ST						ģ	608.75		90.00		609.25		05.609			609.75		610,00		610.25			00-01		
	MINS						AISE (	8.75		9.00	ı	9.25	•	9.50	1		9.75		10.00		10.25		- (	10.00		
	ST HR						in m	EE 10.		EE 10.		EE 10.		EE 10.			EE 10.		EE 10- 10-00		EE 10, 10,25		;	E 10. 10.30		

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

74 -2347.023 10 22.982	17 -2378,312 14 21,961	23 -2408-836 38 20-940	37 -2438.816 50 19.920	54 -2467.920 56 18.899	3 -2495,664 33 17.878	59 -2523.859 52 16.857	~28	1 !	-28	~26	-28	-26
32.994	38.017 285.514	45,023 293,538	54.937 297.460	68.754 298.936	86.433 299.488	REES 105.369 299.752	121,778			148.867	153.256	
234-181 -20-729	234.803	235.205	235.366	235.265	234.888 -16.099	112.547 DEGREES 7 234.224 7 -15.233	233.267	232.019	230.488	228.692	226.657	224.418
11-416	69.207 81.335	66.193 81.890	62-277 82-326	57.923 82.824	54.966 83.241	AZIMUTH 1 55.687 83.657	59.441	63.752	67.345 85.111	70.044 85.527	72.009	73.428 86.530
12,782 -21461,998 39,213 -87,784	-20279.660 -84.399	-18369.889	-15201.952 -66.610	-10049.319 -52.128	-2647.976 -33.908	6 MINUTES 5542.089 -14.373	2		ויו	20783.045	21788.605 36.591	22445.765
12.752	16.026	19.679	24.628 143.596	29.211 142.190	32.704	HOURS 12.08 31.746 141.514	27.712	22.782	18.421	14.597	11.811	9.388 144.500
178.964	174.196 -1200.612	167.240	157.257 -1094.055	141.870	120.988	) 10. 97.685 -930.910	79.019	65.829 -821.350	57.035	50.885 -710.010	46.711	43.468 -598.077
368,316 2339,273 39,934	316.483 2335.506 38.724	268.795 2331.013	227.022 2325.766	195.331 2319.844 34.780	179.329 2313.229 33.355	32.86 DEGREES ELEV.) 612.25 183.040 2305.673	31.874 205.364 2297.619	30.334 241.246 2289.247	285.737 285.615 2280.137	27.081 335.122 2270.299	25.367 387.759 2259.561	23.596 442.374 2248.366
\$10.75	611.00	611.25	611.50	611.75	612.00	32.86 DE 612.25	612.50	612.75	613.00	613.25	613.50	613.75
EE 10: 10.75	EE 16. 11.00	EE 10. 11.25	EE 10. 11.50	EE 10. 11.75	EE 19. 12.00	X EL 1 12.25	EE 10. 12.50	12.75	13.00	13.25	13.50	13.75
	2	10.	10.	10.	5.	10.	10.	EE 10.	EE 10.	10.	EE 10.	EE 10.
	A .		H	=	3	3 B	#	H H	H	#3	<b>m</b>	8

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

#	Ď	EE 10. 14.00	00-419	498-398	40.884	7.610	22891.073	74-447	222-017	158.845	-2695.295
l	ļ		ļ	19.887	2444134	874-647	10000	447.40	641.8-	262-962	9.711
	2	EE 10. 14.25	5 614.25	555.298	39-042	5.969	23201-917	75.172	219.491	164-041	-2778 ATT
				2223.560	-485.045	146.288	46.081	17.392	-1.849	295.476	169.8
in in	5	VY 71 VI 32	7,77	+C6-11							
1		,		012-210	37.317	4.305	22423.689	75.677	216-913	161-977	-2735.629
į				15.972	248.854.	147-175	46.230	87.729	146-9-	294,587	7-576
	=	14.79	EE 113. 14.75 614.75	670-92%	34,251	3.203	23584_RGR	7.4.014	TOT 115	14 260	404 0000
				2196.608	-378.895	147.964	400 CX	20.00	2000	00Ke 100	Ca1CC/7-
ŀ			- 1	13.945			200420	Torece	1000	20000000	6.049
FE	2	EE 10, 15,00	00.519	729.293	35.038	2,020	23703.041	76.222	211.726	16-1-TAO	1977 707
				2182.388	-315.106	168.984	51.513	18,612	-5.153	2.92-978	# C Y - S
ļ	ŀ		Ì	11.078							
		te 30% 15.25	615.25	787.75	33.950	1.276	23749.554	75.327	209.208	164.287	-2701.432
				2167.269	-257.879	149.843	52.751	29-121	-4-208	252.086	4.608
<b>11</b>	LAPS	SET (	EE SET ( -0. DE	DEGREES ELEV.)		10. HOURS 15.4	10. HOURS 15.43 MINUTES	HETH	33.480 DEGREES	ES	
							ACT NOTES				
		AISE (	9	DECREES ELEV.)		22. HOURS 45.0	45.04 HINUTES	AZERUTH	-0.098 UBBREEK	65	
#	27.	45:25	1365.25	759.308	1.332	1.266	1.266 -22362.174	76.704	116,007	29,326	-2512.184
	İ			2485.971	-155.121	274.971	74,123	270,290	-2,551	354.843	177.225
m	ä	45.50	EE 221. 45.50 1365.30	704-490	E STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STATE OF THE STA	1.04	-23 M T - 376	76. 800	116 421		
ĺ	-			2467.455	-2%2-286	281.443	11-4-1	270-613	-3-670	378 - 87E	176.243
nt Tr	23	62.28	EE 27. 65.75 1365.75	7.00.4 7.00.4	A7.9-2	2.038	7. 626 -21674 111	37, 76			
ļ	-			2448-193	-269-511	287,940	73.259	271-120	110-430	33-197	-2539.357
u M	r S	**	A4 A8 4944 A8	10.221						2	717071
ų ų	<b>;</b>			414 - 85% 501 - 85% 501 - 85% 501 - 85% 501 - 85%	06E-W	4-126	-20999.495	76.098	114.287		-2551.702
	İ			12.323			07440	C1110347	-2-317	333-843	174-153
m	EE 22.	¥6.25	1366.23	547.126	11.581	5.546	5.546 -20246.259	75-667	113.258	38.825	-2563.437
				2407-932	-383.531	300.471	66.614	272.009	-6,274	329-609	173-129
				14000		•			,		

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Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

EE 22. 45.50 1	.50 1:	366.50	498.339	15.356	7.016 306.660	-19247.960 63.366	75.088 272.466	112.353	42.581 323.669	-2574.103 172.106
EE 22. 46.75 1366.75	.75 1	366.75	452.374 2363.958	20.376 -496.873	9.347	-17912.150 59.172	74.347	111,583	47.180	-2584.239
EE 22. 47.00 1367.00	.00	367.00	410-259	26.294	10.150	-16115.370 53.989	73.442	110.958	52.821 312.183	-2593.607 170.058
EE 22. 47.25 1367.25	.25 1	367.25	373-330	33.260	11.510	-13709-603	72.408	110.488	59.710 306.933	-2602.224
EE 22. 47.50 1367.50	.50 1	347.50	343.221 2293.393	41.987	13.236	-10555.447 39.746	71.346 274.162	110-181	67.996 302.009	-2609.501 168.010
EE 22. 47.75 1367.75	.75 1	367.75	321.854	52.125 -721.828	14.509	-6605.204	70.438	110.045	77-651 297-223	-2616.869 166.986
EE 22. 48.00 1	.00 I	368.00	311.111 2242.671 27.481	63.495	15.351	-2020.094 20.218	69.923	110.086	88.332	-2623.085 165.962
EE 22. 48.25 13	.25 1	15.24 DE 368.25	15.24 DEGREES ELEV. 368.25 312.065 2216.322	75.398 -833.068	HOURS 48.11 15.201 341.988	11 MINUTES 2785-679 9.796	AZEMUTH 69.971 275.549	68.884 DEGREES 110.311 -13.684	99.357 288.642	-2628.396
EE 22. 48.50 %	.50 %	368.50	29.127 324.625 2189.286	86.663	14.451	7291.792	70.566	110.724	109.906	-2633.047
EE 22. 48.75 1368.75	1.75 1	368.75	30.715 347.528 2161.263	96.725	12.943	11119.716	71,515	111.329	119.342	-2636.885 162.891
EE 22. 49.00 1	.00 13	369.00	32-245 378-662 2132-621	105.107	11.548	14148.407	72.584		127.379	-2639.842
EE 22. 49.25 1369.25	.25 1	369.25	33.717 416.761 2103.829	111.974	10.068	16447.630	73.602	113.119	134,029	-2642.579
EE 22. 49.50 1:	.50 1:	369-50	35.132 459.609 2073.801	117.680	8.337 359.668	18162.432	74.482	114.303	139.454	-2643.949 159.819

Figure 5-32. Sample TRACE-D Program Data-Generation Listing (Continued)

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-2644.979 158.795	-2644,549	-2644.105 156.748	-2642.506	-2640.156 154.700	-2637.244 153.676		İ			
	7		1	1	1					
143.862	147.449	150.376	152.774 260.585	154.744	156.364	ES				
115.673	117.223	118.942	120.817	122.830	124.962	.349 DEGRE				
75.197	75.751 278.918	76.160	76.445	76.626	76.718 280.858	AZIMUTH 137.349 DEGREES				
19438-317 -32.898	20393.591 -36.179	21115-633 -38.843	21667-927 -41.045	22095.104	22428.469 -44.297	MINUTES ION NUMBER				
6.863 2.755	5.586	4.096	3.242	1.945	1.372	URS 51.21 NG REVOLUT				
122.033	126.024	129.088	131.813 -1318.027	133.988 -1370.206	135.838 -1421.396	) 22. HOURS 51.21 MINUTES MINUTES DURING REVOLUTION NUMBER				
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Table 5-15. Data Generation Output Listing Description

Item	Description	Page Reference
1	Group-2 FINP input. The entries shown indicate that a bias of 1000 feet is to be applied to all range observations generated for Station BB.	5-46/5-48
2	Sigmas. In the case of a data generation run, the sigma table is used for the purpose of specifying the standard deviation of random noise which is to be applied to the generated data. Interpretation of the printed output shown is otherwise the same as described under Item 12, Table 5-14.	3-39 5-46/5-48
3	Specification-I input data. The eight columns from left to right contain station identification, data interval, minimum elevation angle, maximum elevation angle, maximum range in nautical miles, and datageneration start and stop times in days, hours, and minutes from midnight of epoch day.  The information shown indicates that the following	3-15 5-47/5-50
	<ul> <li>specifications have been given to the program:</li> <li>a. Observations are to be generated for Station AA at 15-second intervals whenever the computed local elevation angle is above zero degrees.</li> <li>b. No maximum elevation angle is assumed and no maximum range is to be considered (data generated for all ranges and for all elevation angles greater than zero).</li> <li>c. Station AA is assumed to be active during the time interval from epoch until a time 24 hours after midnight of epoch day.</li> </ul>	
	In the case of this particular data generation run, the corresponding Specification-I input items for Stations BB through FF are identical to those for Station AA. However, this need not be true in general, inasmuch as each station is independent of the others with respect to these input items.	

Table 5-15. Data Generation Output Listing Description (Continued

Item		Description		Page Reference
4	the range Station BB radar para of applying a range bi	r indication. The message indicate bias parameter has been selected in the case of a data generation ameters are selected only for the g biases to the generated data, in as on Station BB data. The message the correction of parameters the ignored.	for on run, purpose this case age	3-39, 3-40 5-48
5	the formate purpose of which are for the state is printed horizontal symbols R and the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or the seand U, V or t	con-II data headings. These heading to the table appearing beneath the this table is to define the types of to be generated for each station. It ion-identification column header vertically, the headings appear in rows, with the top row displaying ANGE on the left and LONG. On the cond row the symbols SUR. R on the right. The individual heading in accordance with the following	em. The f data Except, which two g the he right he left	3-13/3-19 5-50/5-54
	Heading	Description or Symbol	Units	٠
	RANGE AZMTH ELEV. R. DOT P. DOT Q. DOT P Q AZ. DT E. DOT R. DDT MU. VIS LAT LONG. SUR. R	Range Local azimuth angle Local elevation angle Range rate Range-rate difference Range-rate difference Range difference Range difference Range difference Rate of change of local azimuth Rate of change of local elevation Second time derivative of range Mutual visibility  Latitude of sub-vehicle point Longitude of sub-vehicle point Surface range, station to sub-	n mi deg deg ft/sec ft/sec ft/sec ft deg/sec deg/sec deg/sec (indica- tor) deg deg n mi	

Table 5-15. Data Generation Output Listing Description (Continued)

Item		Description		Page Reference
5	Heading	Description or Symbol	Units	
(cont)	HIGH T	Altitude above oblate earth	n mi	
	DOPLR	Doppler frequency shift	cps	
	TOOK	Look angle	deg	
]	VARI	Variances	Same as	
			corresp.	
			observa-	
			tions	
	KAPPA	Angle between radius vector and local vertical	deg	
	ASPCT	Aspect angles	deg	
]	ATTEN	Signal attenuation	db	
	X, Y, Z	x, y, 2	n mi	
	T-R,D	Topocentric right ascension and declination	deg	
	G-R, D	Geocentric right ascension and declination	deg	
Ī	HR. ANG	Topocentric hour angle	deg	
	U, V	Horizon-scanner angles u, v	deg	
6	mation). each static identificat low it. Ar line indica defined by the presen Station AA rate, heig ascension	specification table (Specification). The two horizontal lines associated are the line containing the station symbol and the line immedian X on the first line or a Y on the tethat the corresponding quantities that the corresponding quantities that the header is to be general the table header is to be general the example the indicated data type are range, azimuth, elevation, the (altitude), x, y, z, topocentric and declination, topocentric hoursensor angles u and v.	ted with tion- tely be- e second ty a ted. In pes for range c right	5-50/5-54
7	the satelli: utes from position ar are printe	is. Each time the integrated poste crosses the equator, the time midnight of epoch day and the said velocity in the basic coordinated. Position and velocity are give and in units of earth radii and erinute.	in min- itellite le system en in the	3-63 5-5

Table 5-15. Data Generation Output Listing Description (Concluded)

Item	Description	Page Reference
8	Rise message. The time when the satellite becomes visible from a particular station (at the specified minimum elevation angle) is obtained by interpolation and printed in the manner shown, along with the local azimuth angle for the corresponding time.	3-38, 3-39 5-39
9	Time corresponding to generated data. The time shown is to be associated with the data quantities appearing on the line to the right of the time print-out and on the line following. The time is given both in hours (0 through 24) and minutes of the day as identified at the top of the output page, as well as in minutes from start (i.e., minutes from epoch). In the case of the particular output shown, time from start corresponds to the time of day because the epoch chosen for the run happened to be midnight.	5-48
10	Maximum elevation point. The time when the elevation angle reaches its maximum is obtained by interpolation and printed along with the corresponding values for the elevation and azimuth angles in the manner shown.	5-39
11	Set message. When the time at which the elevation angle reaches the specified minimum from above is obtained by interpolation, the print shown at this position occurs.	3-38, 3-39 5-39
12	Duration message. After each pass, a message is printed giving the time in minutes during which the elevation angle was above the input minimum value and the range was below the input maximum value.	5-39

## 5. 5. 5 Residuals Analysis Output Description

The listed output created by a typical residuals analysis run is shown in Figure 5-33. Supplementary descriptive information relating to the indicated areas of this listing is annotated in Table 5-16.

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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Output Listing

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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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Figure 5-33, Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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-0.181334565 0.10064200E -0.152297185	, ,,	0.15800200E -0.1424138 0.216111100E -0.17147092E 0.23245800E -0.1356730E		. ,	0.45191828 0.45531228 0.45531228 0.45194828 0.45184898 0.45184898 0.451948698 0.99715868
0.132201906 08 0.209570306 03 0.16571406E 03	0.21128590E 03 0.16825931E 03 0.21281937E 03	7.21463316E 09 0.1732331E 08 0.2143203E 09 0.17273030E 08 0.21802647E 03 0.17812911E 08 0.18048301E 08		0.15946995 08 0.2293776 08 0.231600236 03 0.193745346 08 0.233468756 93 0.13569038 08	0.23757470E 03 0.1975794E 08 0.23965915E 03 0.24178915E 03 0.24178915E 03 0.20352647E 93 0.2033(982E 08
-0.85C79939E 07 0.11733196E 08 -0.43428040E 07	0.11579624E 08 -0.83104970E 07 0.11433712E 08 -0.32791770E 07	0.11295734E 08 0.11165529E 08 0.11165529E 08 0.11044125E 08 0.11044125E 08 0.11045189E 07 0.11055880E 07		0.105070355 08 -0.76569805 07 0.105528255 08 -0.782095205 07 0.10591585 08 -0.776001595 07	0-10351493E 08 -0.763760E 07 0.10338978E 08 -0.1532844E 08 -0.75055480E 07 0-1034E130E 03 -0.75055480E 07
6F 50 EE 10 EE 50	STA TYP EE 10 EE 10 EE 10 EE 10				20 E E E E E E E E E E E E E E E E E E E
2 45.0000 5 45.0000 5 45.0000	MN SEC. 6 0. 6 15.0000 6 15.0000	6 30.0000 6 20.0000 6 45.0000 7 0.000 7 15.0000	7 30,000 7 30,000 7 45,000 7 45,000 8 0 8 15,000	8 30,0000 8 30,0000 8 45,0000 2 45,0000 9 0,000 9 15,0000	9 32.0000 9 35.0000 9 45.0000 10 0.10 0.10 0.10 0.10 0.10 0.10 0
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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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0.10365885E 08 0.245855705 03 0.4425199E 01 -0.715351569E 07 0.20175158E 08 -0.4315280E 07 -0.10396121E 08 0.24805012E 03 -0.4315280E 03 -0.10397164E 08 0.24895119E 03 0.403529E 01 -0.7154379E 07 0.21051491E 08 -0.93316240E 07 0.10486293E 08 0.2518979E 03 0.38566599E 01 -0.71399729E 07 0.21214408E 08 -0.86866589E 07	METEKS	TICNS, 6 STATICNS, 1653 CELLS IN COMPACTED DATA LIST			
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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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, w	END							u.	FINP INPUT CARD	<b>4</b>
A	DUALS	RESIDUALS ARALYSIS EXAMPLE.	Ē.							
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2			STG	SIGHA TABLE						
					INITIAL CONDITIONS	DNOTITONS				
>		-0.223902116 1.4		ALPHA×	0.1	0.15882923E 03	03 A=	0.24010736E 08	736E 08	
,    -		C. 86714486E GT		DELTA	6	20000	# - E	0.14526680E-06	580E-06	
X1007		ئ. 11.22632358E 04	_	8ETA =	2 m	0.34499@9E		0.15882923E	923E 03	
Tâx	1.4 <b>1</b>	0.59438147E 04		H H	0.2	0.24010754E 08	08 05 1*	-0,50146602E 03	602E 02	
1007	<b>=</b> -	0.238/89/8 05			•	1		*		
¥	HOSPHE	<u> Хуйазрнеже — Тоскнеео</u>	Ba	* 14.74	* 3.20000000E-01 * 0.68299999E CI		W7CDA = 0.499999999E 0Z D2 =-0.15584000E 02	10E 02		
1	i i	0.55304505E-02 J2=	0.108275995-02	1	EARTH FCDEL 13= -0.26930300E-05	DEL 930200E-(	35 J4= -0.15600000E-05 J9= 0.20999999E-06	100E-05 J5=	-0.59999998E-08	
37	Γ	ı	#IZ1	0		=2Sf	0.532900005-07	l	152= -0.Zeugugue or	
		0.17234000E-05	1222	-0.13180000E	300E 02	153# # 461	0.58419999E-08 0.40929399E-08	154= 0.	-0-34499999E 01 C-58250000E 02	
	1	0.44819999E-06	±2£3	"		355	0.84620000E-09		-0.15320000E 02	
	.E3.	0.164299998-06	L41*	2.160000000E	000E ₹2 000E 03	361≖ 362≖	0.37459999E-07	1624 0	0.11314999E 03	
	1	0.153330006-05	-247			363=	U.I.LESCOUDE-07	p	-0-115000005-01	
		0.57190000E-07	1494	-0.109999999E	999E 03 000E 02	164= 165*	0.22560000E-08 0.33275959E-09	L65x -C.	0.00/39999E 02 -0.17749999E 02	
	1	0.15090000E-06	1514	ľ	999E 02	±99°	0.5153COOOE-IO	100 = -01	-0714340000E 02	
##	KOTTO:J	THE FOLLOWING BODIES ARE USED FOR PLANETARY PERTURBATIONS	USED FCR	PLANETAR	Y PERTURB	ATIONS				
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	-									

Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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							173422416315		573422716353	173422563440		573423055244		173422723003	573423216157	173423067507	573423364043	173423233045	213423540032	173423412732	573423722110	173423576154	573424104515	173423761420	573424265753	173424136375	5/3424451146	144112474611	573424562105			
	1 6	8	<b>.</b>	3	9		17165122177÷		571650366020	171647064332		571646211710		171644726523	571644047473	171642502765	571641621156	171640316430	571517755175	171636171600	571635251701	225150559121	571533127720	171631665327	571531005362	171627505456	>/16266UUU54	171625301653	>71624342556			
MIN.	3951.65891	m		Ì	103.71713		000000000000	EPOCH.	.74300000	552737400000		152751600000	TE EDITIES	553755454000	154536310000	554515100000	154637260000	554447540000	1554571000000	555634720030	155660314300	555571234300	154434424000	555631434000	00000014146	22222222222	120223114000	226510614000	156555552400			
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COMPUTED	A,E,I,0,U,T G-Z4010736E 09	90-3089554I°0	0.10300000E-03	70017	-0.50146602E 03	ENTERING	3/ 1764	***THRU	THRUST RE	3/ 1/64	THRUST RE	THRUST RE	OS THE	3/ 1/64	3/ 1/64	3/ 1/64	3/ 1/64	3/ 1/64	3/ 1/64	3/ 1/64		3/ 1/64	5/ 1/64	2/ 1/04		7971 /6			10/1 //	ENTERING	FNYFETME	ENTERING

Figure 5-33., Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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OIFFERENCES FRUM THE MEAN	(f),	)	04 03 04	3 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	03 3 3 4
RESIDUAL VECTCR RESOLVED TATU ORBIT PLANE	RADIAL = -4.576779F 02 IN TRACK = -1.325666F 03 CROSS TRACK» -1.365414E 04 RSUGT = 1.378326E 04	RADIAL	RADIAL = 3.948287E 04 IN TRACK = -6.161978E 03 CRUSS TRACK = -1.703249E 04 RSUBT = 4.343929E 04	RADIAL = -1.612250E 03 IN TRACK = 4.782533E 03 CROSS TRACK= -2.095889E 02 RSUBT = 5.051141E 03	RADIAL 2.382763E 04 IN TRACK = -6.264651E 03 CROSS TRACK= -1.955923E 03 RSURT = 2.471492E 04
L'AE RESIDUAL	0600000E 04 -1.264157E-01 -7.053574E-01 -9.644994E-03	.60600000E 04 -1.986769E 00 2.432930E-01 1.833111E-01	-6074999E 04 -1.184926E-01 -8.447873E-01 5.160069E 00	.6C74999E 04 8.17883E 02 1.197053E-01 2.100745E-01	-1.165610E-01 -7.342668E-02 3.242608E-00
RESIDUAL	99 SYSIM= -3.740HOIE 0 -7.76TBB9E= -4.495118E=	999 SYSTM= -6-959774E 0 -2-165887E 0 4-227158E	73.463439E 0 -9.727299E-0 -9.727299E-0	000 SYSTH= -9.117553E 0 -1.048955E 0 4.856173E 0	000 -3.3 -8.8 1.4
CALCULATED GBS ERVAT ICN	HIN=40 SEC=*9.9999	#114-40 SEC=59.9999 2.1863235 07 -9.147315E 06 -3.858522E 06	NA41 SEC=15:0000 9.630629E C6 - 1.115363E 02 - 6.541174E 00	#IN=41 SEC=15.COOO 2.1855846 07 -9.279807E 06	HIN=41 SEC=30,0000 1,432490E 06 (1,697703E 00 (1,231896E 00
TINE TYPE	R A B	101.00000 X 101.00000 Y 101.00000 L	64 HR= I FI 101.25000 A 101.25000 E	64 HR= 1 FI 101.25000 X 101.25000 Y 101.25000 Z	101.50000 E
ST 11	(2) 101.0000 101.00000 101.00000	3/ 1/6+ CC 101- 101- 101-	3/ [/64 CC 101. 101.	3/ 1/64 cc 101.	*101 *101 *101 *9/1 /6

Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

********		(3) (15)	(E) (E)	03		03	04-	04 04		04 05	005 05 04	5 60	22	8
ANALYSIS	MEAN	4-035440E 03	1.786597E (-1.3683C9E	3.178267E -6.459186E 7.787115E		1	-6.202710E   8.126018E   -1.953763E	6-345263E 7-339431E		2-031317E (	1	5.567109E -1.167869E 1.555396E	9.993837E 02	1.476168E
AEGULTS FOR RESIDUAL	RHS	1.170508E 04	14.135705E 04	3-791724E 03 6-641180E 03 7-844678E 03		35	1	9.561108E 04 1.999938E 04 1.016938E 05				1.171015E 05 1.555428E 05	3.558379E 04 9.993897E 02	1.4913516 05 -1.4761686
AEGULTS.	(1)			77 00 03 45 00 00	E			11 86 10 86 11	<b>(E</b> )	10 23 11 23	22 01 11 23 16 23	11 23	33	
ACCUMULATED	\$0\$	9,309044E 09	4.093779E 09 1.915719E 10 1.283739E 08	6-038412E 08 1-852422E 09 2-594637E 09		4-262205E 10 2-306513E 11	6.295146E 11 9.027879E 11 6.881529E 10	7-851672E 11 3-439786E 10 8-893803E 11	)		2.326510E 1 5.247782E 1 6.321196E 1	1.778465E II 3.153937E 11 5.544522E 11	4.178481E 10	7.339624E 1
************	TYPE (RESCLVED)	RADIAL In Track	CRUSS TRACK (RSUBT) RADIAL	IN TRACK CROSS TRACK (RSUST)		RADIAL IN TRACK	CRUSS TRACK (RSUBT) RADÍAL	IN TRACK CROSS TRACK (RSUBT)		RADIAL In track	CRUSS RRACK (RSUBT) RADIAL	IN TRACK CROSS TRACK (RSUBT)	RADÍAL	CRUSS TRACK
	TYPE	**	<u> </u>	- 2			א ע	> 14		* 4	ш ×	- NJ	~	w.
	12	Ž				ដ				2			£	İ

Figure 5-33. Sample TRACE-D Program Residuals-Analysis Listing (Continued)

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			•					
33 '6.345782E 05 1.567814E 05 33 '6.345782E 04 -6.246407E 04 33 1.3823044E 04 -6.609761E 04 33 1.36250E 05 -1.143839E 05	1.538024E 0		•	-				
8-244571E 11 1-328875E 11 2-019611E 11 4-457719E 11	7.806205E 11						,	
(RSUBT) RADIAL IN TRACK CROSS TRACK	(RSUBT)	LINK NG. 1						
× + ~		CHAIN.						

Figure 5-33. Sample TRACE D Program Residuals-Analysis Listing (Concluded)

Table 5-16. Residuals Analysis Output Listing Description

Item	Description	Page Reference
1	Observation time. This is the time point associated with the information which follows on the next four lines of printed output. The month, day, and year are shown at the left side of the page on the line indicated, followed by the time of day in hours, minutes, and seconds. This in turn is followed by system time (SYSTM), which is the time of day given in terms of seconds from midnight.	
2	Station identification.	5-32/5-34
3.	Observation time in minutes from midnight of epoch.	5-35
4	Observation type. Each of these letters indicates the observation type which produced the three quantities shown on the same line of output immediately to the right of that letter (see Items 5, 6, and 7). In this case the types are range, azimuth, and elevation.	5-37
5	Calculated observation values. The indicated numbers are values of range, azimuth, and elevation which have been computed from the integrated position of the satellite at the observation time and the location of the station associated with the observation. Units are feet and degrees.	3-13/3-19
6	Residuals. The quantities indicated represent the difference between the input observation values and the calculated values (see Item 5) for range, azimuth, and elevation measurements reported by Station CC at the time noted (see Items 1 and 3). Units are identical to observation input units for all residuals.	
7	Time residuals (i.e., the observation residual divided by the calculated time rate of change of the observation). Units are seconds.	3-86

Table 5-15. Residuals Analysis Output Listing Description (Continued)

Item	Description	Page Reference
8	Orbit-plane residuals. These are the components of the residual vector, as determined by the R,A,E residuals, in the orbit-plane coordinate system. Units are feet.	3-84/3-86 5-58
9	R _T , or the square root of the sum of the squares of the radial, in-track, and cross-track components of the residual vector.	3-87
10	Accumulated SOS. The three quantities indicated are the square root of the sum of the squares for the radial, in-track, and cross-track components, respectively, for all R, A, E residuals sets from Station AA.	
11	R _T of accumulated SOS components. The square root of the sum of squares of the radial, intrack, and cross-track SOS components (Item-10 quantities).	3-87
12	Number of points. This indicates the number of R, A, E residual vectors, resolved into orbit-plane components, that are represented in the accumulated results. This number is printed three times only for programming convenience.	3-84/3-86
33	RMS of components. The root-mean-square of the radial, in-track, and cross-track components, respectively, for all R, A, E residual vectors for Station AA. Units are feet.	
14	RMS vector, magnitude. The square root of the sum of squares of the components specified in Item 13. Units are feet.	
15	Component mean values. The arithmetic average of all radial, in-track, and cross-track components, respectively, for residual vectors computed from R,A,E sets from Station AA. Units are feet.	

Table 5-15. Residuals Analysis Output Listing Description (Concluded)

Item	Description	Page Reference
16	Mean-vector magnitude. Square root of the sum of the squares of the quantities specified in Item 15. Units are feet.	
17	Accumulated results for $\hat{x}$ , $\hat{y}$ , $\hat{z}$ data from Station AA. The quantities in this block correspond directly to those in similar positions in the R, A, E block described in Items 1 through 16.	
18	Accumulated results for Station CC.	

# APPENDIX A

STANDARD VALUES AND STORAGE LOCATION OF CONSTANTS

#### APPENDIX A

## STANDARD VALUES AND STORAGE LOCATIONS OF CONSTANTS

Figures A-1 through A-3 illustrate tab listings of standard values and of storage locations of constants applicable to TRACE-D program runs. The listings given in Figures A-1 and A-2 tabulate numerical values and descriptions for the standard entries to the INTEG (integration constants) and C (physical constants) regions. Corresponding entry locations within each of these regions are indicated by the numbers in the left-hand columns of these tabulations. The listing presented in Figure A-3, delineating the "basic running deck" (except for the REIN binary cards), itemizes the standard values assigned to those FINP entries which are input on all TRACE-D runs unless special instructions to the contrary are given.

One particular TRACE-D characteristic associated with input of physical constants which should be noted is that all physical constants are input on each run as part of the FINP data and that none are built into the program. Care must therefore be exercised by the user whenever any of the standard values are altered due to the fact that they are interrelated in some cases. For example, if the number of feet per earth radii were to be changed, it might be necessary to change the entries at C(2), C(3), C(15), C(23), C(24), C(25), and C(30).

Description of entries to locations other than the INTEG or C regions has been given in the basic TRACE-D Program report (see Section 4.3).

Figure A-1. Standard Entries to Integration Constants (INTEG) Region

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1	• CINICIDA		INPUT
<b>-4</b>	.0043752691	•0C43752691 EARTH ROTATION RATE (RAJ/MIN)	NAME
2	<b>•6055303935</b>	.0055303935 GM. EARTH GRAVITATION CONSTANT (ER**3/MIN**2)	
n 4		SHILD FOR SPEED OF LIGHT CORRECTION SHIPS AND IN THE SHIPS SHOULD AND AND AND AND AND AND AND AND AND AN	Scī
	·	(COMPUTED 14 CSET)	
'n		S**2/A**2 H (1-E)**2 (CCYPCTEL 1/ CSET)	
۶	ć.	FACTOR FOR DECREASING BOUNDS IN L.S. SCLUTTOR	
~		2*E-E**2 (COMPUTED IN CSET)	
Φ,	.0043752691	ATMOSPHERE ROTATION RATE (KAD/MIN)	
σ.	<b>,</b>	EARTH RADIUS	
13		TYPUT N FOR N-STGVA RESIDUAL ECITOR	CEDIT
<b>-1</b>		INPUT SCALE FACTOR FOR N-SIGNA REGISCIAL ADITION	
12		ERC, GO THÁC 1ST ITERATIO	
13	3260-8399	FEET/KILOKETER	-
14	57.2957755	ANGLE CONVERSION FACTOR	
15	20925738.	A. EARTH RADIUS IN FEET	
16	332951.3	RECATIVE WASS OF SUN	The state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the s
17	.0122955	NOOM	
<b>₽</b>	.814979	VENUS	
19	128701.	RAKS	
20	317.887	JUD 11ER	
23	95.120	SATURN	
22	23454-865	EARTH-HADIIVASTRUICMICAL UNIT	
23	3443.9336	NAUTICAL MILES (6076.1155 FT)/EARTH RADIUS	
54	20925738.	1/0 DISTANCE CONVERSION FACTOR	
25	34876243	170 VELOCITY CONVERSION FACTOR	
56	32-174	GO (USED FOR CDA/W AND THRUST/W)	
27		INPUT PARAMETER OIFFERENCE FOR TRAJECTORY DIFFERENCING	20157
87		INFUL THRESPOLD FOR PERCENT OTHE FOR TRED UTFERENCING	
29	1	CONSTANT FOR DOPPLER HATE	
30	348762.3	FT/SEC DER EK/MIN	
15	6.1	FACTOR FOR INCREASING BOUNDS IN I SESCENTION	
35		RAD/MIN PER DEG/SEC	
33	59295	ä	
34	298.3	KECIPROCAL OF E = ELLIPTICITY	
35	300000	CRITICAL ALTITUDE (FI)	
36	82505.922	DEGIDAY PER RADIMIN	
37-	65	DIRECTION COSTNES OF REDN ANTS FOR LOOP ANGLE	

Figure A-2. Standard Entries to Physical Constants (C) Region

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Figure A-2. Standard Entries to Physical Contants (C) Region (Concluded)

Figure A-3. Standard FINP Entries

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Figure A-3. Standard FINP Entries (Concluded)

APPENDIX B

DERIVATION OF V MATRIX

#### APPENDIX B

### DERIVATION OF V MATRIX

In the variational equations associated with TRACE-D program procedure, the dependence of the gravitational force upon vehicle position is represented by the matrix

$$V = \frac{\partial}{\partial x} \left( -\frac{\mu X}{r^3} \right) + \frac{\partial F_1}{\partial x}$$

which for v-matrix derivation purposes may be written

$$V = \frac{\partial F}{\partial X}$$

where

 $X = (x, y, z)^{T} = \text{vector position of vehicle}$ 

F = gravitational force vector

The components of F in an equatorial coordinate system with the principal axis in the direction of the Greenwich meridian are

$$\begin{pmatrix} f_{x} \\ f_{y} \\ f_{z} \end{pmatrix} = \begin{pmatrix} \cos\phi\cos\lambda & -\sin\lambda & -\sin\phi\cos\lambda \\ \cos\phi\sin\lambda & \cos\lambda & -\sin\phi\sin\lambda \\ \sin\phi & 0 & \cos\phi \end{pmatrix} \begin{pmatrix} g_{U} \\ g_{E} \\ g_{N} \end{pmatrix}$$

where

 $\phi$  = geocentric latitude of vehicle position

 $\lambda = longitude$  of vehicle position

gu,E,N - force vector components in the local horizontal coordinate system, wherein the coordinate axes are directed Up (along the radius vector), East, and North

The foregoing equation also may be written in vector notation, or

The components in an equatorial inertial coordinate system with the principal axis in the direction of  $\lambda$  (vernal equinox) are obtained by a similar transformation in which a replaces  $\lambda$ .

Using subscripts to denote differentiation, and expanding in spherical coordinates  $(r, \phi, \lambda)$ ,

$$F_{X} = F_{r}^{r}_{X} + F_{\phi}^{\phi}_{X} + F_{\lambda}^{\lambda}_{X}$$

$$= RG_{r}^{r}_{X} + R_{r}^{Gr}_{X} + RG_{\phi}^{\phi}_{X} + R_{\phi}^{G\phi}_{X} + RG_{\lambda}^{\lambda}_{X} + R_{\lambda}^{G\lambda}_{X}$$

$$= R(G_{R}^{r}_{X} + G_{\phi}^{\phi}_{X} + G_{\lambda}^{\lambda}_{X}) + R_{\phi}^{G\phi}_{X} + R_{\lambda}^{G\lambda}_{X}$$

Noting that

$$R_{\phi} = R \begin{pmatrix} 0 & 0 - 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} = RE_{1}$$

$$R_{\lambda} = \begin{pmatrix} 0 - 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} R = E_{2}R$$

then

$$\begin{split} \mathbf{F}_{\mathbf{X}} &= \mathbf{R}(\mathbf{G}_{\mathbf{r}}\mathbf{r}_{\mathbf{X}} + (\mathbf{G}_{\phi} + \mathbf{E}_{1}\mathbf{G})\phi_{\mathbf{X}} + \mathbf{G}_{\lambda}\lambda_{\mathbf{X}}) + \mathbf{E}_{2}\mathbf{R}\mathbf{G}\lambda_{\mathbf{X}} \\ &= \mathbf{R}(\frac{1}{\mathbf{r}}\,\mathbf{G}_{\mathbf{r}}\mathbf{X}^{\mathrm{T}} + (\mathbf{G}_{\phi} + \mathbf{E}_{1}\mathbf{G})\phi_{\mathbf{X}} + \mathbf{G}_{\lambda}\lambda_{\mathbf{X}}) + \mathbf{E}_{2}\mathbf{F}\lambda_{\mathbf{X}} \\ &= \mathbf{R}(\frac{1}{\mathbf{r}}\,\mathbf{G}_{\mathbf{r}}\mathbf{X}^{\mathrm{T}} + (\cos\phi\,\mathbf{G}_{\phi} + \cos\phi\,\mathbf{E}_{1}\mathbf{G})\frac{\phi_{\mathbf{X}}}{\cos\phi} + \mathbf{G}_{\lambda}\lambda_{\mathbf{X}}) + \mathbf{E}_{2}\mathbf{F}\lambda_{\mathbf{X}} \end{split}$$

The latter expression permits the desired matrix  $V = F_X$  to be computed after  $\phi_X/\cos\phi$ ,  $\lambda_X$  and  $G_r$ ,  $G_\phi$ ,  $G_\lambda$ , respectively, have been calculated from geometrical formulas and from applicable equations for G (see Section 3.6.1).

In deriving expressions for  $G_r$ ,  $G_\phi$ , and  $G_\chi$  it is convenient to make use of the relations  $\sin \phi = z/r$  and  $\lambda = \tan^{-1} y/x$ , wherefrom

$$\frac{\phi_{x}}{\cos \phi} = \frac{-xz}{r^{3}\cos^{2}\phi} = \frac{-xz}{r(x^{2} + y^{2})}$$

$$\frac{\phi_{y}}{\cos \phi} = \frac{-yz}{r(x^{2} + y^{2})}$$

$$\frac{\phi_{z}}{\cos \phi} = \frac{-z^{2}}{r(x^{2} + y^{2})} + \frac{r}{(x^{2} + y^{2})} = \frac{r^{2} - z^{2}}{r(x^{2} + y^{2})}$$

$$\lambda_{x} = \frac{-y}{x^{2} + y^{2}}$$

$$\lambda_{y} = \frac{x}{x^{2} + y^{2}}$$

$$\lambda_{z} = 0$$

In the foregoing expressions it should be noted that  $\alpha_{\mathbf{x}} = \lambda_{\mathbf{x}}$ , inasmuch as  $\alpha$  and  $\lambda$  differ only by a time-dependent term.

The vector G has previously been given (Section 3.6.1) as

$$\begin{split} g_{U} &= -\frac{\mu}{r^{2}} \left[ 1 - \sum_{n=2}^{n_{1}} (n+1) J_{n} \left( \frac{a_{e}}{r} \right)^{n} P_{n}(\sin \phi) \right. \\ &+ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+1) J_{nm} \left( \frac{a_{e}}{r} \right)^{n} P_{n}^{m}(\sin \phi) \cos m(\lambda - \lambda_{nm}) \right] \\ g_{E} &= -\frac{\mu}{r^{2} \cos \phi} \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} m J_{nm} \left( \frac{a_{e}}{r} \right)^{n} P_{n}^{m}(\sin \phi) \sin m(\lambda - \lambda_{nm}) \\ g_{N} &= \frac{\mu}{r^{2}} \left[ -\sum_{n=2}^{n_{1}} J_{n} \left( \frac{a_{e}}{r} \right)^{n} P_{n}^{r}(\sin \phi) \cos \phi \right. \\ &+ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} J_{nm} \left( \frac{a_{e}}{r} \right)^{n} P_{n}^{m'}(\sin \phi) \cos \phi \cos m(\lambda - \lambda_{nm}) \right] \end{split}$$

where

 $g_{U,E,N}$  = Up, East, and North components of vector G

 $\mu$  = product GM of Newtonian gravitational constant and the earth mass

r,  $\phi$ ,  $\lambda$  = geocentric distance, geocentric latitude, and east longitude, respectively, of a point

a_e = mean equatorial radius of the earth

J_n, J_{nm} = numerical coefficients

Pn - Legendre polynomial of the first kind of degree n

 $\boldsymbol{p}_{n}^{m}$  . Associated Legendre function of the first kina

 $\lambda_{nm}^{-1}$  longitudes associated with the  $J_{nm}^{-1}$ 

Differentiating the foregoing expressions for  $g_U$ ,  $g_E$ , and  $g_N$ , then

$$\frac{\partial g_{U}}{\partial r} = \frac{\mu}{r^{3}} \left[ 2 - \sum_{n=2}^{n_{1}} (n+1)(n+2) J_{n} \left( \frac{a_{e}}{r} \right)^{n} P_{n} (\sin \phi) + \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+1)(n+2) J_{nm} \left( \frac{a_{e}}{r} \right)^{n} P_{n}^{m} (\sin \phi) \cos m(\lambda - \lambda_{nm}) \right]$$

$$\frac{\partial g_E}{\partial r} = \frac{\mu}{r^3 \cos \phi} \left[ \sum_{n=2}^{n_2} \sum_{m=1}^{n} m(n+2) J_{nm} \left( \frac{a_e}{r} \right)^n P_n^m (\sin \phi) \sin m(\lambda - \lambda_{nm}) \right]$$

$$\frac{\partial g_{N}}{\partial r} = \frac{\mu}{r^{3}} \left[ \sum_{n=2}^{n_{1}} (n+2) J_{n} \left( \frac{a_{e}}{r} \right)^{n} P'_{n} (\sin \phi) \cos \phi \right]$$
$$= \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+2) J_{nm} \left( \frac{a_{e}}{r} \right)^{n} P'_{n} (\sin \phi) \cos \phi \cos m(\lambda - \lambda_{nm}) \right]$$

$$\frac{\partial g_{U}}{\partial \phi} \cos \phi = \frac{\mu \cos \phi}{r^{2}} \left[ \sum_{n=2}^{n_{1}} (n+1) J_{n} \left( \frac{a_{e}}{r} \right)^{n} P'_{n} (\sin \phi) \cos \phi \right]$$
$$- \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+1) J_{nm} \left( \frac{a_{e}}{r} \right)^{n} P'_{n} (\sin \phi) \cos \phi \cos m(\lambda - \lambda_{nm}) \right]$$

$$\frac{\partial g_E}{\partial \phi} \cos \phi - \frac{-\mu \cos \phi}{r^2} \left[ \sum_{n=2}^{n_2} \sum_{m=1}^{n} \ m J_{nm} \! \left( \! \frac{a_e}{r} \! \right)^n P_n^{m'} \! \left( \sin \phi \right) \! \sin m (\lambda - \lambda_{nm}) \right] + g_E \! \sin \phi$$

$$\begin{split} \frac{\partial g_N}{\partial \phi} &\cos \phi = \frac{-\mu \cos \phi}{r^2} \left[ -\sum_{n=2}^{n_1} J_n \! \left( \!\! \frac{a_e}{r} \!\! \right)^n \left\{ P_n'' \left( \sin \phi \right) \! \sin \phi \right\} \right. \\ &+ \sum_{n=2}^{n_2} \sum_{m=1}^n J_{nm} \! \left( \!\! \frac{a_e}{r} \!\! \right)^n \left\{ P_n''' \left( \sin \phi \right) \! \cos^2 \phi \right. \\ &- P_n''' \left( \sin \phi \right) \! \sin \phi \right\} \cos m (\lambda - \lambda_{nm}) \right] \\ &\frac{\partial g_U}{\partial \lambda} = \frac{\mu}{r^2} \left[ \sum_{n=2}^{n_2} \sum_{m=1}^n m(n+1) J_{nm} \! \left( \!\! \frac{a_e}{r} \!\! \right)^n \!\! P_n'' \! \left( \sin \phi \right) \! \sin m (\lambda - \lambda_{nm}) \right] \\ &\frac{\partial g_E}{\partial \lambda} = \frac{-\mu}{r^2 \cos \phi} \left[ \sum_{n=2}^{n_2} \sum_{m=1}^n m^2 J_{nm} \! \left( \!\! \frac{a_e}{r} \!\! \right)^n \!\! P_n'' \! \left( \sin \phi \right) \! \cos m (\lambda - \lambda_{nm}) \right] \end{split}$$

and

$$\frac{\partial g_{N}}{\partial \lambda} = \frac{-\mu}{r^{2}} \left[ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} m J_{nm} \left( \frac{a_{e}}{r} \right)^{n} P_{n}^{m'} (\sin \phi) \cos \phi \sin m (\lambda - \lambda_{nm}) \right]$$

The terms containing second derivatives of Legendre polynomials in the preceding equation for  $\partial g_{N}^{}/\partial \phi \cos \phi$  are calculated using the recursion formulas

$$\cos^2 \phi \ P_n''(\sin \phi) = 2 \sin \phi \ P_n'(\sin \phi) - n(n+1)P_n(\sin \phi)$$

and

$$\cos^2\phi \ P_n^{m''}(\sin\phi) = 2\sin\phi \ P_n^{m'}(\sin\phi) - \left\{n(n+1) - \frac{m^2}{\cos^2\phi}\right\} \ P_n^{m}(\sin\phi)$$

which may be rearranged in the forms

$$\cos^3 \phi \ P_n''(\sin \phi) - \cos \phi \sin \phi \ P_n'(\sin \phi) = \sin \phi \cos \phi \ P_n'(\sin \phi)$$
$$- n(n+1)\cos \phi \ P_n(\sin \phi)$$

 $\cos^3\phi\ P_n^{m''}(\sin\phi)-\sin\phi\cos\phi\ P_n^{m'}(\sin\phi)=\sin\phi\cos\phi\ P_n^{m'}(\sin\phi)$ 

$$-\left\{n(n+1)\cos^2\phi-m^2\right\}\frac{P_n^m(\sin\phi)}{\cos\phi}$$

The equation containing the second derivatives of the Legendre polynomials consequently becomes

$$\frac{\partial g_{N}}{\partial \phi} \cos \phi = \frac{\mu}{r^{2}} \left[ -\sum_{n=1}^{n_{1}} J_{n} \left( \frac{a_{e}}{r} \right)^{n} \cos \phi (\sin \phi P'_{n} (\sin \phi) - n(n+1) P_{n} (\sin \phi)) \right]$$

$$+ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} J_{nm} \left( \frac{a_{e}}{r} \right)^{n} \left( \sin \phi \cos \phi P_{n}^{m'} (\sin \phi) - n(n+1) P_{n} (\sin \phi) \right)$$

$$- \left\{ n(n+1) \cos^{2} \phi - m^{2} \right\} \frac{P_{n}^{m} (\sin \phi)}{\cos \phi} \cos m(\lambda - \lambda_{nm})$$

Using the GRAV subroutine notation (see Appendix F1, wherein

$$A_n = -(n+1)J_n \left(\frac{a_e}{r}\right)^n P_n(\sin \phi)$$

$$B_{nm} = (n+1)J_{nm}\left(\frac{a_e}{r}\right)^n P_n^m(\sin \phi)$$

$$C_{nm} = \frac{m}{\cos \phi} J_{nm} \left(\frac{a_e}{r}\right)^n P_n^m(\sin \phi)$$

$$D_{n} = J_{n} \left(\frac{a_{e}}{r}\right)^{n} P'_{n}(\sin \phi) \cos \phi$$

$$E_{nm} = - J_{nm} \left(\frac{a_e}{r}\right)^n P_n^{m'} (\sin \phi) \cos \phi$$

$$F_{nm} = \sin m(\lambda - \lambda_{nm})$$

$$G_{nm} = \cos m(\lambda - \lambda_{nm})$$

the expressions for  $\mathbf{G}_{\mathbf{r}},~\mathbf{G}_{\phi},~\mathbf{G}_{\lambda}$  then become (for  $\mathbf{G}_{\mathbf{r}})$ 

$$\frac{\partial g_{U}}{\partial r} = \frac{\mu}{r^{3}} \left[ 2 + \sum_{n=2}^{n_{1}} (n+2)A_{n} + \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+2)B_{nm}G_{nm} \right]$$

$$\frac{\partial g_{E}}{\partial r} = \frac{\mu}{r^{3}} \left[ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+2)C_{nm}F_{nm} \right]$$

$$\frac{\partial g_{N}}{\partial r} = \frac{\mu}{r^{3}} \left[ \sum_{n=2}^{n_{1}} (n+2)D_{n} + \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+2)E_{nm}G_{nm} \right]$$

(for  $G_{\phi}$ )

$$\frac{\partial g_{U}}{\partial \phi} \cos \phi = \frac{\mu \cos \phi}{r^{2}} \left[ \sum_{n=2}^{n_{1}} (n+1)D_{n} + \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} (n+1)E_{nm}G_{nm} \right]$$

$$\frac{\partial g_{E}}{\partial \phi} \cos \phi = \frac{\mu}{r^{2}} \left[ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} m E_{nm} F_{nm} \right] + g_{E} \sin \phi$$

$$\frac{\partial g_{N}}{\partial \phi} \cos \phi = \frac{\mu}{r^{2}} \left[ \sum_{n=2}^{n_{1}} - (\sin \phi D_{n} + n \cos \phi A_{n}) \right]$$

$$-\sum_{n=2}^{n_2}\sum_{m=1}^{n} (\sin \phi E_{nm} + \left| \frac{n(n+1)}{m} \cos^2 \phi - m \right| C_{nm}) G_{nm}$$

and (for  $G_{\lambda}$ )

$$\frac{\partial g_{U}}{\partial \lambda} = \frac{-\mu}{2} \left[ \sum_{n=2}^{n_2} \sum_{m=1}^{n} mB_{nm}G_{nm} \right]$$

$$\frac{\partial g_{E}}{\partial \lambda} = \frac{-\mu}{r^{2}} \left[ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} mC_{nm}G_{nm} \right]$$

$$\frac{\partial g_{N}}{\partial \lambda} = \frac{\mu}{r^{2}} \left[ \sum_{n=2}^{n_{2}} \sum_{m=1}^{n} m E_{nm} F_{nm} \right]$$

The three vectors  $G_r$ ,  $\cos \phi$   $G_{\phi}$ , and  $G_{\lambda}$  thus obtained are then applied in the previously indicated computation for  $V = F_X$ .

APPENDIX C

DERIVATION OF T MATRIX

#### APPENDIX C

#### DERIVATION OF T MATRIX

In the variational equations associated with TRACE-D program procedure, the dependence of the drag force upon vehicle position is represented by the matrix

$$\begin{split} T &= \frac{\partial F_3}{\partial X} \\ &= -\frac{1}{2} \binom{C_D^A}{W} \frac{\partial}{\partial X} \left( \rho V_A \dot{X}_A \right) \\ &= -\frac{1}{2} \binom{C_D^A}{W} \left( V_A \dot{X}_A \frac{\partial \rho}{\partial X} + \rho \dot{X}_A \frac{\partial V_A}{\partial X} + \rho V_A \frac{\partial \dot{X}_A}{\partial X} \right) \end{split}$$

The derivatives of the factors  $\rho$ ,  $V_{\begin{subarray}{c} A \end{subarray}}$  appearing in the latter expression then are

$$\frac{\partial V_{A}}{\partial X} = \frac{\partial}{\partial X} [(\dot{x} + \omega_{e} y)^{2} + (\dot{y} - \omega_{e} x)^{2} + \dot{z}^{2}]^{1/2}$$
$$= \frac{\omega_{e}}{V_{A}} (-\dot{y}_{A}, \dot{x}_{A}, 0)$$

$$\frac{\partial \dot{\mathbf{x}}_{\mathbf{A}}}{\partial \mathbf{X}} = \begin{bmatrix} 0 & \omega_{\mathbf{e}} & 0 \\ -\omega_{\mathbf{e}} & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

 $\frac{\partial \rho}{\partial x} = \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial x}$ 

In connection with the first of the above relationships it should be noted that

$$\frac{\partial h}{\partial X} = \left(\frac{\partial h}{\partial x}, \frac{\partial h}{\partial y}, \frac{\partial h}{\partial z}\right)$$

where

$$\frac{\partial h}{\partial x} = \frac{x}{r} \left\{ 1 - \frac{a_e \epsilon (2 - 3\epsilon + \epsilon^2) z^2}{\left[r^2 - (2\epsilon - \epsilon^2)(x^2 + y^2)\right]^{3/2}} \right\}$$

$$\frac{\partial h}{\partial y} = \frac{y}{r} \left\{ 1 - \frac{a_e \epsilon (2 - 3\epsilon + \epsilon^2) z^2}{\left[r^2 - (2\epsilon - \epsilon^2)(x^2 + y^2)\right]^{3/2}} \right\}$$

$$\frac{\partial h}{\partial z} = \frac{z}{r} \left\{ 1 - \frac{a_e \epsilon (2 - 3\epsilon + \epsilon^2)(x^2 + y^2)}{\left[ x^2 - (2\epsilon - \epsilon^2)(x^2 + y^2) \right]^{3/2}} \right\}$$

$$h = r - \frac{a_e(1 - \epsilon)}{\left[1 - (2\epsilon - \epsilon^2) \frac{x^2 + y^2}{r^2}\right]^{1/2}}$$

 $\epsilon$  = ellipticity of reference ellipsoid

and also that  $\partial \rho/\partial h$ , the rate of change of density with altitude, depends both upon the model atmosphere and its parameters and upon h.

The term  $\partial \rho / \partial h$  either may be approximated by using

$$\frac{\partial \rho}{\partial h} = \rho' \frac{\rho}{h}$$

with values of p' specified respectively within the altitude intervals  $0 \le h < 108$  and  $108 \le h < 378$  nautical miles or may be calculated from expressions for density.

In the latter case, for  $76 \le h < 108$  nautical miles  $(\rho' = \rho_1)$ ,

$$\rho_1 = 5.606 \times 10^{-12} \left( \frac{76}{h} \right)^{d_1} \left[ \frac{108 - h}{32} + 0.85 \left( \frac{h - 76}{32} \right)^{4/3} F_{10.7} \right] \left[ 1 + \frac{h - 76}{153} \left( \frac{1 + \cos \psi'}{2} \right)^3 \right]$$

and for  $108 \le h < 378$  nautical miles  $(\rho' = \rho_2)$ ,

$$\rho_2 = \rho_0(h)(0.85F_{10.7}) \left\{ 1 + 0.19 \left[ \exp(0.012h) - 1.9 \right] \left( \frac{1 + \cos \psi'}{2} \right)^3 \right\}$$

where

$$\log_{10}\rho_{0}(h) = d_{2} - 0.00368h + 6.363 \exp[-0.0048h]$$

 $d_1$ ,  $d_2$  = numbers input to the program at execution time

 $F_{10.7}$ ,  $\psi'$  = Lockheed-Jacchia model-atmosphere parameters (Ref. 12)

Differentiating each of these expressions with respect to h then yields

$$\frac{\partial \rho_1}{\partial h} = \frac{-d_1 \rho}{h} - 5.606 \times 10^{-12} \left( \frac{76}{h} \right)^d \left[ \frac{1}{32} - \left( \frac{1 + \cos \psi'}{2} \right)^3 \left( \frac{184 - 2h}{4896} \right) \right]$$

$$+ 5.606 \times 10^{-2} \left( \frac{76}{h} \right)^d (0.85) F_{10.7} \left( \frac{h - 76}{32} \right)^{1/3} \left[ \frac{1}{24} - \left( \frac{1 + \cos \psi'}{2} \right)^3 \left( \frac{532 - 7h}{14688} \right) \right]$$

and

$$\frac{\partial \rho_2}{\partial h} = -\rho \frac{\left[0.00368 + 0.0305424 \exp(-0.0048h)\right]}{0.4342944819} + (0.85)F_{10.7}$$

$$\times \exp\{2.302585[d_2 - 0.00368h + 6.363 \exp(-0.0048h)]\}$$

$$\times \left[0.001938\left(\frac{1 + \cos\psi'}{2}\right)^3 \exp\{0.0102h\}\right]$$

Combining the foregoing results, the elements  $T_{ij}$  of the T matrix then are

$$T_{11} = -\frac{C_D^A}{2W} \left( V_A \dot{x}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial x} - \frac{\rho \omega_e \dot{x}_A \dot{y}_A}{V_A} \right)$$

$$T_{12} = -\frac{C_D^A}{2W} \left( V_A \dot{x}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial y} + \frac{\rho \omega_e \dot{x}_A^2}{V_A} + \rho V_A \omega_e \right)$$

$$T_{13} = -\frac{C_D^A}{2W} \left( V_A \dot{x}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial z} \right)$$

$$T_{21} = -\frac{C_D^A}{2W} \left( V_A \dot{y}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial x} - \frac{\partial \omega_e \dot{y}_A^2}{V_A} - \rho V_A \omega_e \right)$$

$$T_{22} = -\frac{C_D^A}{2W} \left( v_A \dot{y}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial y} + \frac{\partial \omega_e \dot{x}_A \dot{y}_A}{V_A} \right)$$

$$T_{23} = -\frac{C_D^A}{2W} \left( v_A \dot{y}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial z} \right)$$

$$T_{31} = -\frac{C_D^A}{2W} \left( V_A \dot{z}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial x} - \frac{\partial \omega_e \dot{y}_A \dot{z}_A}{V_A} \right)$$

$$T_{32} = -\frac{C_D^A}{2W} \left( V_A \dot{z}_A \frac{\partial \rho}{\partial h} \frac{\partial h}{\partial y} + \frac{\partial \omega_e \dot{x}_A \dot{z}_A}{V_A} \right)$$

$$T_{33} = -\frac{C_D^A}{2W} \left( v_A \dot{z}_A \frac{\partial_p}{\partial h} \frac{\partial h}{\partial z} \right)$$

# APPENDIX D

ANALYTIC SOLUTION OF CERTAIN VARIATIONAL EQUATIONS

## APPENDIX D

### ANALYTIC SOLUTION OF CERTAIN VARIATIONAL EQUATIONS

When the forces acting on a vehicle are symmetric about the polar axis of the earth, the variational equations for the two initial-condition parameters a (right ascension) and  $\Omega$  (right ascension of ascending node) have the analytic solutions

$$\frac{\partial x}{\partial a} = -y$$

$$\frac{\partial \dot{x}}{\partial a} = -\dot{y}$$

$$\frac{\partial y}{\partial a} = x$$

$$\frac{\partial \dot{y}}{\partial a} = \dot{x}$$

$$\frac{\partial z}{\partial a} = 0$$

$$\frac{\partial \dot{z}}{\partial a} = 0$$

and

F

$$\frac{\partial \mathbf{x}}{\partial \Omega} = -\mathbf{y}$$

$$\frac{\partial \dot{x}}{\partial \Omega} = -\dot{y}$$

$$\frac{\partial y}{\partial \Omega} = x$$

$$\frac{\partial \dot{\mathbf{y}}}{\partial \Omega} = \dot{\mathbf{x}}$$

$$\frac{\partial z}{\partial \Omega} = 0$$

$$\frac{\partial \dot{z}}{\partial \Omega} = 0$$

These solutions may be derived from consideration of the vector equation

$$X = \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} r \cos \delta \cos \alpha \\ r \cos \delta \cos \alpha \\ r \sin \delta \end{pmatrix}$$

wherein r,  $\delta$ , and a represent instantaneous values. Differentiating with respect to  $a_0$ , the initial value of right ascension, then leads to

$$\frac{\partial X}{\partial \alpha_{o}} = \frac{\partial X}{\partial \mathbf{r}} \quad \frac{\partial \mathbf{r}}{\partial \alpha_{o}} + \frac{\partial X}{\partial \delta_{o}} \cdot \frac{\partial \delta}{\partial \alpha_{o}} + \frac{\partial X}{\partial \alpha_{o}} \cdot \frac{\partial \alpha}{\partial \alpha_{o}}$$

Noting that

$$\frac{\partial X}{\partial a} = \begin{pmatrix} -y \\ x \\ 0 \end{pmatrix}$$

it thus is necessary only to show that the relations

$$\frac{\partial \mathbf{r}}{\partial \mathbf{a}_{o}} = \frac{\partial \delta}{\partial \mathbf{a}_{o}} = 0 \qquad , \qquad \frac{\partial \mathbf{a}}{\partial \mathbf{a}_{o}} = 1$$

which are intuitively plausible in the case of axially symmetric forces, hold in order to complete the derivation of the analytic solution

$$\frac{\partial X}{\partial a_0} = \begin{pmatrix} -y \\ x \\ 0 \end{pmatrix}$$

Letting

$$R = \begin{pmatrix} r \\ \delta \\ \alpha \end{pmatrix}$$

a differential equation for R under the symmetry assumption would be of the form

$$\ddot{R} = G(r, \delta, \dot{r}, \dot{\delta}, \dot{a})$$

or

$$\ddot{R} = G(R, \dot{R})$$

with initial conditions

$$R(t_{o}) = \begin{pmatrix} r_{o} \\ \delta_{o} \\ \alpha_{o} \end{pmatrix}$$

and

$$\dot{R}(t_{o}) = \begin{pmatrix} \dot{r}_{o} \\ \dot{\delta}_{o} \\ \dot{\alpha}_{o} \end{pmatrix}$$

but with no dependence upon a.

Differentiating with respect to  $\boldsymbol{\alpha}_{\text{O}}$  and interchanging orders of differentiation then yields

$$\ddot{R}_{a_0} = \frac{\partial G}{\partial R} R_{a_0} + \frac{\partial G}{\partial R} \dot{R}_{a_0}$$

with initial conditions

$$R_{\alpha_{0}}(t_{0}) = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

and

$$\dot{R}_{\alpha_{0}}(t_{0}) = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}.$$

Inasmuch as the third column of the matrix  $\partial G/\partial R$  is  $\partial G/\partial a$ , which is always zero by the symmetry assumption, then

$$R_{a_0}(t) = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

necessarily is a unique solution which, when expressed in component form, gives the required relations

$$\frac{\partial \mathbf{r}}{\partial \mathbf{a}_{\mathbf{o}}} = 0$$
 ,  $\frac{\partial \delta}{\partial \mathbf{a}_{\mathbf{o}}} = 0$  ,  $\frac{\partial \mathbf{a}}{\partial \mathbf{a}_{\mathbf{o}}} = 1$ 

#### APPENDIX E

BINARY EPHEMERIS (B7) TAPE FORMATS

#### APPENDIX E

#### BINARY EPHEMERIS (B7) TAPE FORMATS

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The format and characteristics of the TRACE-D program binary ephemeris (B7) tape are illustrated in Figures E-1 through E-4. Setup information for generation of this tape in conjunction with a TRACE-D program run has been fully described in the basic document (see Section 5.1.2.2).

#### 1. EVEN-MINUTE FORMAT

The RESIDUE link may be used to difference two ephemeris tapes and to resolve resulting differences into orbit-plane coordinates. Tapes applicable to this procedure are typically contractor-produced, but may also, for example, involve a combination of one contractor tape and one TRACE-D generated tape. These tapes must be compatible with the IBM 7094 computer and IBM 729-VI tape units and must be in the binary mode with 36 bits per word and a density of 800 bits per inch.

It should be noted that the rectangular coordinates involved in this connection are in the usual inertial system, with the principal axis along the mean equinox at midnight of epoch day and the Z axis along the axis of rotation.

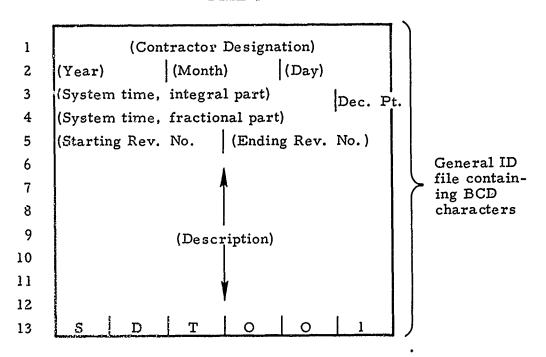
#### 2. EXPANDED FORMAT

Future modifications to the TRACE-D program will result in addition of a number of words to the data records of the B7 tape. The logic for specifying the time points will also be generalized. The expanded formatias well as revised usage instructions, will be made available as such programming changes are introduced.

General File 1 (1 record) Identification, BCD EOF Record Format Identification, BCD Epoch Data Record, Floating Point File 2 (arbitrary number of records) Even-Minute Data Record, Floating Point-Even-Minute Data Record, Floating Point EOF End of Tape File 3 (1 record) Identification, BCD

Figure E-1. Binary Ephemeris (B7) Tape Schematic Format

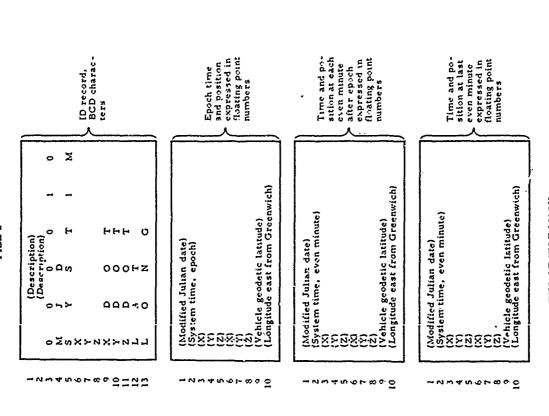
EOF



#### Notes:

- 1. Quantities enclosed in parentheses describe entry content. Characters not enclosed in parentheses indicate literal content (i. e., the BCD representation of a decimal point, or 73, should occupy the last six bits of Word No. 3.
- 2. System time is in seconds from midnight of current day.
- 3. Words No. 2 through 4 designate epoch time.
- 4. Words No. 6 through 12 are used to describe a particular ephemeris run, and should include earth and atmosphere model designations, any unusual parameters associated with the fit which determined the vector, and any other information distinguishing the ephemeris.

Figure N-2. File 1 Detailed Format



Modified Julian date is defined as Julian date minus 2, 400, 000, 5

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Vehicle geodetic latitude is defined as the angle from the equitorial plane to a line normal to the surface of the WGS-1960 ellipsoid and intersecting the satellite position.

System time of the first data record (Record 2, File 2) is time of epoch. System time of the second data record is the first even minute after epoch. Subsequent times are at each even minute.

÷

System time is in seconds from midnight of current day. Record 1, File 2 defines the numbers and positions of the various quantities in the following data records.

X and X quantities are in units of feet and feet per second, latitude in units of degrees positive north and negative south, and longitude in units of degrees positive east in the range 0 to 360 referenced to Greenwich.

۲.

Intermediate even-minute records have formal electricities (irst even-minute record, An arbitrar) number of even-minute records is allowed.

÷

Quantities enclosed in parentheses describe entry content. Characters not enclosed in parentheses indicate literal content.

Notes:

^رة بن

end of file mark

Figure E-3. File 2 Detailed Format

**** 

<u>C</u>.

FILE 3

E	N	D	0	F	T
A	P	E	0	0	0
0	·0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0
. 0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0

End of tape file containing BCD characters

END OF FILE MARK

Figure E-4. Special File Indicating End of Tape

#### APPENDIX F

CHARACTERISTICS OF COW, FINP, AND GRAV SUBROUTINES

#### Appendix F

#### CHARACTERISTICS OF COW, FINP, AND GRAV SUBROUTINES

The material contained in Appendix F consists of information relating to subroutines COW, FINP, and GRAV, and is included to satisfy interest in the specific methods employed by these routines or in details regarding their usage in connection with the TRACE-D program. The following pages have been extracted from a Programming Handbook used by members of the Aerospace Corporation Computation and Data Processing Center.

It should be noted that since the following subroutine writeups are reproductions of instructions appearing in the Handbook, none of the contained symbols, notation, or references should be associated with other portions of this document. Thus, within the context of these extracted pages, reference to Appendices A or B would refer to the material appended to a particular subroutine writeup rather than to Appendices A or B of this primary report.

#### Appendix F

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I2  $\geqslant$  +0; Variable step-size mode of operation is used. I2  $\stackrel{\textstyle >}{<}$  0; Fixed step-size mode of operation is used.

IB; the first IB( $\leq$  N) equations are tested to determine whether it is necessary to halve, or possible to double, the step-size or to proceed with a Cowell integration step.

IR; for a given step-size H, the Cowell integration step is H and the Runge-Kutta integration step is H/IR. If IR = 0 in the calling sequence, it will be set to 4.

ER= 1.0E-S, where S is the number of significant figures desired.

If ER = 0 in the call sequence, it will be set to 1E-9.

HMIN is the minimum step size.

HMAX is the maximum step size, set to lE18 if HMAX = 0 in tacalling sequence.

YMP is the minimum  $y_1$  value allowed for testing. (See Appendix A, RW DE6F for further details.) (Page F-14) If  $y_{min} = 0$  in the calling sequence, it will be set to 1.

DAUX is the location of the entry point of a subroutine which evaluates the second-order derivatives. This must be defined by use of an F car? in the main program and must use COMMON for input and output.

Region T contains the following information prior to set-up entry:

T(2)=x, initial value of independent variable. T(3)=h. value of step-size.

T(3)= h , value of step-size.

T(4)= y₁

 $\begin{array}{c}
\vdots \\
T(3+N) = y_{n}
\end{array}$ values of dependent variables  $y_1$ 

 $T(4+N) = y_1^{(4)}$ values of the first derivatives  $y_1^{(4)}$ 

values of the first derivatives  $y_1'$  $T(3+2N) = y_N''$ 

 $T(\frac{1}{4}+2N) = y_{\frac{1}{2}}^{1}$   $\vdots$   $T(\frac{3}{3}N) = y_{\frac{1}{2}}^{1}$ values of the second derivatives  $y_{\frac{1}{2}}^{1}$  to be supplied by the auxiliary DAUX

Note: This region and the parameter N should be placed in COMMON since it is necessarily referred to in the main program and in the auxiliary. The cell T(1) is set up by the subprogram RW COW and will contain N scaled at 35.



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b. Calling sequence for integrating one step:

CALL ELL (TEST)

Upon return from ELL, TEST will be plus if the integration was a Runge-Kutta step and minus if the integration was a Cowell step.

c. Calling Sequence for Special Usage (See Appendices A and B, RW DE6F)
(Pages F-14 and F-18)

CALL BULL (K,H)

K=1. Running change of coordinates. After any Cowell integration  $\overline{\text{step}}$  (TEST = -), this entry will initialize the beginning of a change of coordinates. Starting with the present values, one begins to save eight consecutive sets of  $y_i$  starting at T(11N+4) (and  $y_i^*$  starting at T(3N+4) if they appear in the  $y_i^*$ ). He continues to use the integration entry above. The next seven integrations will be Cowell steps and all testing will be discontinued during this period. After the eighth set of  $y_i(y_{i7})$ , and  $y_i^*(y_{i7})$  if necessary, have been stored, the user may change the second derivative evaluation routine DAUX and the units of x and h. The units of the eight sets of  $y_i$  and  $y_i^*$  may be changed while storing each set or after all eight sets have been stored. When another integration step is asked for, the routine will perform the change of coordinates and proceed to a Cowell integration step. The routine will be ready for another change of coordinates and will operate under standard conditions.

K=2. Change of step-size, not prior to a change of coordinates. During the integration procedure, the user may wish to output for a specific value of x without interrupting the Cowell/Runge-Kutta integration procedure. Or, he may wish to change the value of the step-size h prior to a running change of coordinates. He can do this after any integration entry with the following procedure:

With the new value of H, CALL BULL (2,H).

Thus, the integration step will be h/R. Continue with the regular integration entry to integrate further.

K=3. This is simply a direct transfer to the Runge-Kutta integration subroutine and should be used to end exactly at a specific value of x. The integration step will be H. This procedure could be used in the middle of the integration procedure if 2. above is used immediately afterwards to restart in the Cowell/Runge-Kutta system.



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If a change of step-size prior to a change of coordinates is desired, the user must prevent the routine from doubling again until after the change of coordinates. The following sequence will accomplish this:

- 1) CALL BULL (4,H), value of H is ignored.
- 2) CALL BULL (2,H) see option K = 2. After the change of coordinates:
- 3) CALL BULL (5,H), value of H is ignored.

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D2 faction 10 RWDE5F Page 1 June 29, 1959

#### Identification

RWDE5F: Floating Point Runge-Kutta Integration of Second-Order Equations 704 - SAP

J. F. Holt, June 29, 1959

Space Technology Laboratories, Inc.

#### Purpose

To solve a set of N simultaneous second-order, ordinary differential equations, in which first derivatives may or may not appear.

#### Restrictions

No internal checks are made for overflow or underflow. The user must provide an auxiliary subroutine which evaluates the second order derivatives. Initial conditions must be set up prior to the first entry.

#### Method

A fourth order Runge-Kutta method* is used for second-order equations of the general type, y''=f(x,y,y'). However, the subroutine can also be used for special second-order equations, y''=f(x,y). (See Reference and Appendix A.) (Page F-8)

While input and output to the routine are single precision, double precision is used internally in the calculation of the dependent variables and the first derivatives in order to control round-off errors. Truncation error can be controlled by choosing an appropriate step-size.

Before returning to the main program, both entries utilize the auxiliary subroutine to compute the second derivatives. Thus, the values of the variables and derivatives are consistent at all times.

#### Usage

Calling sequence to set up a problem:

A. With 1st Derivatives	With 1st Deriva	tives
-------------------------	-----------------	-------

B. Without 1st Derivatives

Loc.	Instruction	Loc.	Instruction
α	TSX DE5F,4	α	TSX DE5F,4
$\alpha$ +l	PZE T,O,V	α+l	MZE T,O,V
C+2	Return	α+2	Return

Calling sequence to integrate all variables one step:

Loc.	Instruction	Comments
α	TSX DE5F+1,4	Integration entry. The step-size
$\alpha$ +l	Return	h may be varied with each entry.

The address T is the first of 9N+3 cells irranged as follows:

Loc.	Contents	Comment.	,
T	PZE N,O,O	N is the number of equations.	Fixed point.

^{*} J. B. Scarborough, Numerical Mathematical Analysis.
3rd Ed., Johns Hopkins Press, Baltimore, 1955. (pp.300-301)



D2 RWDE5F Page 2 June 29, 1959 Usage - continued

Loc.	Contents	Comment
T+l	x	Value of independent variable. Floating point
T+2	h	Value of step-size. Floating point.
T+3	y ₁ thru	Values of dependent variables y _i .
to	$y_{N}^{-}$	Floating point.
T+N+3	yj thru	Values of first derivatives y.
to	y,	Floating point.
T+2N+3	y" thru	Locations where the user's auxiliary subroutine must store the second deriva-
to	$y_N''$	tives $y_1^n$ .
T+3N+3	etc.	6N cells of temporary storage.

T+4N+3 through T+5N+2 and T+8N+3 through T+9N+2 of the 6N cells of temporary storage contain the least significant parts of  $y_1^*$  and  $y_1^*$  respectively. These 2N cells must be preserved throughout the integration procedure. The other 4N cells of temporary storage may be utilized between integration steps. T through T+3N+2 (except for varying the step-size) must also be preserved between integrations.

The address V is the entry point of the auxiliary subroutine which evaluates and stores the second-derivatives  $y_1^u$  and is entered by the calling sequence:

Loc.	Instruction	Comments
α	TSX V,4	Index registers need not be saved by the
α+l	Return	auxiliary subroutine.

User must return via TRA 1,4 from V.

#### Space Requirements

212 cells of program and constants.

3 cells of COMMON through COMMON + 2.

#### Timing

Set-up Time:

.012 (12N + 152) ms. + time for 1 entry to the auxiliary subroutine.

To integrate one step:

1. With 1st Derivatives

.012 (474N + 182) ms. + time for 4 entries to the auxiliary subroutine

2. Without 1st Derivatives

.012 (381N + 182) ms. + time for 3 entries to the auxiliary subroutine

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#### APPENDIX A

#### Method

Reference: J. B. Scarborough, Numerical Analysis, 3rd Ed., JohnsHopkins Press, Baltimore 1955.

Let the system of equations to be solved be given in the form:

$$y_{i}^{"} = f_{i}^{'}(x, y_{1}, ..., y_{n}, y_{1}^{i} ..., y_{n}^{i})$$

$$y_{i}(x_{0}) = y_{10}, y_{i}^{i}(x_{0}) = y_{10}^{i}$$
(i = 1,2,...,N)

Let  $y_{in}$  and  $y_{in}^*$  be the values of  $y_i$  and  $y_i^*$  at  $x = x_n$ ;  $f_{in}$  be the second derivative of  $y_i$  at  $x = x_n$ ; and h be the increment (step-size) of the independent variable x. The Runge-Kutta formulas (Ref. (1), pp.300-301) used in this subroutine are as follows:

$$k_{i1} = h f_{i} (x_{n}, y_{in}, y_{in}^{i})$$

$$k_{i2} = h f_{i} (x_{n} + \frac{h}{2}, y_{in} + \frac{h}{2} y_{in}^{i} + \frac{h}{8} k_{i1}, y_{in}^{i} + \frac{k_{i1}}{2})$$

$$k_{i3} = h f_{i} (x_{n} + \frac{h}{2}, y_{in} + \frac{h}{2} y_{in}^{i} + \frac{h}{8} k_{i1}, y_{in}^{i} + \frac{k_{i2}}{2})$$

$$k_{i4} = h f_{i} (x_{n} + h, y_{in} + h y_{in}^{i} + \frac{h}{2} k_{i3}, y_{in}^{i} + k_{i3})$$

$$\Delta y_{in} = h \left[ y_{in}^{i} + \frac{1}{3} (k_{i1} + k_{i2} + k_{i3}) \right]$$

$$\Delta' y_{in} = \frac{1}{6} \left[ k_{i1} + 2k_{i2} + 2k_{i3} + k_{i4} \right]$$

$$y_{i'n+1} = y_{in} + \Delta y_{in}$$

$$y'_{i'n+1} = y'_{in} + \Delta' y_{in}$$

For the special second-order equation,

3) 
$$y_1'' = f_1(x, y_1,...,y_n)$$
 (1st derivatives missing)

it should be noted that  $k_{12}=k_{13}$ , so that the above formulas reduce to the following Runge-Kutta formulas:

$$k_{12} = h f_{1} (x_{n}, y_{1n})$$

$$k_{12} = h f_{1} (x_{n} + \frac{h}{2}, y_{1n} + \frac{h}{2} y_{1n}^{r} + \frac{h}{8} k_{11})$$

$$k_{13} = h f_{1} (x_{n} + h, y_{1n} + h y_{1n}^{r} + \frac{h}{2} k_{12})$$

$$\Delta y_{1n} = h \left[ y_{1n}^{r} + \frac{1}{6} (k_{11} + 2k_{12}) \right]$$

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4) - continued

$$\Delta' y_{in} = \frac{1}{6} (k_{i1} + 4k_{i2} + k_{i3})$$

$$y_{i'n+1} = y_{in} + \Delta y_{in}$$

$$y'_{i'n+1} = y'_{in} + \Delta' y_{in}$$
where  $k_{i1}$  of (2) is now  $k_{i3}$  of (4).

The subroutine can be made to take advantage of this fact by a simple change in the calling sequence -- thus speeding up the integration process.

The user must provide a starting value for h. Since each integration step is independent, the value of h may be changed at will between integration steps. Negative values of h may be supplied for backward integration.

Except for the initial starting conditions, the values of y, and y' are kept in double precision. All intermediate values, which are supplied for the user's auxiliary program, are done in single precision. The equations of  $\Delta y_i$  and  $\Delta^i y_i$  have been modified as follows:

6) 
$$\Delta^{i}y_{in} = \frac{h}{6}(k_{11}^{*} + 2k_{12}^{*} + 2k_{13}^{*} + k_{14}^{*}),$$

where the  $k^* = f(x,y,y^*)$  (i.e., not multiplied by h).

The values of k* in these equations are accumulated in single precision. These sums are multiplied by h/5, and the most and least significant parts of this product are used to complete the formation of  $y_1, y_1, y_2$  in double precision.

These double precision values of y₁, n+1 and y₁, n+1 are saved for the next integration step.

The values of the variables and derivatives (i.e.,  $x,y,y^2$ , and  $y^2$ ) are consistent at the end of each integration step.

#### Number of Pages

Writeup 4 Listing 4 Total 8

D2 Section 10 RW DE6F Page 1 August 10, 1959

#### Identification

RW DE6F Floating Point Cowell (Second Sum), Runge-Kutta Integration of Second-Order Equations 709/7090 SCAT J. F. Holt and W. G. Strang, August 10, 1959 Space Technology Laboratories, Inc.

#### Purpose

To solve a set of N simultaneous second-order ordinary differential equations, in which first derivatives may or may not appear.

#### Restrictions

No internal checks are made for overflow or underflow. The user must provide an auxiliary subroutine which evaluates the second-order derivatives. The initial conditions must be set up prior to the first entry.

#### Method

A fourth-order Runge-Kutta method**(RW DE5F) is used to start the integration and to change the step-size during integration. A Cowell "second-sum" method based on sixth differences is used to continue the integration. While input to this routine is single precision, double precision is used internally to control round-off errors. Truncation error can be controlled by choosing an appropriate step-size, or by using the variable step-size mode of operation. The set-up entry uses the auxiliary subroutine to evaluate the second-order derivatives. The values of the variables and derivatives are consistent at all times. A detailed description of the method used is available in Appendix A. (Page F-14.)

#### Usage

Calling sequence to set up a problem:

Loc.	Instruction	Comnents
α	TSX DE6F,4	Set up entry
<b>α+1</b>	PO T,0,V	Option, addresses of storage and auxiliary subroutines.
C+2	Pl B,O,R	Option and Parameters
α+3	DEC 1E-S	S is the number of significant figures desired.

^{**} J. B. Scarborough Numerical Mathematical Analysis, Third Edition, Johns Hopkins Press, Baltimore, 1955 (pp. 301-302)

^{*} Modified by Jim Holt, Aerospace Corporation, April 1, 1963.

#### AEROSPACE CORPORATION

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#### Usage (continued)

TOC.	<u>Instruction</u>	Comments
a+4	DEC h _{min}	Minimum step-size. Floating point.
α+5	DEC h	Maximum step-size. Floating point.
<u>α+6</u>	DEC y _{min}	Minimum y value allowed for testing.  Floating point. (See Appendix A for details of y min.) (Page F-14.)

Calling sequence to integrate all variables one step:

α TSX DE6F+1,4 Integration entry.
α+1 Return Sign of AC will be plus if the integration was Runge-Kutta and minus if Cowell.

The address T is the first of 30N+3 cells arranged as follows:

N is the number of equations. Fixed point. T PZE N,0,0 Value of independent variable. Floating 141 x point. T+2 Value of step-size. Floating point. y_i thru Values of the dependent variables y, . T+3 thru T+N+2 Floating point. УN Values of the first derivatives y: T+N+3 thru y; thru T+2N+2 Floating point.  $\lambda_i^N$ y" thru T+2N+3 thru Locations where the usa's auxiliary subroutine must store the second У'n derivatives y". T+3N+2 T+3N+3 thru T+30N+2 27N cells of temporary storage.

T+3N+3 thru T+9N+2 (6N) are used by the Runge-Kutta subroutine (RW DE5F). T+4N+3 thru T+5N+2 and T+8N+3 thru T+9N+2 contain the least significant parts (except when a change of coordinates is in progress) of y; and y;

respectively, and must be preserved throughout the entire integration procedure. The final 21N cells of the T storage are used by the Cowell subroutine and must also be preserved. (See Appendix B for a detailed description of these 27N cells.) (Page F-18.)

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The address V is the entry point of the auxiliary subroutine which evaluates the derivatives y, and is entered by the calling sequence:

Loc. Instruction Comments α TSX V.h Index registers need not be saved in V. α+1 Return Return must be made via a TRA 1,4.

The first B  $(\leqslant \aleph)$  equations are tested to determine whether it is necessary to halve or possible to double the step-size or to proceed with a Cowell integration step.

For a given step-size h, the Cowell integration step is h and the Runge-Kutta integration step is h/R.

#### <u>Options</u>

PO = PZE1st derivatives are present in the evaluation of the second derivatives.

= MZE 1st derivatives are missing in the evaluation of the second derivatives.

Pl = PZE Variable step-size mode of operation is used.

Fixed step-size mode of operation is used. = MZE

If IE-S,  $h_{\min}$ ,  $h_{\max}$ , and  $y_{\min}$  are not specified (0 in first calling sequence), the subroutine will set them to 1E-9, 0, 1E18, and 1., respectively.

Special Usage (See Appendices A and B for complete details.)(PagesF-14, F-16)

The following special usages are possible:

- 1. Running change of coordinates.
- 2. Running start.
- Change of step-size by use in the Cowell/Runge-Kutta system.
- Change of step-size for a final integration or at some prescribed value of x.

Space Required (In addition to T and V).

955 cells of program and constants. (Includes DE5F)

44 cells of COMMON thru COMMON + 43.

#### Timing

Set-up time. (V=time for 1 entry to the auxiliary subroutine.)

.00218 12N + 512O. ms. +iV.

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#### Timing (continued)

#### To integrate one step:

- 1. Runge-Kutta (AC=+ after an integration return.)
  - a) With 1st derivatives.

b) Without 1st derivatives.

.00218 
$$[383N + (8N + 18)/R + 240]$$
 ms. + 3V.

- 2. Cowell (AC= after an integration return.)
  - a) With 1st derivatives.

b) Without 1st derivatives.

3. Change of Coordinates. (In addition to first part of 2A or 2B)

#### Number of Pages

Writeup Appendix A 4 Appendix B

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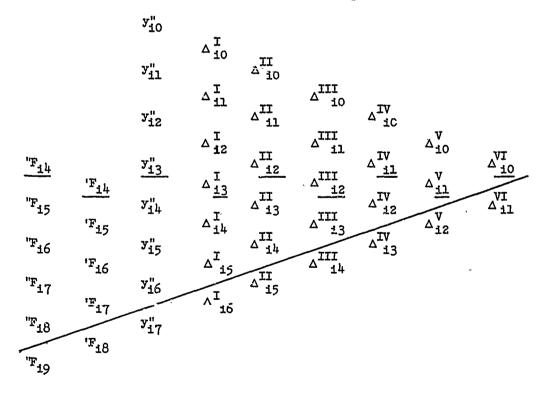
#### APPENDIX A - METHCO

This routine is prepared to solve the following system:

1) 
$$y_{i}^{"} = f_{i}^{(x,y_{i},...,y_{N}, y_{i}^{!},...,y_{N}^{!})}$$
  
 $y_{i}(x_{0}) = y_{i0}^{}, y_{i}^{!}(x_{0}) = y_{i0}^{!}$ 
1 = 1, 2,..., N

In case none of the  $\mathbf{f_i}$  involve the first derivatives  $\mathbf{y_i}$ , time is saved by indicating: this in the set-up. The Runge-Kutta routine RWDE5F is used to start the integration and also to change the step-size h. The user must ask for each integration step, and the routine will follow this sequence:

- 1. R Runge-Kutta steps of size  $\frac{h \text{ start}}{R}$  are taken to obtain  $y_{11}$ ,  $y_{11}$ ,  $y_{11}$ . This is continued until we reach  $y_{16}$ ,  $y_{16}$ ,  $y_{16}$ , after a total of 6R Runge-Kutta steps. The integer R (=4 if unspecified) simply allows Runge-Kutta to operate at a smaller step than the main program.
- 2. For each of the N equations, that part of the difference table above the diagonal line is constructed in three steps:



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#### APPENDIX A (Continued)

First the known  $y_{10}^{"}$  through  $y_{16}^{"}$  are differenced to give the right half of the table. Next are calculated in extra precision:

2) "
$$F_{14} = \frac{y_{13}}{10} - c_0 y_{13} - c_2 \Delta_{12}^{II} - c_4 \Delta_{11}^{IV} - c_6 \Delta_{10}^{VI}$$

3) 
$$P_{14} = \frac{y_{13}^{\prime}}{h} - p_0 y_{13}^{\prime\prime} - p_1 \Delta_{13}^{\prime\prime} - p_2 \Delta_{12}^{\prime\prime\prime} - p_3 \Delta_{12}^{\prime\prime\prime\prime}$$

- 
$$D_{i_4} \Delta_{i1}^{IV}$$
 -  $D_5 \Delta_{i1}^{V}$  -  $D_6 \Delta_{i0}^{VI}$ 

The table is then completed down to the diagonal line, by requiring the difference between any entry and the entry above to equal the entry to the right. The constants used in equations (2) - (7) are given in the description of the Livermore Cowell routine.

3. Before going to a Cowell step, the step-size h is tested. The tests are omitted, however, if the user so indicates in the initial calling sequence, in which case h is fixed. Only the first B equations are used to test, where  $1 \le B \le N$  and B = N if unspecified. We determine—

$$V = \frac{\max}{1 \leqslant i \leqslant B} \left| \frac{\Delta^{V}_{i1}}{\max(y_{i6}, y_{min})} \right|$$
. If  $V \geqslant \frac{10^{3-S}}{h^{2}}$ , then the

ratio of 5th difference to function is too large -- if S decimal places are to be retained at that step. Therefore, h is reduced to h/2 and Runge-Kutta re-entered for another sequence of 6R steps. These begin with the latest calculated values  $(y_{16}, y_{16}')$  and no ground is retraced. The constant  $y_{\min}$  (=1. if unspecified) prevents division by y near a zero; for example, in sine calculation ymin=.1 avoids difficulty near 180°. The integer S, taken as 9 if unspecified, allows a larger h if chosen smaller, say S = 7.

If 
$$\frac{10^{-1-S}}{h^2} < v < \frac{10^{3-S}}{h^2}$$
, we proceed to a Cowell step.

If  $V \leqslant \frac{10^{-1-S}}{h^2}$ , we may be able to dcuble h. We test further to see that  $W = \frac{\max}{1 \leqslant 1 \leqslant B} \quad \left| \frac{\Delta^{VI}_{1}}{\max(y_{16}, y_{\min})} \right| \leqslant \frac{10^{-1-S}}{h^2},$ 

$$W = \frac{\max}{1 \leqslant i \leqslant B} \qquad \frac{\Delta_{ij}^{VI}}{\max(y_{i6}, y_{min})} \leqslant \frac{20^{-1-S}}{h^2},$$

and if so, we re-enter Runge-Kutta after replacing h by 2h, since the step-size h has led to needlessly small difference to function ratios. Of course, h is not halved or doubled if this would violate  $h_{\min}$  or  $h_{\max}$ , which are 0 and  $10^{18}$  if unspecified. unspecified.

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APPENDIX A (Continued)

4. The Cowell integration begins with predictions --

4) 
$$y_{17} = h^2 ("F_{18} + N_0 y_{16}" + N_1 \Delta_{15}^I + \dots + N_6 \Delta_{10}^{VI})$$

5) 
$$y_{17}^{\prime} = h$$
  $('F_{17} + \dot{N}_0 y_{16}^{\prime\prime\prime} + \dot{N}_1 \Delta_{15}^{\prime\prime} + \dots + \dot{N}_6 \Delta_{10}^{\prime\prime\prime})$ 

These use the row of the difference table above the diagonal line; only this row is needed for a Cowell step and is kept up to date at the integration proceeds. (We mention that the above prediction for  $y_{17}^i$  is omitted in the missing first derivative option.) Now from  $y_{17}^i$  and  $y_{17}^i$ , we obtain  $y_{17}^{ii}$  and then complete the row of differences out to  $\Delta_{11}^{VI}$  under the diagonal line in the table. With this row, we calculate final corrected values—

6) 
$$y_{17} = h^2 ("F_{18} + B_0 y_{17}" + \dots + B_6 \Delta_{11}^{VI})$$

7) 
$$y_{17}^{*} = h$$
 ("F₁₇ +  $\dot{B}_{O}y_{17}^{"} + \dots + \dot{B}_{6} \Delta_{11}^{VI}$ )

From these we get corrected values for  $y_{17}^{"}$ , and recalculate the entire row under the diagonal line. This completes the integration step. Using the new row of differences, the next step begins by testing the step-size (i.e., at 3.).

#### Further Properties Of The Frogram

In some problems, information about the first derivative (velocity) may be less reliable than information about the function (position). The user may then choose a "running change of coordinates" or a "running start;" these depend on the fact that with 8 consecutive values of the  $y_1$  (and the  $y_1$  in case first derivatives are present in the  $f_1$ ) the Cowell part of the program can be self-starting. The mathematics is simple: step No. 1 is omitted, and No. 2 modified to calculate " $F_{14}$  and " $F_{15}$  from Eq. (2) (instead of " $F_{14}$  and " $F_{14}$ ). The difference table may again be completed, and Cowell integration begins. The user, having tested the AC to establish that the previous step was a Cowell step, begins a running change of coordinates by setting cell DE6F + 500 to non-zero. He then sets up a counter and begins immediately to store 8 consecutive values of the  $y_1$  starting at T+3+llN (and  $y_1$  starting at T+2+3N, if they appear in the  $f_1$ ). After changing the coordinates the 8th time, the user may change the second derivative evaluation routines; if x and h are to be in new units this should also be done. When another step is asked for, the routine will form a difference table in the new coordinates and proceed to a Cowell step.

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#### APPENDIX A (Continued)

The mechanics of a running start are similar; after going through the set-up routine, the user loads his values of  $y_{i0}$  through  $y_{i7}$  (and the  $y_i^*$  if needed in the  $f_i$ ) into the same locations as above and makes the required transfer.

There may also be occasions on which the user will wish to modify h himself; e.g., if he wishes to produce the numerical solution at some prescribed value of x, or if he wishes to approach a running change of coordinates at a step-size smaller than that being used by the routine. The technique of modifying h is described in Appendix B. (Page F-18.)

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#### APPENDIX B

#### USAGE AND CODING INFORMATION

There are essentially two entries to the subroutine. The first entry must be made once at the beginning to set up the addresses, options, parameters, etc. of the routine for integration of N simultaneous second-order, ordinary differential equations, in which first derivatives may or may not appear. The first entry utilizes the auxiliary subroutine to evaluate the second-order derivatives at the initial conditions. Thus, the initial conditions must be set up prior to the first entry. The second entry may be used any number of times after the first to integrate all y from x to x+h by a Cowell step; or x to x+h/R by a Runge-Kutta step.

The first entry has the following calling sequence:

Loc.	Instruction	Comments
α	TSX DE6F,4	Setup entry.
α+1	PO T,0,V	Option, addresses of storage and auxiliary subroutine.
α+2	Pl B,O,R	Option and parameters.
α+3	DEC 1E-S	S is the number of significant figures desired.
α+4	DEC h _{min}	Minimum step-size. Floating point.
α+5	DEC h	Maximum step-size. Floating point.
α+6	DEC y _{min}	Minimum y, value allowed for testing. Floating point.
α+7	Return	-

(α+1): T is the address of the first word of a block of 30N+3 cells of temporary storage arranged as follows:

Loc.	Contents	Comments
T	PZE N,0,0	N is the number of equations. Fixed point.
T+1	x	Value of independent variable. Floating point.
S+T	h	Value of step-size. Floating point.
T+3 thru	y _i thru]	Values of the dependent variables y _i .
T+N+2	y _N	Floating point.
T+N+3 thru	yi thru	Values of the first derivatives y:
T+2N+2	УN	Floating point.
T+2N+3 thru	y" thru	Locations where the user's auxiliary subroutine must
T+3N+2	y <u>"</u>	store the second derivatives $y_i^{"}$ . Floating point.
T+3N+3 thru	T+30N+2	27N cells of temporary storage.

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#### APPENDIX B (Continued)

The next 27N storages of T are temporary storages. The Runge-Kutta subroutine uses the first 6N cells (T+3N+2 thru T+9N+2) and the Cowell routine uses the final 2lN cells (T+9N+3 thru T+30N+2). However, if a change of coordinates (see SPECIAL USAGE) is made, the Cowell routine will also use the first 6N cells. The attached T STORAGE CHART shows the setup of the entire T region. The N cells starting at T+5N+3 and the N cells starting at T+6N+3 are used by the Runge-Kutta subroutine to compute  $\Delta$ 'y_{iN} and  $\Delta$ y_{iN}. However,  $\triangle$ 'y_{iN} and  $\triangle$  y_{iN} are destroyed before final exit, and these cells contain intermediate values of no significance to the user. The left side of the chart shows the storage for the normal case where 6R Runge-Kutta steps are taken (using the first 9N cells of T for each integration) before an attempt is made to proceed to a Cowell step. At the beginning of each set of R steps, the Cowell subroutine saves the values of the second derivatives (7 sets starting at T+11N+3). In addition, the values of y₁₃ and y'₁₃ are saved, starting at T+9N+3 and T+10N+3 respectively, for use in the central difference equations where "F $_{1\dot{4}}$  and 'F $_{1\dot{4}}$  are calculated. Care must be exercised in using certain values in the temporary region. For instance, after a Runge-Kutta integration step, the most significant values of  $y_i$  and  $y_i^*$ , starting at T+7N+3 and T+3N+3 respectively, will be the values of the previous integration; while the least significant values of  $y_i$  and  $y_i$ , starting at T+8N+3 and T+N+3 respectively, will be the values of the present integration. The Cowell routine also saves the least significant values of  $y_i$  and  $y_i'$  (unless a change of coordinates is in progress) in these same storages at the end of each integration. The llN storages starting at T+19N+3 contain the right half of the N difference tables, an example of which is shown in Appendix A. (p F-14) The right side of the chart shows other values which are stored in the T region during a change of coordinates and will be explained later under SPECIAL USAGE. Even though only one symbol is given  $(y_{10}^*$ , etc.), it should be understood that N values are stored as in the left side of the chart. Thus,  $y_{10}^i$  signifies  $y_{10}^i$ ,  $y_{20}^i$ ,  $y_{30}^i$ , . . . .  $y_{N0}^i$ .

The address V is the entry point of an auxiliary subroutine which the user must provide to evaluate the second derivatives  $y_1^u$ . This subroutine must store  $y_1^u$  in T+2N+3 through T+3N+2 as shown above. The subroutine is entered by the calling sequence:

Loc.	Instruction	Comments
α	TSX V,4	Index registers need not be saved.
α+1	Return	Return via a TRA 1,4.

The derivatives  $y_1^*$  are evaluated during the setup and at the end of each integration step. Thus, the values of the variables and the derivatives are consistent at all times. Extra precision is recommended for the evaluation of the second derivatives  $y_1^*$ .

PO should be set to PZE if the first derivatives are present in the evaluation of the second derivatives. If first derivatives are not present, PO should be set to MZE.

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#### AFFENDIX B (Continued)

 $(\alpha+2)$ : F1 should be set to PZE if a variable step-size is wanted. For a fixed step-size, P1 should be set to MZE. The former allows doubling and halving while the latter restricts the routine to a fixed h. The user may change the mode of operation externally at any time by setting cell DE6F+501 to plus for a variable step-size and minus for a fixed step-size.

Only the first B ( $1 \le B \le N$ ) equations are tested to determine doubling or halving of h. Thus, the user should arrange the N equations in descending order of importance, and specify B accordingly. If B = 0 in the calling sequence, it will be set to N.

R is the ratio of the Covill step-size to the Runge-Kutta step-size. Thus, smaller integration steps can be taken in the Runge-Kutta subroutine by setting R greater than 1. If R=0 in the calling sequence, it will be set to 4. R is saved in the decrement of cell DE6F+516 and in floating point in cell DE6F+517. After any Cowell integration step (AC=-), the user could change R by changing BOTH of these cells.

(c+3): 1E-S is a floating point number where S is the number of significant figures of accuracy desired at each step. The user should experiment with S to fit his own particular problem. The 1 of 1E-S may also be varied from 1 to 9 (1E-S thru 9E-S) for a finer degree of control over the accuracy testing. If 1E-S=0 in the calling sequence, it will be set to 1E-9.

 $(\alpha+4)$ :  $h_{\min}$  is a floating point number giving a lower bound for h.  $h_{\min}$  is saved in cell DE6F+509 and can be changed at any time.

( $\alpha$ +5):  $h_{max}$  is a floating point number giving an upper bound for h. If  $h_{max}$ =0 in the calling sequence, the upper bound will be set to lEl8.  $h_{max}$  is saved in cell DE6F+510 and can be changed at any time.

( $\alpha$ +6):  $y_{min}$  is a positive floating point number which is used in testing the step-size. If  $y_{min}$ =0 in the calling sequence, it will be set to 1.  $y_{min}$  is saved in cell DE6F+511 and can be changed at any time.

If the fixed step-size mode of operation is selected (Pl=MZE), then B, lE-S,  $h_{\min}$ ,  $h_{\max}$ , and  $y_{\min}$  are all ignored by the subroutine. (If Pl=MZE, set B = l for maximum efficiency.)

The integration entry has the following calling sequence:

Loc.	Instruction	Comments						
α	TSX DE6F+1,4	Integrates all variables one step.						
α+l	Return ,							

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#### APPENDIX B (Continueà)

Upon return from the integration entry, the accumulator will be plus if the integration was a Runge-Kutta step and minus if the integration was a Cowell step. Ordinarily, x will have been advanced to x + h/R for a Runge-Kutta step and to x + h for a Cowell step. However, in the variable h mode, it is possible that the value of h in T+2 prior to the integration entry has been changed to h/2 or 2h. In this case, the integration step will be a Runge-Kutta step, and the value of x will be either x + h/2R or x + 2h/R. All values of  $y_1$ ,  $y_1$ , and  $y_1$  will be consistent with the new value of x. The user must never change the value of the step-size h except as described under SPECIAL USAGE.

Special Usage (See Appendix A. Further Properties Of The Program.) (Page F-16.)

1. Running change of coordinates. (Normal Entries.)

After any Cowell integration step (AC=-), the user may initialize the beginning of a change of coordinates by setting cell DE6F+500 to non-zero. Starting with the present values, he begins to save eight consecutive sets of  $y_i$  starting at T+1N+3 (and  $y_i'$  starting at T+3N+3 if they appear in the  $y_i''$ ). He continues to use the integration entry above. The routine will detect the non-zero value stored in cell DE6F+500 and will begin a count-down in cell DE6F+502 from 8 (-1) 0. The next seven integrations will be Cowell steps and all testing will be discontinued during this period. After the eighth set of  $y_i$  ( $y_i$ ), and  $y_i'$  ( $y_i'$ ) if necessary, have been stored (DE6F+502 will have a fixed point 1 in the address), the user may change the second derivative evaluation routine V and the units of x and h. The units of the eight sets of  $y_i$  and  $y_i'$  may be changed while storing each set, or after all eight sets have been stored. When another integration step is asked for, the routine will perform the change of coordinates and proceed to a Cowell integration step. Cell DE6F+500 will be restored to zero, and an 8 will be restored to the address of cell DE6F+502. Thus, the routine will be ready for another change of coordinates and will operate under standard conditions.

2. Running start. (Special Entry.)

A running start is similar to a running change of coordinates except that the user must supply all eight sets of  $y_i$  (and  $y_i$  if necessary) at one time. The following sequence of operations must be followed:

- A. Set up the initial conditions in the T storage. Only N, x, and h are needed, although the eight sets of  $y_i$  (but not  $y_i$ ) can also be stored at this time. x must correspond to  $y_{i,7}$  and h must be the interval at which the  $y_i$  have been obtained. Thus,  $x = x_0 + 7h$  where  $x_0$  corresponds to  $y_0$  (and  $y_0$ ).
- B. Use the first entry calling sequence to set up all parameters and options. The V subroutine will be used but will have no effect on the problem. Also, cells T+4N+3 thru T+5N+2 and T+6N+3 thru T+9N+2 will be set to zero. Thus, the eight sets of y' must be stored AFTER the setup entry.

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#### APPENDIX B (Continued)

- C. Store eight consecutive sets (equal intervals) of  $y_i$  starting at cell T+11N+3 (and eight consecutive sets of  $y_i$  starting at cell T+3N+3, if needed).
- D. Execute the following calling sequence one time:

Loc.	Instruction	Comments				
α	TSX DE6F+16,4	Enter only once.				
α+l	Return	Integrates 1 step.				

- E. Continue with the regular integration entry (TSX DE6F+1,4) to integrate further. Step D integrates all variables one Cowell step, and  $x(x_0 + 7h)$  is advanced to  $x + h(x_0 + 8h)$ . From this point, the routine will operate under normal conditions.
- 3. Change of step-size in the Cowell/Runge-Kutta System. (Special Entry.)

During the integration procedure, the user may wish to output for a specific value of x without interrupting the Cowell/Runge-Kutta integration procedure. Or, he may wish to change the value of the step-size h prior to a running change of coordinates. He can do this after any integration entry with the following procedure:

With the new value of h in the AC,

Loc.	Instruction	Comments
α	TSX DE6F+22,4	Changes h and starts new series of 6R
α+1	Return	Runge-Kutta steps.

Thus, the integration step will be h/R. Continue with the regular integration entry (TSX DE6F+1,4) to integrate further.

If the above procedure is being used to reduce the step-size prior to a change of coordinates, the user must prevent the routine from doubling again until after the change of coordinates. Doubling can be prevented either by storing zero in cell DE6F+510 (h_{max}), or by setting cell DE6F+501 (fixed step-size) negative prior to the above entry. After the change of coordinates, the user may restore the above cells.

4. Change of step-size for a final integration. (Special Entry.)

This is simply a direct transfer to the Runge-Kutta integration subroutine and should be used to end exactly at a specific value of x.

After changing the value of h in T+2,

Loc.	Instruction	Comment
α	TSX DE6F+588,4	Integrates one step with the Runge-Kutta
α+1	Return	subrouting.

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#### APPENDIX B (Continued)

The integration step will be the value of h in T+2. This procedure could be used in the middle of the integration procedure if 3. above (TSX DE6F+22,4) is used immediately afterwards to restart in the Cowell/Runge-Kutta system.

In addition to the user's auxiliary subroutine and the 30N+3 cells for the T storage, the storage requirements are 955 words for RWDE6F plus 141 words of COMMON.

The value of the independent variable x is accumulated in double precision when incremented by h. The least significant part of x is saved in cell DE6F+718.

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				API	PENDIX B	- T STO	RAGE C	HART		gust ]	11, 1959	
T	N	x	h									
<b>T</b> +3	Уl	ъ	•	•	УN	Initial c	Initial conditions which user must supply.					
T+N+3	у;	y'2			$\mathbf{y}_{\mathbf{N}}^{i}$							
T+2N+3	y <u>"</u>	у <u>"</u>			У'n	2nd deriv	2nd derivatives stored by V subroutine.					
T+3N+3	у'	у!	•		УN	Most sign	ifican	t	yio	y"io	Coordinate Change	
T+4N+3	y <u>'</u>	y ₂			$y_N^i$	Least sig	nifica	nt	yil	y"il	8 sets of consecu-	
<b>T</b> +5N+3	Δy' ₁	Δ y ₂ '			Δ V,	Destroyed	by R.	κ.	y _{i2}	y"i2	tive y' saved by	
T+6N+3	$\Delta_{y_1}$	Δyž			Δ _N	Destroyed	by R.I	κ.	у;3	у"3	user if y"=f(x,y,	
T+7N+3	Уı	y ₂		،	y _N .	Most sign	ifican	t	y;4	у"14	y'). Cowell	
E+184T	Уl	ъ2	•		УN	Least sig	nifica	nt	у <u>і</u> 5	у",	stores y" over	
T+9N+3	у ₁₃	y ₂₃	•	•	ъ _{м3}	Saved for	centre	al	y¦6	у ₁₆	y;.	
T+10N+3	у <b>і</b> 3	y23			у <mark>й</mark> З	difference	equa	tions.	y;7	у ₁₇		
T+11N+3	у"10	У ₂₀	•	•	y"o	Normal Ca	se.		y _{i0}		Coordinate Change	
T+12N+3	у <u>"</u> 1	у <u>"</u>			y",	Saved from	n 6r r		yil		8 sets of consecu-	
T+13N+3	y <u>"</u> 2	y"22		•	y"2	steps. U	sed to	form	y _{i2}		tive y saved by	
T+14N+3	у <u>"</u> 3	у <u>"</u> 3	•		у <mark>"</mark> 3	difference	l i		У ₁₃	(	user. Cowell uses	
T+15N+3	y <u>"</u> 4	y <u>"</u> 4	•		y <mark>n</mark> 4	an attemp	t to pr		y ₁₄	!	(with V sub) to	
T+16N+3	y <u>"</u> 5	У <mark>2</mark> 5	•	•	у <u>"</u>	to a Cowe:	Ll step	p.	y ₁₅		form y" above.	
T+17N+3	y <u>"</u> 6	y <u>"</u> 6	•	٠	у <u>"</u>				y ₁₆			
T+18N+3	Used	only i	coor	linat	es chang	ged.			y ₁₇		_	
T+19N+3	7 NI	Δ <u>11</u>	∆ IV	VII	Δ ₁₄	Δ ₁₅ y ₁₆	"F ₁₈	•	l .	'F ₃	llN storages.	
T+19N+14	Δ 20 Σ	ΔSI	V ZZ	Δ ^{II}	I AII	Δ ^I ₂₅ y ₂₆	"F ₂₈				N sets of	
T+19N+25	ΔVI	ν Δ ₃₂	Δ32	Δ ^{II} 3	I 434	Δ ₃₅ y ₃₆			'F3'			
•	Δ ₃₀	- 32	. 34	3	34	35 50	1 1	! ! :		1 1	next Cowell	
•		:	•	:		:   :	Most Sig.	Lst. Sig.	Most Sig.	:  Lst	oll stan	
	, VI	۸۷	TU	-	T T			را ا			,   (See App. A)	
T+30N-8	∇ NO	ANL	V _{IA}	VII VII	I AII	ΔI y"6	"F _{N8}	"F _{n8}	'F _N	'F _N	(Page F-14)	
								Ì				

FORTRAN Subroutine

19 Section 52 RW FINP Page 1 August 24, 1961

#### Identification

RW FINP - Decimal, Octal, BCD, Variable Data Input 7090 FAP Subroutine W. J. Stoner, August 24, 1961 Aerospace Corporation

#### Purpose

To read a set of Hollerith punched data and/or header cards into core with one FORTRAN CALL statement.

To convert the data fields to binary and store in core according to their associated conversion codes.

#### Restrictions

This routine uses (CSH)S to accomplish the BCD card image read. Tape troubles or other errors from this routine are indicated by the print-out of HPR 1,4.

This routine uses (EXE) to print HPR 2, h in case of errors such as non-Hollerith characters, data out of range, illegal format, subscripts too large for the array previously defined, etc. Upon detection of any error, control is immediately sent to (EXE) and no more cards are processed.

#### Method

Decimal numbers are converted to binary integers and then scaled to the indicated power of ten.

Octal numbers are converted to binary integers.

Hollerith words are stored directly.

Range: Decimal to floating binary conversion 10 ** 38 Decimal to fixed binary; 1 to 9 digits*
Decimal integer to binary integer; 1 to 5 digits
Octal integer to binary integer; 0 to 235 - 1

*the magnitude of the number depends upon the location of the decimal point.

#### Usage

#### Format:

 The data card format, available on keypunch form M-1, consists of four subfields containing the conversion code, location, number, and exponent respectively. AEROSPACE CORPORATION

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FORTRAN Subroutine RW FINP Page 2 August 24, 1961

	Data Field	Data Field	Data Field	Data Field
Sub field	ı	2	3	4
Conversion code Location Value Exponent	1 2-6 7-16 17-18	19 20-24 25-34 35-36	37 38-42 43-52 53-54	55 56-60 61-70 71-72

where conversion code is one of the alphabetic characters defined below which specifies the type of conversion to be used on the value field, the location specifies the cell into which the converted value field is to be stored, the value subfield contains the data to be converted, and the exponent contains the power of ten by which floating data is to be scaled, or the location of the binary point of fixed point data.

2. The header card format consists of a conversion code in column 1, a sequence number in columns 2-6 and any Hollerith information in columns 7-72.

#### Decimal Points:

Decimal points may be placed anywhere in the value field except that they may not occur in the same column as a minus sign (ll punch) since this results in a non-Hollerith character. If the decimal point would normally appear at the right of the number punched in the value field, then it is optional.

#### Minus Signs:

Minus signs are 11 punches over any digit of the field. If all of the available columns of the field are not used, minus signs may be punched as the left character of the field.

#### Yalues:

Values must always be written to the extreme left of a field. It is not necessary that the entire field be filled as the first blank denotes the end of value. Superfluous low order zeros should be cmitted as they increase conversion error.

The only exception to partial fields is BCI data where the entire field, including blanks, is stored.

#### Location:

The location may be specified by wither absolute cotal, a variable or array name, or the element subscripts in a one or two dimensional array. If the locations contains five digits, it is interpreted as octal. All five columns must be punched for octal locations.

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If the location contains at least one (1) non-numeric character, it is interpreted as a variable or array name which must appear exactly as given in the CALL statement (see Calling Sequence below). The contents of the number and exponent fields, if they are numeric data, are stored in the cell for the variable or the first cell for the array. This locatio then becomes the origin for all subscript locations following until another variable or array name is encountered. Caution must be taken to load an array name prior to subscript locations.

If the location contains four or fewer digits, it is interpreted as a subscript except for conversion code H explained below. Single dimension array subscripts must be left-justified with leading zeros optional. Two dimension array subscripts must be denoted by two subfields of two columns each containing i and j respectively. The i and j subfields must be separated by a comma and must contain two-digit integers.

If the location is left blank, then the location counter within the routine is decreased by 1 and the associated number is stored in the cell immediately preceding the cell where the last number was stored. Thus, an entire array may be read in by specifying the initial location only.

## Conversion Codes:

Blank: Floating decimal

The number in the value field times the power of ten in the expouent field is converted to floating binary. Checks are made for overflow and format errors.

## F: Fixed decimal

The number in the value field is converted to fixed point binary and stored with the binary point located at the position specified by the number in the exponent field. An overflew electric check is made.

#### I: Decimal integer

The number in the value field is converted to a fixed point binary integer with the binary point following position 17. The exponent field is ignored. A decimal point is considered an error.

#### B: Octal

The value plus exponent fields are converted as a logical octal word.

It is not necessary to include leading zeros but the first octal digit must always occupy the leftmost position of the field.

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#### D: BCI Data

The contents of the value plus exponent fields are interpreted as two BCI words and stored in two consecutive cells in descending order beginning at the location specified by the location field.

#### H: Heading Card

A card with an H in column 1 is considered a BCI heading card. If the location field is blank, the card is ignored. If the location field contains a left-justified one to four digit positive decimal integer V (octal, negative, or variable locations are not permitted), columns 7-72 of the card are stored directly in 11 consecutive words in descending order. The location of the first of these words is calculated by the reutine as HEAD (1+11*(V-1)) where HFAD is defined as the last variable or array named in the CALL statement. Each card may be used as one record of output using FORMAT option A with column 7 of the card providing the code for printer spacing on output.

## A: Variable names as data

The value plus exporant fields are interpreted in a product FAP instruction format AAAAA T DDDDD P where the fields to replace are address, tag, docrement and prefix respectively. The address and decrement fields are defined normally to be 5 characters and the tag and prefix as one octal numeric character each. Any field containing less than the normal number of characters must end with a comma while fields of normal length must not. Any address or decrement field containing less then 5 numeric characters is converted as decimal while those of all 5 numeric characters are converted as octal. Any address or decrement field containing at least one non-numeric character is interpreted as a variable or array name. Variable addresses cause the entire word from the compiler generated calling sequence to be loaded into the location word (i.e., the TSX X is stored in the location specified if X is the variable appearing in the address field). Variable decrements cause the right-most 18 bits from the compiler generated calling sequence to be loaded into the location word's prefix and decrement. Numeric tags and prefixes are loaded directly into the corresponding parts of the location words. Null fields are not loaded. Since the first blank indicates the end of the loading of a word, address only, address-tag, address-tag-decrement, or entire word may be loaded as desired.

#### G: Temporary Origin

The value in the first location field on the card is used as a temporary origin "or vaules. The location is saved and if data cards follow with blank location fields the corresponding data is stored consecutively in descending order beginning with the cell specified in the location in the G card. Columns 7-72 are ignored and may be used to identify the table.

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The first non-blank location starts a new origin. If this non-blank location is a subscript, it references the last variable or array named, which may or may not have been on the G card.

#### J: Transfer

The location specified with this prefix must be an octal address and is the only part of the data field that is interpreted. The subroutine causes a transfer to the octal location specified and does not interpret the remaining fields on the card.

L: Two dimension array imax, jmax definition

The location field contains the name of the array to be loaded. The value field is defined to consist of 2 subfields, separated by a comma, of 2 columns each containing the two-digit decimal integers for  $i_{\max}$  and  $j_{\max}$  respectively where  $i_{\max}$  and  $j_{\max}$  gerafally appear in a DIMENSION statement. The  $i_{\max}$  and  $j_{\max}$  values are retained to compute the successive subscripted locations until redefined. Blank address fields may follow this array definition if successive elements of the array are to be loaded.

M: Two dimension array  $i_{max}$ ,  $j_{max}$  definition

Conversion is identical to L except the entire array is preset to zero.

## E: End Case

This defines an end-of-case and control is returned to the FORTRAN object program. The rest of this field and the remaining fields on the card are ignored.

## Calling Sequence:

The following two types of CALL statements may be used:

- I. CALL FINP (n,X,Y,ZETA,...,mHX(5)Y(5)ZETA(2)...) where
  - A. n is the number of variables and/or arrays in the list, excluding n itself.
  - B. X, Y, ZETA,... are the names of variables and/or arrays restricted to at most 5 characters each, one character of which is non-numeric.
  - C. m is 6 times n. Hence, mH allows for 6n Hollerith characters to follow.



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- D. X(5)Y(5)ZETA(2)... is a list of the items previously maned in exactly the same order with (1) indicating the number, i, of blanks necessary to provide six Kollerith characters for each item. Since each item name is restricted to 5 characters, the minimum value of (1) is (1).
- II. CALL FINP (0) where the number of items is given as zero. This CALL statement must be used only after a CALL statement of type I has been executed. When the subroutine encounters a zero for the number of items, it immediately refers to the last executed CALL FINP with a non-zero number of items for the names of the items to be loaded.

## Space Requirements

613 cells.

## Number of Pages

Writeup 6 Listing 12 Total 18 FORTRAN Subroutine*

CO Section 52 ASC GRAV Page 1 30 August 1963

## Identification

ASC GRAV - Gravitational Force Components 709/7690 FAP Language Subroutine*
R. J. Mercer, 30 August 1963
Aerospace Corporation

#### Purpose

Compute the components of the gravitational force, as derived from a general earth potential function, in a local horizontal coordinate system, and, optionally, obtain by rotation the components in an equatorial system with either the Greenwich meridian or an inertial direction as principal axis.

#### Restrictions

Only 18 cells are currently provided for the storage of  $\sin \lambda_{nm}$  and  $\cos \lambda_{nm}$ . This is sufficient for  $n_2 = 4$ . For larger values of  $n_2$ , the BSS instructions at the end of the subroutine must be appropriately modified.

GRAV refers to, but does not include, the subroutines SIN and COS.

## Mathematical Method

The potential function is

$$U = \frac{\mu}{r} \left[ 1 - \sum_{n=2}^{n} J_n \left( \frac{e}{r} \right)^n P_n(\sin \varphi) + \sum_{n=2}^{n} \sum_{m=1}^{n} J_{nm} \left( \frac{e}{r} \right)^n P_n^m(\sin \varphi) \cos m \left( \lambda - \lambda_{nm} \right) \right]$$

where

is the product GM of the Newtonian gravitational constant and the mass of the earth.

r, φ, λ are the geocentric distance, geocentric latitude and (east) longitude of a point,

a is the mean equatorial radius of the earth,

J_n, J_{nm} are numerical coefficients,

P_n is the Legendre polynomial of the first kind of degree n,

Pn is the Legendre associated function of the first kind,

 $\lambda_{mn}$  are longitudes associated with the  $I_{nm}$ .

^{*} Easily converted to SCAT; see Usage.



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In the local horizontal coordinate system, in which the coordinate axes are directed Up (along the radius vector), East and North (see figure), the force

$$\begin{split} g_U &= \frac{\partial U}{\partial r} \\ &= -\frac{\mu}{r^2} \left[ 1 - \frac{\Sigma}{n=2} \left( n+1 \right) J_n \left( \frac{a_e}{r} \right)^n P_n \left( \sin \phi \right) \right. \\ &+ \frac{n_e}{n=2} \frac{n}{m=1} \left( n+1 \right) J_{nm} \left( \frac{a_e}{r} \right)^n P_n^m \left( \sin \phi \right) \cos m \left( \lambda - \lambda_{nm} \right) \right] \\ g_E &= \frac{1}{r \cos \phi} \frac{\partial U}{\partial \lambda} \\ &= -\frac{\mu}{r^2 \cos \phi} \frac{\Sigma}{n=2} \frac{\Sigma}{m=1} m J_{nm} \left( \frac{a_e}{r} \right)^n P_n^m \left( \sin \phi \right) \sin m \left( \lambda - \lambda_{nm} \right) \\ g_N &= \frac{1}{r} \frac{\partial U}{\partial \phi} \\ &= \frac{\mu}{r^2} \left[ -\frac{n_1}{n=2} J_n \left( \frac{a_e}{r} \right)^n P_n^t \left( \sin \phi \right) \cos \phi \right. \\ &+ \frac{n_e}{n=2} \frac{\Sigma}{m=1} J_{nm} \left( \frac{a_e}{r} \right)^n P_n^{mt} \left( \sin \phi \right) \cos \phi \cos m \left( \lambda - \lambda_{nm} \right) \right] \end{split}$$

The Legendre functions and their derivatives are computed from the recursion formulas

$$\begin{split} P_{n} & \left( \sin \phi \right) = \frac{-\left( n - 1 \right)}{n} P_{n-2} \left( \sin \phi \right) + \left( 2n - 1 \right) \sin \phi P_{n-1} \left( \sin \phi \right) \\ P_{n}^{t} & \left( \sin \phi \right) = \sin \phi P_{n-1}^{t} \left( \sin \phi \right) + n P_{n-1} \left( \sin \phi \right) \\ \frac{P_{n}^{m} \left( \sin \phi \right)}{\cos \phi} = \frac{-\left( n + m - 1 \right)}{n} \frac{P_{n-2}^{m} \left( \sin \phi \right)}{\cos \phi} + \left( 2n - 1 \right) \sin \phi \frac{P_{n-1}^{m} \left( \sin \phi \right)}{\cos \phi} \\ \frac{P_{m}^{m} \left( \sin \phi \right)}{\cos \phi} = 1 \cdot 3 \cdot \dots \cdot (2m - 1) \left( \cos \phi \right)^{m-1} \end{split}$$



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$$P_n^{m^t}(\sin \varphi) \cos \varphi = (n+1) \sin \varphi \frac{P_n^m(\sin \varphi)}{\cos \varphi} - (n-m+1) \frac{P_{n+1}^m(\sin \varphi)}{\cos \varphi}$$

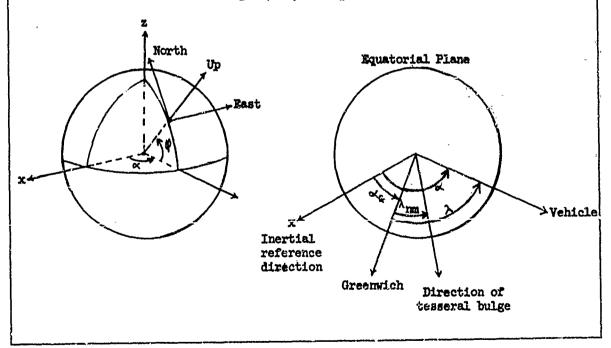
The use of the quotient  $\frac{P_n^m \; (\sin \phi)}{\cos \phi}$  avoids numerical difficulties at high latitudes in the equation for  $g_n$  .

The components of the force vector in an equatorial coordinate system with  ${\bf x}$  in the direction of the Greenwich meridian are

$$\begin{pmatrix} g_{\chi} \\ g_{y} \\ g_{z} \end{pmatrix} = \begin{pmatrix} \cos \phi \cos \lambda & -\sin \lambda & -\sin \phi \cos \lambda \\ \cos \phi \sin \lambda & \cos \lambda & -\sin \phi \sin \lambda \\ +\sin \phi & 0 & \cos \phi \end{pmatrix} \begin{pmatrix} g_{U} \\ g_{E} \\ g_{N} \end{pmatrix}$$

The components in an equatorial inertial coordinate system with x in the direction of  $\gamma$  (vernal equinox) are obtained by a similar transformation in which  $\alpha$  replaces  $\lambda$ .

Optionally, either longitude  $\lambda$  or both  $\alpha$  and  $\alpha_G$  (inertial right ascensions of the vehicle and Greenwich - see figure) may be input.



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#### Usage

The subroutine is written in the FAP language for use with FORTRAN II programs, in which arrays are stored backwards. With three simple changes, which are carefully described in the comments of the symbolic cards, the subroutine can be assembled for use with machine language programs in which arrays are stored forwards.

The subroutine has an initial, a regular and a third entry point. In the initial entrance, all addresses are set up from the calling sequence, and certain preliminary computations are performed. At the regular entrance (for which no calling sequence is used), the force components are evaluated using the options and the locations of the constants and variables (input and output) specified in the initial entrance calling sequence.

The initial entry to the FAP version must be with the statement:

CALL GRAV1 (GM, AE, FN1, FJN, FN2, FJNM, FLNM, ØP1, ØP2, ARG, GLH, GX, ØP3, A, B, C, D, E, F, G, R, U)

Only address set ups and preliminary computations are performed; the acceleration components are not evaluated. The regular entry is with the statement

CALL GRAV

The machine language version is entered initially with

TSX GRAV + 2, 4

PZE GM

PZE AE

: (etc.)

PZE U

Normal return

and for the computation of acceleration components with

TSX GRAY, 4

Normal return

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In numerical integration, it is often unnecessary to recompute the perturbative accelerations for the corrector step. A third entry

CALL GRAV2

or TSX GRAV + 3, 4

provides this option. When so used, the subroutine uses the last-computed summations, but recomputes  $\mu$  and the rotation matrix before forming  $g_U$ ,

 $g_E$ ,  $g_N$ ,  $g_x$ ,  $g_y$ ,  $g_z$  and U.

The subroutine arguments are the 22 locations

GM.  $GM = \mu$ 

AE a

FNL n (floating point)

FIN Array containing J₂, J₃, ..., J_{n₁}

FN2 n_p (floating point)

FJNM Array containing J₂₁, J₃₁, ..., J_{n2}1, J₂₂, J₃₂, ..., J_{n2}2, J₃₃, ..., J_{n2}n₂

Film Array containing  $\lambda_{rem}$  (in degrees) in like order

pPl Zero for longitude input; non-zero for right ascension input (see ARG).

Positive for rotation of output to inertial coordinates (right ascension input, ppl \neq 0, must be used); negative for rotation of output to earthfixed system; zero for no output rotation.

ARG Array containing, in order, the input variables

r,  $\sin \varphi$ ,  $\cos \varphi$ ,  $\begin{cases} \sin \lambda, \cos \lambda & \text{if } \not \in \mathbb{N} = 0 \\ \sin \alpha_{G}, \cos \alpha_{G}, \sin \alpha, \cos \alpha & \text{if } \not \in \mathbb{N} \neq 0 \end{cases}$ 

GLH Output array containing accelerations  $g_U$ ,  $g_E$ ,  $g_N$  in basic local horizontal coordinate system.

Output array containing (if  $p_2 \neq 0$ ) accelerations in chosen (see  $p_2$ ) equatorial coordinate system.

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- Mon-zero if individual terms in the components of GLH are to be saved in regions A, B, ..., G; Zero if not. (Regions A, B, ..., G are not cleared by GRAV.)
- A Array containing (if  $\phi P3 \neq 0$ )  $A_n = -(n+1) J_n \left(\frac{a_e}{r}\right)^n P_n$  ( $\sin \varphi$ ) for  $n = 2, ..., n_1$ .
- B Array;  $B_{nm} = (n+1) J_{nm} \left(\frac{3}{r}\right)^n P_n^m (\sin \varphi)$  in order as in FJNM.
- C Array;  $C_{nm} = \frac{m}{\cos \varphi} J_{nm} \left(\frac{a_e}{r}\right)^n P_n^m (\sin \varphi)$
- D Array;  $D_n = J_n \left(\frac{a_e}{r}\right)^n P_n^t (\sin \varphi) \cos \varphi$
- E Array;  $E_{nm} = -J_{nm} \left(\frac{a_e}{r}\right)^n P_n^{m'} (\sin \varphi) \cos \varphi$
- F Array;  $\sin m(\lambda \lambda_{mn})$  in order as in FURM
- G Array;  $\cos m(\lambda \lambda_{nm})$  in like order
- R Rotation matrix, stored by columns, specified by \$P2.
- U The value of the potential function.

## Space Required

482 cells.

## Checkout

All intermediate results were hand computed for a case with  $n_1 = 4$ ,  $n_2 = 2$ . Spot checks were made on many other cases, in which the various options were tested.

#### Number of Pages

Writeup 6

## REFERENCES

- 1. R. J. Mercer, et al.. <u>TRACE-Aerospace Orbit Determination</u> Program, TDR-269(4110-04)-1, Aerospace Corp., El Segundo. Calif. (1964).
- 2. C. S. Christensen. A. R. Jacobsen. and R. J. Mercer, TRACE-C Powered Flight Trajectory Determination Program. TOR 469(5352)-1. Aerospace Corp., El Segundo, Calif. (1965).
- 3. V. N. Faddeeva, <u>Computational Methods of Linear Algebra</u>, Dover Publications Inc., New York (1959), p. 81.
- 4. Henry Scheffé, The Analysis of Variance. John Wiley & Sons Inc., New York (1961), p. 14.
- 5. T. A. Magness, and J. B. McGuire, Statistics of Crbit Determination-Correlated Observations, 8976-6001-RU-000, Space Technology Labs., (TRW Systems, TRW Inc.), Redondo Beach, Calif. (15 December 1961), p. iv.
- 6. R. J. Mercer, Physical Constants for Satellite Calculations, TOF-469(5110-02)-2, Aerospace Corp. El Segundo, Calif. (1965).
- 7. IRIG Standard Format for Data Transmission. IRIG Document No. 102-63, Inter-Range Instrumentation Group of the Range Commander's Council: copies may be requested from: Secretariat. Range Commander's Council, Attn: ChSc-RCC, White Sands Missile Range, New Mexico 88002, or Defense Documentation Center, Cameron Station, Alexandria, Virginia 22314. (1964).
- 8. R. H. Hudson, <u>Subtabulated Lunar and Planetary Ephemerides</u>, Technical Release No. 34-239. Jet Propulsion Lab., California Institute of Technology, Pasadena, Calif (2 November 1960).
- 9. R. J. Mercer, "RW FEQX." <u>Programming Handbook</u>, Computation and Data Processing Center. Aerospace Corp., El Segundo, Calif. (27 June 1960). Also available as SHARE Distribution No. 946. Data Processing Div., International Business Machines Corp.. White Plains, New York.
- 10. Planetary Coordinates for the Years 1960-1980. H. M. Almanac Office, Her Majesty's Stationery Office, London (1958), pp. xix, 109.

## REFERENCES (cont.)

- 11. The ARDC Model Atmosphere, 1959. Geophysics Research Directorate, Air Force Cambridge Research Center. Bedford, Mass.
- 12. Density of the Atmosphere, LMSC-A082333, Missiles and Space Div., Lockheed Aircraft Corp. (1 November 1961).
- 13. J. F. Holt, and W. G. Strang, "RW DE6F," Programming Handbook, Computation and Data Processing Center, Aerospace Corp., El Segundo, Calif. (10 August 1959). Also available as SHARE Distribution No. 775, Data Processing Div., International Business Machines Corp., White Plains, New York.
- 14. F. L. Alt, ed., Advances in Computers, Vol. 3, Academic Press Inc., (1962), especially pp. 42 ff.
- 15. F. B. Hildebrand, Introduction to Numerical Analysis, McGraw-Hill Book Company, New York (1956).
- 16. T. E. Sterne, An Introduction to Celestial Mechanics, Interscience Publishers Inc., New York (1960), Chap. 5.
- 17. F. R. Moulton, An Introduction to Celestial Mechanics, The Macmillan Company, New York (1914), pp. 237 ff.
- 18. Harald Cramer, <u>Mathematical Methods of Statistics</u>, Princeton University Press, Princeton, New Jersey (1946), p. 301.

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11 SUPPLEMENTARY NOTES	12. SPONSORING MILITA	RY ACTIV	//TY				
	Space Systems Division						
	1	ce Systems Command					
	Los Angeles, California						
13 ABSTRACT							
The TRACE-D computer program i	is designed for a	ise on	the IBM				
7094 machine as the principal tool in design and analysis studies of							
all aspects of orbital operations. Its principal characteristics are							
completeness of the equations of motion, a comprehensive set of							
differential correction parameters, and the ability to simultaneously process observations of several satellites taken by a number of							
different types of sensors. The report includes objectives, equations,							
program structure, and complete instructions for input data pre-							
paration and program operation.							
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KEY WORDS

Differential Correction Geopotential Models Least Squares
Orbit Determination Sensor Calibration TRACE Tracking Program
Tracking System Analysis
Trajectory Computations
Variational Equations

Abstract (Continued)

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